



**FINAL JEE–MAIN EXAMINATION – JANUARY, 2023**  
**Held On Wednesday 1st February, 2023**  
**TIME : 9 : 00 AM to 12 : 00 NOON**

**SECTION-A**

**Q.1** Match the List I with List II

|    | List I                  |      | List II                            |
|----|-------------------------|------|------------------------------------|
| A. | Intrinsic Semiconductor | I.   | Fermi-level near conduction band   |
| B. | n-type semiconductor    | II.  | Fermi-level at middle              |
| C. | p-type semiconductor    | III. | Fermi-level near valence band      |
| D. | Metals                  | IV.  | Fermi-level inside conduction band |

Choose the **correct** answer from the options given below:

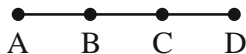
- (1) (A) → I, (B) → II, (C) → III, (D) → IV
- (2) (A) → II, (B) → I, (C) → III, (D) → IV
- (3) (A) → II, (B) → III, (C) → I, (D) → IV
- (4) (A) → III, (B) → I, (C) → II, (D) → IV

**Official Ans. by NTA (3)**

**Ans. (3)**

**Sol.** Based on theory.

**2.** An object moves with speed  $v_1$ ,  $v_2$ , and  $v_3$  along a line segment AB, BC and CD respectively as shown in figure. Where  $AB = BC$  and  $AD = 3 AB$ , then average speed of the object will be :



- (1)  $\frac{(v_1 + v_2 + v_3)}{3}$
- (2)  $\frac{v_1 v_2 v_3}{3(v_1 v_2 + v_2 v_3 + v_3 v_1)}$
- (3)  $\frac{3v_1 v_2 v_3}{v_1 v_2 + v_2 v_3 + v_3 v_1}$
- (4)  $\frac{(v_1 + v_2 + v_3)}{3v_1 v_2 v_3}$

**Official Ans. by NTA (3)**

**Ans. (3)**

**Sol.**  $AB = x$

$BC = x$

$2x + CD = 3x$

$CD = x$

$$\langle v \rangle = \frac{3x}{\frac{x}{v_1} + \frac{x}{v_2} + \frac{x}{v_3}} = \frac{3v_1 v_2 v_3}{v_2 v_3 + v_1 v_3 + v_1 v_2}$$

**3.** Given below are two statements :

**Statement-I:** Acceleration due to gravity is different at different places on the surface of earth.

**Statement-II:** Acceleration due to gravity increases as we go down below the earth's surface.

In the light of the above statements, choose the **correct** answer from the options given below

- (1) Both Statement I and Statement II are true
- (2) Both Statement I and Statement II are false
- (3) Statement I is true but Statement II is false
- (4) Statement I is false but Statement II is true

**Official Ans. by NTA (3)**

**Ans. (3)**

**Sol.**  $g_{eff} = g - \omega^2 R_e \sin^2 \theta$ ,  $\theta \rightarrow$  co-latitude angle

$$g_{eff} = g \left( 1 - \frac{d}{R_e} \right), d \text{ here depth}$$

**4.** Match the List-I with List-II.

|    | List I                        |      | List II                   |
|----|-------------------------------|------|---------------------------|
| A. | AC generator                  | I.   | Presence of both L and C  |
| B. | Transformer                   | II.  | Electromagnetic Induction |
| C. | Resonance phenomenon to occur | III. | Quality factor            |
| D. | Sharpness of resonance        | IV.  | Mutual Inductance         |

Choose the **correct** answer from the options given below:

- (1) A-IV, B-II, C-I, D-III
- (2) A-II, B-I, C-III, D-IV
- (3) A-II, B-IV, C-I, D-III
- (4) A-IV, B-III, C-I, D-II

**Official Ans. by NTA (3)**

**Ans. (3)**

**Sol.** Based on theory.

5. Match the List-I with List-II:

|    | List I      |      | List II  |
|----|-------------|------|--|
| A. | Microwaves  | I.   | Radio active decay of the nucleus                          |
| B. | Gamma rays  | II.  | Rapid acceleration and deceleration of electron in aerials |
| C. | Radio waves | III. | Inner shell electrons                                      |
| D. | X-rays      | IV.  | Klystron valve   |

Choose the **correct** answer from the options given below:

- (1) A-I, B-II, C-III, D-IV
- (2) A-IV, B-I, C-II, D-III
- (3) A-I, B-III, C-IV, D-II
- (4) A-IV, B-III, C-II, D-I

**Official Ans. by NTA (2)**

**Ans. (2)**

**Sol.** Based on theory.

6. If earth has a mass nine times and radius twice to the of a planet P. Then  $\frac{v_e}{3} \sqrt{x} \text{ ms}^{-1}$  will be the minimum velocity required by a rocket to pull out of gravitational force of P, where  $v_e$  is escape velocity on earth. The value of x is

- (1) 2
- (2) 3
- (3) 18
- (4) 1

**Official Ans. by NTA (1)**

**Ans. (1)**

**Sol.**  $v_{(\text{escape})\text{plant}} = \sqrt{\frac{2GM_p}{R_p}}$

$$= \sqrt{\frac{2G\left(\frac{M_e}{9}\right)}{\left(\frac{R_e}{2}\right)}} = \frac{v_e \sqrt{2}}{3} \therefore x = 2$$

7. 'n' polarizing sheets are arranged such that each makes an angle  $45^\circ$  with the preceding sheet. An unpolarized light of intensity  $I$  is incident into this arrangement. The output intensity is found to be

$\frac{I}{64}$ . The value of  $n$  will be:

- (1) 3
- (2) 6
- (3) 5
- (4) 4

**Official Ans. by NTA (2)**

**Ans. (2)**

**Sol.** After passing through first sheet

$$I_1 = \frac{I}{2}$$

After passing through second sheet

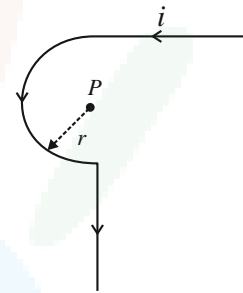
$$I_2 = I_1 \cos^2(45^\circ) = \frac{I}{4}$$

After passing through  $n^{\text{th}}$  sheet

$$I_n = \frac{I}{2^n} = \frac{I}{64}$$

$$n = 6$$

8. Find the magnetic field at the point P in figure. The curved portion is a semicircle connected to two long straight wires.



- (1)  $\frac{\mu_0 i}{2r} \left(1 + \frac{2}{\pi}\right)$
- (2)  $\frac{\mu_0 i}{2r} \left(1 + \frac{1}{\pi}\right)$
- (3)  $\frac{\mu_0 i}{2r} \left(\frac{1}{2} + \frac{1}{2\pi}\right)$
- (4)  $\frac{\mu_0 i}{2r} \left(\frac{1}{2} + \frac{1}{\pi}\right)$

**Official Ans. by NTA (3)**

**Ans. (3)**

**Sol.**  $B_p = \left(\frac{\mu_0 i}{4r} + \frac{\mu_0 i}{4\pi r}\right) = \frac{\mu_0 i}{2r} \left(\frac{1}{2} + \frac{1}{2\pi}\right)$

9. Which of the following frequencies does not belong to FM broadcast.

- (1) 106 MHz
- (2) 64 MHz
- (3) 99 MHz
- (4) 89 MHz

**Official Ans. by NTA (2)**

**Ans. (2)**

**Sol.** FM broadcast range is 88MHz to 108MHz

10. A steel wire with mass per unit length  $7.0 \times 10^{-3} \text{ kg m}^{-1}$  is under tension of 70 N. The speed of transverse waves in the wire will be:

- (1)  $200 \pi \text{ m/s}$
- (2) 100 m/s
- (3) 10 m/s
- (4) 50 m/s

**Official Ans. by NTA (2)**

**Ans. (2)**

**Sol.**  $v = \sqrt{\frac{T}{\mu}} = \sqrt{\frac{70}{70 \times 10^{-3}}} = 100 \text{ m/s}$

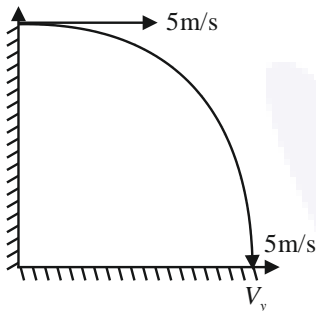
11. A child stands on the edge of the cliff 10 m above the ground and throws a stone horizontally with an initial speed of  $5 \text{ ms}^{-1}$ . Neglecting the air resistance, the speed with which the stone hits the ground will be \_\_\_\_\_  $\text{ms}^{-1}$  (given,  $g = 10 \text{ ms}^{-2}$ ).

- (1) 20 (2) 15  
(3) 30 (4) 25

Official Ans. by NTA (2)

Ans. (2)

Sol.



$$v_y = \sqrt{2gh} = \sqrt{200}$$

$$v_{net} = \sqrt{25 + 200} = 15 \text{ m/s}$$

12. A proton moving with one tenth of velocity of light has a certain de Broglie wavelength of  $\lambda$ . An alpha particle having certain kinetic energy has the same de-Broglie wavelength  $\lambda$ . The ratio of kinetic energy of proton and that of alpha particle is:

- (1) 2 : 1 (2) 4 : 1  
(3) 1 : 2 (4) 1 : 4

Official Ans. by NTA (2)

Ans. (2)

Sol.  $KE = \frac{p^2}{2m} = \frac{h^2}{2m\lambda^2}$

$$\frac{KE_p}{KE_\alpha} = \frac{m_\alpha}{m_p} = 4 : 1$$

13. A sample of gas at temperature  $T$  is adiabatically expanded to double its volume. The work done by the gas in the process is (given,  $\gamma = \frac{3}{2}$ ):

- (1)  $W = TR [\sqrt{2} - 2]$  (2)  $W = \frac{T}{R} [\sqrt{2} - 2]$   
(3)  $W = \frac{R}{T} [2 - \sqrt{2}]$  (4)  $W = RT [2 - \sqrt{2}]$

Official Ans. by NTA (4)

Ans. (4)

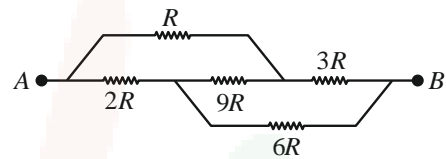
Sol.  $T_1 V_1^{\gamma-1} = T_2 V_2^{\gamma-1}$

$$TV^{1/2} = T_2 (2V)^{1/2}$$

$$T_2 = \frac{T}{\sqrt{2}}$$

$$W = \frac{R(T_1 - T_2)}{\gamma - 1} = \frac{R\left(T - \frac{T}{\sqrt{2}}\right)}{\frac{1}{2}} = RT(2 - \sqrt{2})$$

14. The equivalent resistance between  $A$  and  $B$  of the network shown in figure:

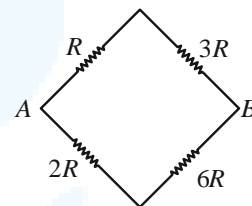


- (1)  $11 \frac{2R}{3}$  (2)  $14R$   
(3)  $21R$  (4)  $\frac{8}{3}R$

Official Ans. by NTA (4)

Ans. (4)

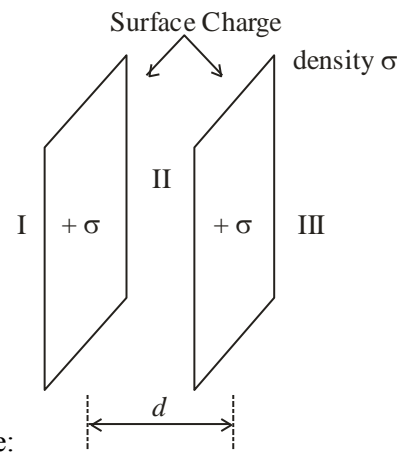
Sol. Wheat stone bridge is in balanced condition.



$$\frac{1}{R_{eq}} = \frac{1}{4R} + \frac{1}{8R}$$

$$R_{eq} = \frac{8R}{3}$$

15. Let  $\sigma$  be the uniform surface charge density of two infinite thin plane sheets shown in figure. Then the electric fields in three different region  $E_I$ ,  $E_{II}$  and  $E_{III}$  are:



$E_{III}$  are:



$$(1) \vec{E}_I = \frac{2\sigma}{\epsilon_0} \hat{n}, \vec{E}_{II} = 0, \vec{E}_{III} = \frac{2\sigma}{\epsilon_0} \hat{n}$$

$$(2) \vec{E}_I = 0, \vec{E}_{II} = \frac{\sigma}{\epsilon_0} \hat{n}, \vec{E}_{III} = 0$$

$$(3) \vec{E}_I = \frac{\sigma}{2\epsilon_0} \hat{n}, \vec{E}_{II} = 0, \vec{E}_{III} = \frac{\sigma}{2\epsilon_0} \hat{n}$$

$$(4) \vec{E}_I = -\frac{\sigma}{\epsilon_0} \hat{n}, \vec{E}_{II} = 0, \vec{E}_{III} = \frac{\sigma}{\epsilon_0} \hat{n}$$

**Official Ans. by NTA (4)**

**Ans. (4)**

**Sol.** Assuming RHS to be  $\hat{n}$

$$\vec{E}_I = \frac{\sigma}{2\epsilon_0} (-\hat{n}) + \frac{\sigma}{2\epsilon_0} (-\hat{n}) = -\frac{\sigma}{\epsilon_0} \hat{n}$$

$$\vec{E}_{II} = 0,$$

$$\vec{E}_{III} = \frac{\sigma}{2\epsilon_0} (\hat{n}) + \frac{\sigma}{2\epsilon_0} (\hat{n}) = \frac{\sigma}{\epsilon_0} (\hat{n})$$

**16.** A mercury drop of radius  $10^{-3}$  m is broken into 125 equal size droplets. Surface tension of mercury is  $0.45 \text{ Nm}^{-1}$ . The gain in surface energy is:

- (1)  $2.26 \times 10^{-5} \text{ J}$                       (2)  $28 \times 10^{-5} \text{ J}$   
 (3)  $17.5 \times 10^{-5} \text{ J}$                       (4)  $5 \times 10^{-5} \text{ J}$

**Official Ans. by NTA (1)**

**Ans. (1)**

**Sol.** Initial surface energy =  $0.45 \times 4\pi (10^{-3})^2$

$$\frac{4}{3} \pi (10^{-3})^3 = 125 \times \frac{4\pi}{3} R_{\text{new}}^3$$

$$\therefore 10^{-3} = 5 R_{\text{new}}$$

$$\therefore R_{\text{new}} = \frac{10^{-3}}{5} \text{ m}$$

$$\text{So, final surface energy} = 0.45 \times 125 \times 4\pi \left(\frac{10^{-3}}{5}\right)^2$$

$$\text{Increase in energy} = 0.45 \times 4\pi \times (10^{-3})^2 \left[\frac{125}{25} - 1\right]$$

$$= 4 \times 0.45 \times 4\pi \times 10^{-6}$$

$$= 2.26 \times 10^{-5} \text{ J}$$

**17.** The mass of proton, neutron and helium nucleus are respectively 1.0073 u, 1.0087 u and 4.0015u. The binding energy of helium nucleus is:

- (1) 14.2 MeV                      (2) 28.4 MeV  
 (3) 56.8 MeV                      (4) 7.1 MeV

**Official Ans. by NTA (2)**

**Ans. (2)**

**Sol.** B.E of Helium =  $(2m_p + 2m_n - m_{He}) c^2$   
 = 28.4 MeV

**18.**  $\left(P + \frac{a}{V^2}\right) (V - b) = RT$  represents the equation of

state of some gases. Where  $P$  is the pressure,  $V$  is the volume,  $T$  is the temperature and  $a, b, R$  are the constants. The physical quantity, which has dimensional formula as that of  $\frac{b^2}{a}$ , will be :

- (1) Bulk modulus                      (2) Modulus of rigidity  
 (3) Compressibility                      (4) Energy density

**Official Ans. by NTA (3)**

**Ans. (3)**

**Sol.**  $[b] = [V]$

$$\left[\frac{a}{b^2}\right] = [P] \quad \therefore \left[\frac{b^2}{a}\right] = \frac{1}{[P]} = \frac{1}{[B]} = [K]$$

**19.** The average kinetic energy of a molecule of the gas is

- (1) proportional to absolute temperature  
 (2) proportional to volume  
 (3) proportional to pressure  
 (4) dependent on the nature of the gas

**Official Ans. by NTA (1)**

**Ans. (1)**

**Sol.** Basic theory

Translational *K.E* on average of a molecule is  $\frac{3}{2}$

KT which is independent of nature, pressure and volume.

**20.** A block of mass 5 kg is placed at rest on a table of rough surface. Now, if a force of 30N is applied in the direction parallel to surface of the table, the block slides through a distance of 50 m in an interval of time 10s. Coefficient of kinetic friction is (given,  $g = 10 \text{ ms}^{-2}$ ):

- (1) 0.60                                      (2) 0.75  
 (3) 0.50                                      (4) 0.25

**Official Ans. by NTA (3)**

**Ans. (3)**

**Sol.**  $S = ut + \frac{1}{2} at^2$

$$50 = 0 + \frac{1}{2} \times a \times 100$$

$$a = 1 \text{ m/s}^2$$

$$F - \mu mg = ma$$

$$30 - \mu \times 50 = 5 \times 1$$

$$50\mu = 25$$

$$\mu = \frac{1}{2}$$



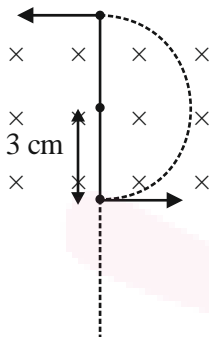
SECTION-B

21. A charge particle of  $2 \mu\text{C}$  accelerated by a potential difference of  $100\text{V}$  enters a region of uniform magnetic field of magnitude  $4 \text{ mT}$  at right angle to the direction of field. The charge particle completes semicircle of radius  $3 \text{ cm}$  inside magnetic field. The mass of the charge particle is  $\_\_\_\_ \times 10^{-18} \text{ kg}$ .

Official Ans. by NTA (144)

Ans. (144)

Sol.  $r = \frac{mv}{qB} = \frac{\sqrt{2km}}{qB}, m = \frac{r^2 q^2 B^2}{2k}$



$$m = \frac{1}{100} \times \frac{3}{100} \times 2 \times 2 \times 4 \times 10^{-3} \times 4 \times 10^{-3} \times 10^{-12}$$

$$= \frac{2 \times (100) \times 10^{-6}}{2 \times (100) \times 10^{-6}}$$

$$= 144 \times 10^{-18} \text{ kg}$$

22. In an experiment to find emf of a cell using potentiometer, the length of null point for a cell of emf  $1.5 \text{ V}$  is found to be  $60 \text{ cm}$ . If this cell is replaced by another cell of emf  $E$ , the length-of null point increases by  $40 \text{ cm}$ . The value of  $E$  is  $\frac{x}{10} \text{ V}$ . The value of  $x$  is  $\_\_\_\_\_\_$ .

Official Ans. by NTA (25)

Ans. (25)

Sol.  $\frac{E_1}{E_2} = \frac{l_1}{l_2}$

$$\frac{1.5}{E_2} = \frac{60}{60 + 40} = \frac{6}{10} = \frac{3}{5}$$

$$E_2 = \frac{5}{2} = \frac{x}{10}$$

$$x = 25$$

23. A small particle moves to position  $5\hat{i} - 2\hat{j} + \hat{k}$  from its initial position  $2\hat{i} + 3\hat{j} - 4\hat{k}$  under the action of force  $5\hat{i} + 2\hat{j} + 7\hat{k} \text{ N}$ . The value of work done will be  $\_\_\_\_\_\_ \text{ J}$ .

Official Ans. by NTA (40)

Ans. (40)

Sol.  $W = \vec{F} \cdot (\vec{r}_f - \vec{r}_i)$

$$= (5\hat{i} + 2\hat{j} + 7\hat{k}) \cdot ((5\hat{i} - 2\hat{j} + \hat{k}) - (2\hat{i} + 3\hat{j} - 4\hat{k}))$$

$$W = 40 \text{ J}$$

24. A light of energy  $12.75 \text{ eV}$  is incident on a hydrogen atom in its ground state. The atom absorbs the radiation and reaches to one of its excited states. The angular momentum of the atom in the excited state is  $\frac{x}{\pi} \times 10^{-17} \text{ eVs}$ . The value of  $x$  is  $\_\_\_\_\_\_$  (use  $h = 4.14 \times 10^{-15} \text{ eVs}$ ,  $c = 3 \times 10^8 \text{ ms}^{-1}$ ).

Official Ans. by NTA (828)

Ans. (828)

Sol. In the ground state energy  $= -13.6 \text{ eV}$

So energy

$$\frac{-13.6 \text{ eV}}{n^2} = -13.6 + 12.75$$

$$\frac{-13.6 \text{ eV}}{n^2} = -0.85$$

$$n = \sqrt{16}$$

$$n = 4$$

$$\text{Angular momentum} = \frac{nh}{2\pi} = \frac{4h}{2\pi} = \frac{2h}{\pi}$$

$$\text{Angular momentum} = \frac{2}{\pi} \times 4.14 \times 10^{-15}$$

$$= \frac{828 \times 10^{-17}}{\pi} \text{ eVs}$$



25. A certain pressure 'P' is applied to 1 litre of water and 2 litre of a liquid separately. Water gets compressed to 0.01% whereas the liquid gets compressed to 0.03%. The ratio of Bulk modulus of water to that of the liquid is  $\frac{3}{x}$ . The value of x is \_\_\_\_\_.

Official Ans. by NTA (1)

Ans. (1)

Sol.  $B_{water} = \frac{-\Delta P}{\left(\frac{\Delta V}{V}\right)} = \frac{-\Delta P}{\frac{0.01}{100}}$

$$B_{liquid} = \frac{-\Delta P}{\frac{0.03}{100}}$$

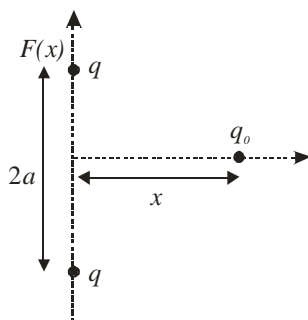
$$\frac{B_{water}}{B_{liquid}} = 3$$

$$x = 1$$

26. Two equal positive point charges are separated by a distance 2a. The distance of a point from the centre of the line joining two charges on the equatorial line (perpendicular bisector) at which force experienced by a test charge  $q_0$  becomes maximum is  $\frac{a}{\sqrt{x}}$ . The value of x is \_\_\_\_\_.

Official Ans. by NTA (2)

Ans. (2)



Sol.

$$F = \frac{2Kqq_0x}{(x^2 + a^2)^{3/2}}$$

For F to be maximum

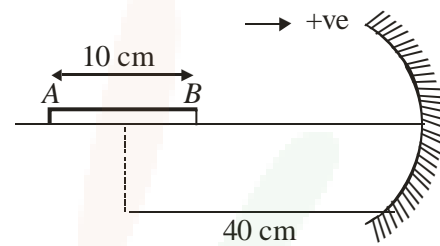
$$\frac{dF}{dx} = 0$$

$$x = \frac{a}{\sqrt{2}}$$

27. A thin cylindrical rod of length 10 cm is placed horizontally on the principle axis of a concave mirror of focal length 20 cm. The rod is placed in a such a way that mid point of the rod is at 40 cm from the pole of mirror. The length of the image formed by the mirror will be  $\frac{x}{3}$  cm. The value of x is \_\_\_\_\_.

Official Ans. by NTA (32)

Ans. (32)



Sol.

$$U_A = -45 \text{ cm}, f = -20 \text{ cm}$$

$$V_A = \frac{-45 \times (-20)}{-45 - (-20)} = \frac{-900}{25} = -36 \text{ cm}$$

$$\text{And } U_B = -35 \text{ cm}$$

$$\therefore V_B = \frac{-35 \times (-20)}{-35 - (-20)} = \frac{700}{-15}$$

$$\therefore V_A - V_B = \text{length of image}$$

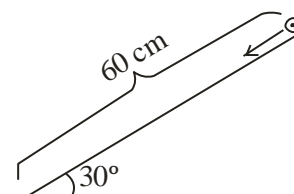
$$= \left(-36 + \frac{140}{3}\right) \text{ cm}$$

$$= \frac{-108 + 140}{3} \text{ cm}$$

$$= \frac{32}{3} \text{ cm}$$

$$\therefore x = 32$$

28. A solid cylinder is released from rest from the top of an inclined plane of inclination  $30^\circ$  and length 60 cm. If the cylinder rolls without slipping, its speed upon reaching the bottom of the inclined plane is \_\_\_\_\_  $\text{ms}^{-1}$ . (Given  $g = 10 \text{ ms}^{-2}$ )



Official Ans. by NTA (2)

Ans. (2)



**Sol.**  $v = \sqrt{\frac{2gh}{1 + \frac{k^2}{R^2}}}$

Where  $h = 60 \sin 30^\circ = 30 \text{ cm}$

$$k^2 = \frac{R^2}{2}$$

$$v = 2 \text{ ms}^{-1}$$

**29.** The amplitude of a particle executing SHM is 3 cm. The displacement at which its kinetic energy will be 25% more than the potential energy is: \_\_\_\_\_ cm.

**Official Ans. by NTA (2)**

**Ans. (2)**

**Sol.**  $KE = PE + \frac{PE}{4}$

$$KE = \frac{5}{4} PE$$

$$\frac{1}{2} m\omega^2 (A^2 - x^2) = \frac{5}{4} \times \frac{1}{2} m\omega^2 x^2$$

$$[v = \omega\sqrt{A^2 - x^2}]$$

$$A^2 - x^2 = \frac{5}{4} x^2$$

$$\frac{9x^2}{4} = A^2$$

$$\boxed{x = \frac{2}{3} A}$$

$$\therefore x = \frac{2}{3} \times 3 \text{ cm}$$

$$x = 2 \text{ cm}$$

**30.** A series LCR circuit is connected to an ac source of 220V, 50Hz. The circuit contain a resistance  $R = 100\Omega$  and an inductor of inductive reactance  $X_L = 79.6 \Omega$ . The capacitance of the capacitor needed to maximize the average rate at which energy is supplied will be \_\_\_\_\_  $\mu\text{F}$ .

**Official Ans. by NTA (40)**

**Ans. (40)**

**Sol.** To maximize the average rate at which energy supplied i.e. power will be maximum.

So in LCR circuit power will be maximum at the condition of resonance and in resonance condition

$$X_L = X_C$$

$$79.6 = \frac{1}{\omega C}$$

$$\therefore C = \frac{1}{2\pi \times 50 \times 79.6}$$

$$\therefore \boxed{C = 40\mu\text{F}}$$