TEST PAPER OF JEE(MAIN) EXAMINATION – 2019

(Held On Saturday 12th JANUARY, 2019) TIME : 02 : 30 PM To 05 : 30 PM

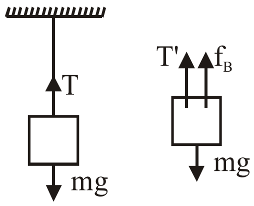
PHYSICS

1. A load of mass M kg is suspended from a steel wire of length 2 m and radius 1.0 mm in Searle's apparatus experiment. The increase in length produced in the wire is 4.0 mm. Now the load is fully immersed in a liquid of relative density 2. The relative density of the material of load is 8. The new value of increase in length of the steel wire is :

(1) 4.0mm (2) 3.0mm (3) 5.0mm (4) zero

Ans (2)

Sol.



$$\frac{F}{A} = y.\frac{\Delta\ell}{\ell}$$

$\Delta\ell \propto F$ .....(i)

$T = mg$

$$T = mg - f_B = mg - \frac{m}{\rho_b}.\rho_\ell.g$$

$$= \left(1 - \frac{\rho_\ell}{\rho_b}\right)mg$$

$$= \left(1 - \frac{2}{8}\right) mg$$

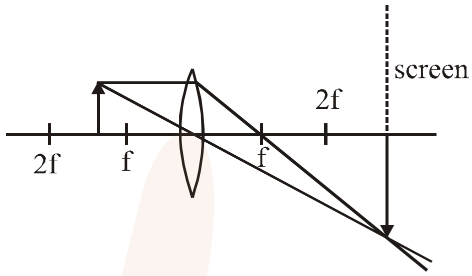
$$T' = \frac{3}{4}mg$$

From (i)

$$\frac{\Delta\ell'}{\Delta\ell} = \frac{T'}{T} = \frac{3}{4}$$

$$\Delta\ell' = \frac{3}{4} \cdot \Delta\ell = 3 \text{ mm}$$

2. Formation of real image using a biconvex lens is shown below :



If the whole set up is immersed in water without disturbing the object and the screen position, what will one observe on the screen ?

(1) Image disappears

(2) No change

(3) Erect real image

(4) Magnified image

Ans (1)

Sol. From $\frac{1}{f} = (\mu_{rel} - 1)\left(\frac{1}{R_1} - \frac{1}{R_2}\right)$

Focal length of lens will change hence image disappears from the screen.

3. A vertical closed cylinder is separated into two parts by a frictionless piston of mass m and of negligible thickness. The piston is free to move along the length of the cylinder. The length of the cylinder above the piston is ℓ_1, and that below the piston is ℓ_2, such that $\ell_1 > \ell_2$. Each part of the cylinder contains n moles of an ideal gas at equal temperature T. If the piston is stationary, its mass, m, will be given by :

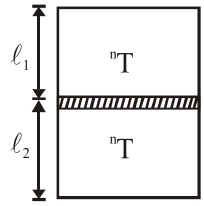
(R is universal gas constant and g is the acceleration due to gravity)

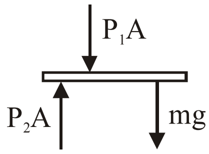
(1) $\frac{nRT}{g}\left[\frac{1}{\ell_2} + \frac{1}{\ell_1}\right]$ (2) $\frac{nRT}{g}\left[\frac{\ell_1 - \ell_2}{\ell_1\ell_2}\right]$

(3) $\frac{RT}{g}\left[\frac{2\ell_1 + \ell_2}{\ell_1\ell_2}\right]$ (4) $\frac{RT}{ng}\left[\frac{\ell_1 - 3\ell_2}{\ell_1\ell_2}\right]$

Ans (2)

Sol.





$P_2A = P_1A + mg$

$$\frac{nRT.A}{A\ell_2} = \frac{nRT.A}{A\ell_1} + mg$$

$$nRT\left(\frac{1}{\ell_2} - \frac{1}{\ell_1}\right) = mg$$

$$m = \frac{nRT}{g}\left(\frac{\ell_1 - \ell_2}{\ell_1.\ell_2}\right)$$

4. A simple harmonic motion is represented by:

$y = 5(\sin 3\pi t + \sqrt{3}\cos 3\pi t)$ cm

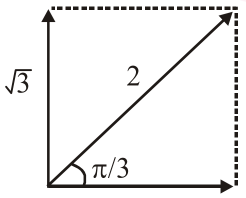
The amplitude and time period of the motion are:

(1) 5cm, $\frac{3}{2}$s (2) 5cm, $\frac{2}{3}$s

(3) 10cm, $\frac{3}{2}$s (4) 10cm, $\frac{2}{3}$s

Ans. (4)

Sol.



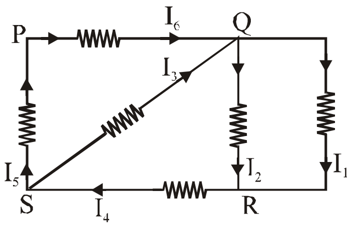
$$y = 5\left[\sin(3\pi t) + \sqrt{3}\cos(3\pi t)\right]$$

$$= 10\sin\left(3\pi t + \frac{\pi}{3}\right)$$

Amplitude = 10 cm

$$T = \frac{2\pi}{w} = \frac{2\pi}{3\pi} = \frac{2}{3}\text{sec}$$

5. In the given circuit diagram, the currents, $I_1 = -0.3A$, $I_4 = 0.8$ A and $I_5 = 0.4$ A, are flowing as shown. The currents I_2, I_3 and I_6, respectively, are :



(1) 1.1 A, 0.4 A, 0.4 A

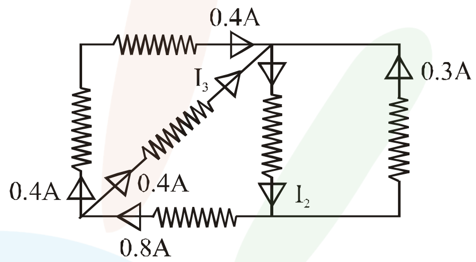
(2) –0.4 A, 0.4 A, 1.1 A

(3) 0.4 A, 1.1 A, 0.4 A

(4) 1.1 A, –0.4 A, 0.4 A

Ans. (1)

Sol.



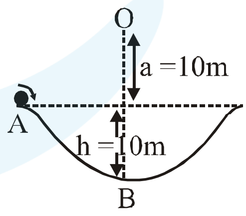
From KCL, $I_3 = 0.8 - 0.4 = 0.4A$

$I_2 = 0.4 + 0.4 + 0.3$

$= 1.1$ A

$I_6 = 0.4A$

6. A particle of mass 20 g is released with an initial velocity 5 m/s along the curve from the point A, as shown in the figure. The point A is at height h from point B. The particle slides along the frictionless surface. When the particle reaches point B, its angular momentum about O will be : (Take g= 10 m/s²)



(1) 8kg-m²/s (2) 6kg-m²/s

(3) 3kg-m²/s (4) 2kg-m²/s

Ans. (2)

Sol. Work Energy Theorem from A to B

$$mgh = \frac{1}{g}mv_B^2 - \frac{1}{g}mv_A^2$$

$$2gh = v_B^2 - v_A^2$$

$$2\times10\times10 = v_B^2 - 5^2$$

$$v_B = 15\,m/s$$

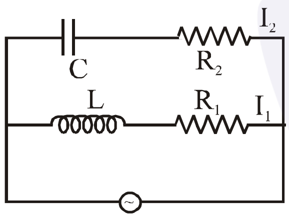
Angular momentum about 0

L_0 = mvr

$= 20\times10^{-3}\times20$

L_0 = 6 kg.m^2/s

7.

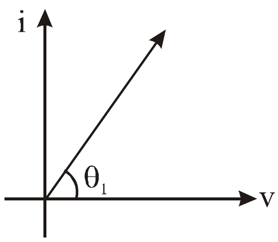


In the above circuit, $C = \frac{\sqrt{3}}{2}\mu F$, R_2 = 20Ω, $L = \frac{\sqrt{3}}{10}$ H and R_1 = 10Ω. Current in L-R_1 path is I_1 and in C-R_2 path it is I_2. The voltage of A.C source is given by $V = 200\sqrt{2}\sin(100t)$ volts. The phase difference between I_1 and I_2 is :

(1) 30° (2) 0° (3) 90° (4) 60°

Ans. **(Bonus)**

Sol.



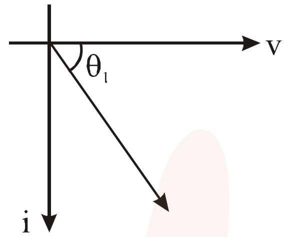
$$x_e = \frac{1}{\omega_c} = \frac{4}{10^{-6}\times\sqrt{3}\times100} = \frac{2\times10^4}{\sqrt{3}}$$

$$\tan\theta/2\ \frac{x_e}{R_e} = \frac{10^3}{\sqrt{3}}$$

θ_1 is close to 90

For L–R circuit

$$x_L = w_L = 100\times\frac{\sqrt{3}}{10} = \sqrt{3}$$



R_1 = 10

$$\tan\theta_2 = \frac{x_e}{R}$$

$$\tan\theta_2 = \sqrt{3}$$

θ_2 = 60

So phase difference comes out 90 + 60 = 150.

Therefore Ans. is Bonus

If R_2 is 20 KΩ

then phase difference comes out to be 60+30 = 90°

8. A paramagnetic material has 10^{28}atoms/m^3. Its magnetic susceptibility at temperature 350 K is 2.8 $\times10^{-4}$. Its susceptibility at 300 K is :

(1) 3.672×10^{-4} (2) 3.726×10^{-4}

(3) 3.267×10^{-4} (4) 2.672×10^{-4}

Ans (3)

Sol. $x \propto \frac{1}{T_C}$

curie law for paramagnetic substane

$$\frac{x_1}{x_2} = \frac{T_{C_2}}{T_{C_1}}$$

$$\frac{2.8\times10^{-4}}{x_2} = \frac{300}{350}$$

$$x_2 = \frac{2.8\times350\times10^{-4}}{300}$$

$= 3.266 \times 10^{-4}$

9. A 10 m long horizontal wire extends from North East to South West. It is falling with a speed of $5.0 ms^{-1}$, at right angles to the horizontal component of the earth's magnetic field, of $0.3 \times 10^{-4} Wb/m^2$. The value of the induced emf in wire is :

(1) $2.5 \times 10^{-3}V$ (2) $1.1 \times 10^{-3}V$

(3) $0.3 \times 10^{-3}V$ (4) $1.5 \times 10^{-3}V$

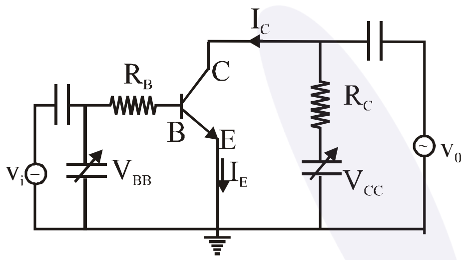
Ans (4)

Sol. Induied emf = $Bv\ell$

$= 0.3 \times 10^{-4} \times 5 \times 10$

$= 1.5 \times 10^{-3}$ V

10.



In the figure, given that V_{BB} supply can vary from 0 to 5.0 V, $V_{CC} = 5V$, $\beta_{dc} = 200$, $R_B = 100 k\Omega$, R_C=l kΩ and V_{BE}=1.0 V, The minimum base current and the input voltage at which the transistor will go to saturation, will be, respectively :

(1) 20μA and 3.5V (2) 25μA and 3.5V

(3) 25μA and 2.5V (4) 20μA and 2.8V

Ans (2)

Sol. At saturation, $V_{CE} = 0$

$V_{CE} = V_{CC} - I_C R_C$

$\Rightarrow I_C = \frac{V_{CC}}{R_C} = 5 \times 10^{-3}$ A

Given

$$\beta_{dc} = \frac{I_C}{I_B}$$

$$I_B = \frac{5\times10^{-3}}{200}$$

$I_B = 25$ μA

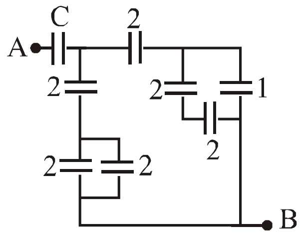
At input side

$V_{BB} = I_B R_B + V_{BE}$

$= (25mA)(100k\Omega) + 1V$

$V_{BB} = 3.5$ V

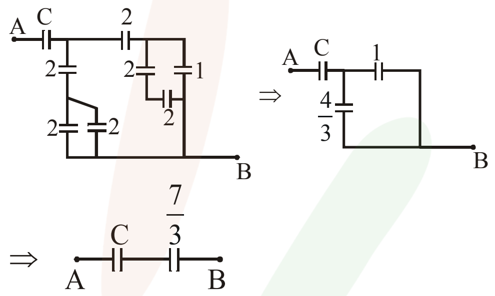
11. In the circuit shown, find C if the effective capacitance of the whole circuit is to be 0.5 μF. All values in the circuit are in μF.



(1) $\frac{7}{10}$μF (2) $\frac{7}{11}$μF (3) $\frac{6}{5}$μF (4) 4μF

Ans (2)

Sol.



From equs.

$$\frac{\frac{7C}{3}}{\frac{7}{3}+C} = \frac{1}{2}$$

$\Rightarrow$ 14 C = 7 + 3 C

$\Rightarrow C = \frac{7}{11}$

12. Two satellites, A and B, have masses m and 2m respectively. A is in a circular orbit of radius R, and B is in a circular orbit of radius 2R around the earth. The ratio of their kinetic energies, T_A/T_B, is:

(1) 2 (2) $\sqrt{\frac{1}{2}}$ (3) 1 (4) $\frac{1}{2}$

Ans (3)

Sol. Orbital velocity $V = \sqrt{\frac{GMe}{r}}$

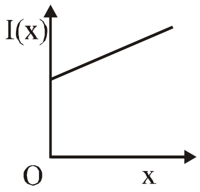
$$T_A = \frac{1}{2} m_A V_A^2$$

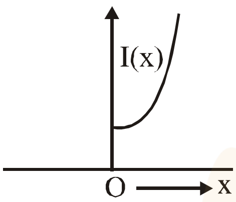
$$T_B = \frac{1}{2} m_B V_B^2$$

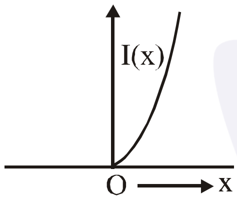
$$\Rightarrow \frac{T_A}{T_B} = \frac{m \times \frac{Gm}{R}}{2m \times \frac{Gm}{2R}}$$

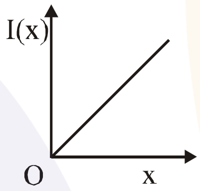
$$\Rightarrow \frac{T_A}{T_B} = 1$$

13. The moment of inertia of a solid sphere, about an axis parallel to its diameter and at a distance of x from it, is I(x)'. Which one of the graphs represents the variation of I(x) with x correctlv?

(1) 

(2) 

(3) 

(4) 

Ans. **(2)**

Sol. $I = \frac{2}{5}mR^2 + mx^2$

14. When a certain photosensistive surface is illuminated with monochromatic light of frequency ν, the stopping potential for the photo current is $-V_0/2$. When the surface is illuminated by monochromatic light of frequency ν/2, the stopping potential is $-V_0$. The threshold frequency for photoelectric emission is:

(1) $\frac{3\nu}{2}$ (2) 2ν (3) $\frac{4}{3}\nu$ (4) $\frac{5\nu}{3}$

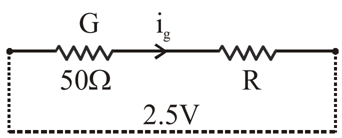
Ans. **(BONUS)**

15. A galvanometer, whose resistance is 50 ohm, has 25 divisions in it. When a current of 4×10^{-4} A passes through it, its needle (pointer) deflects by one division. To use this galvanometer as a voltmeter of range 2.5 V, it should be connected to a resistance of:

(1) 6250 ohm (2) 250 ohm
(3) 200 ohm (4) 6200 ohm

Ans. **(3)**

Sol. $I_g = 4 \times 10^{-4} \times 25 = 10^{-2}$ A



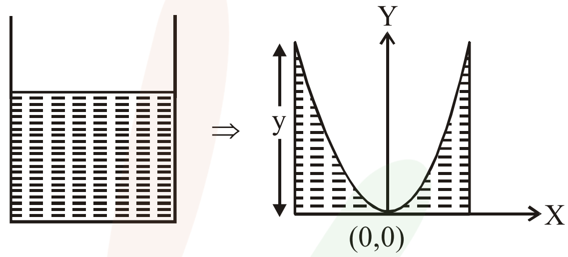
$2.5 = (50 + R)\ 10^{-2}\ \therefore\ R = 200\ \Omega$

16. A long cylindrical vessel is half filled with a liquid. When the vessel is rotated about its own vertical axis, the liquid rises up near the wall. If the radius of vessel is 5 cm and its rotational speed is 2 rotations per second, then the difference in the heights between the centre and the sides, in cm, will be:

(1) 1.2 (2) 0.1 (3) 2.0 (4) 0.4

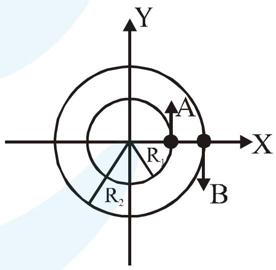
Ans. **(3)**

Sol.



$$y = \frac{\omega^2 x^2}{2g} = \frac{(2\times 2\pi)^2 \times (0.05)^2}{20} \simeq 2 \text{ cm}$$

17. Two particles A, B are moving on two concentric circles of radii R_1 and R_2 with equal angular speed ω. At t = 0, their positions and direction of motion are shown in the figure :

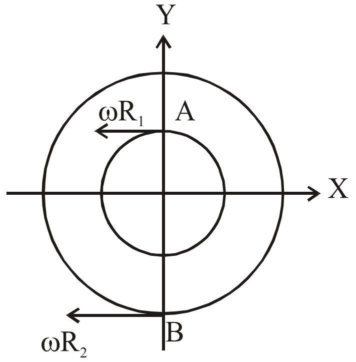


The relative velocity $\vec{\upsilon}_A - \vec{\upsilon}_B$ at $t = \frac{\pi}{2\omega}$ is given by :

(1) $-\omega(R_1 + R_2)\hat{i}$ (2) $\omega(R_1 + R_2)\hat{i}$
(3) $\omega(R_1 - R_2)\hat{i}$ (4) $\omega(R_2 - R_1)\hat{i}$

Ans. **(4)**

Sol. $\theta = \omega t = \omega\frac{\pi}{2\omega} = \frac{\pi}{2}$



$$\vec{V}_A - \vec{V}_S = \omega R_1(-\hat{i}) - \omega R_2(-i)$$

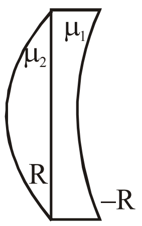
18. A plano-convex lens (focal length f_2, refractive index μ_2, radius of curvature R) fits exactly into a plano-concave lens (focal length f_1, refractive index μ_1, radius of curvature R). Their plane surfaces are parallel to each other. Then, the focal length of the combination will be :

(1) $f_1 - f_2$ (2) $f_1 + f_2$

(3) $\frac{R}{\mu_2 - \mu_1}$ (4) $\frac{2f_1f_2}{f_1 + f_2}$

Ans. (3)

Sol.



$$\frac{1}{F} = \frac{1}{f_1} + \frac{1}{f_2} = \frac{1-\mu_1}{R} + \frac{\mu_2 - 1}{R}$$

19. Let ℓ, r, c and v represent inductance, resistance, capacitance and voltage, respectively. The dimension of $\frac{\ell}{rcv}$ in SI units will be:

(1) [LTA] (2) [LA^{-2}] (3) [A^{-1}] (4) [LT^2]

Ans. (3)

Sol. $\left[\frac{\ell}{r}\right] = T$

$[CV] = AT$

So, $\left[\frac{\ell}{rCV}\right] = \frac{T}{AT} = A^{-1}$

20. In a radioactive decay chain, the initial nucleus is $^{232}_{90}Th$. At the end there are 6 α-particles and 4 β-particles which are emitted. If the end nucleus, If $^{A}_{Z}X$, A and Z are given by :

(1) A = 208; Z = 80

(2) A = 202; Z = 80

(3) A = 200; Z = 81

(4) A = 208; Z = 82

Ans. (4)

Sol. $^{232}_{90}Th \longrightarrow {}^{208}_{78}Y + {}^{4}_{2}He$

$^{208}_{78}Y \longrightarrow {}^{208}_{82}X + 4\beta$ praticle

21. The mean intensity of radiation on the surface of the Sun is about 10^8 W/m². The rms value of the corresponding magnetic field is closest to :

(1) 10^2T (2) 10^{-4}T

(3) 1T (4) 10^{-2}T

Ans. (2)

Sol. $I = \varepsilon_0\ C\ E^2_{rms}$

$\&E_{rms} = cB_{rms}$

$I = \varepsilon_0\ C^3\ B^2_{rms}$

$B_{rms} = \sqrt{\frac{I}{\epsilon_0 C^3}}$

$B_{rms} \approx 10^{-4}$

22. A resonance tube is old and has jagged end. It is still used in the laboratory to determine velocity of sound in air. A tuning fork of frequency 512 Hz produces first resonance when the tube is filled with water to a mark 11 cm below a reference mark, near the open end of the tube. The experiment is repeated with another fork of frequency 256 Hz which produces first resonance when water reaches a mark 27 cm below the reference mark. The velocity of sound in air, obtained in the experiment, is close to:

(1) 328ms^{-1} (2) 322ms^{-1}

(3) 341ms^{-1} (4) 335ms^{-1}

Ans. (1)

23. An ideal gas is enclosed in a cylinder at pressure of 2 atm and temperature, 300 K. The mean time between two successive collisions is 6×10^{-8} s. If the pressure is doubled and temperature is increased to 500 K, the mean time between two successive collisions will be close to:

(1) 4×10^{-8}s (2) 3×10^{-6}s

(3) 2×10^{-7}s (4) 0.5×10^{-8}s

Ans. **(1)**

Sol. $t \propto \frac{\text{Volume}}{\text{velocity}}$

$\text{volume} \propto \frac{T}{P}$

$\therefore \; t \propto \frac{\sqrt{T}}{P}$

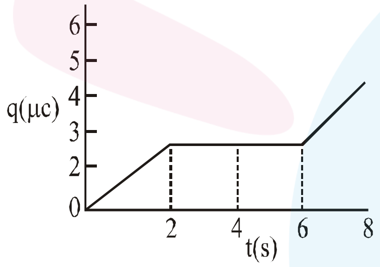
$\frac{t_1}{6\times10^{-8}} = \frac{\sqrt{500}}{2P} \times \frac{P}{\sqrt{300}}$

$t_1 = 3.8 \times 10^{-8}$

$\approx 4 \times 10^{-8}$

24. The charge on a capacitor plate in a circuit, as a function of time, is shown in the figure:

What is the value of current at t = 4 s ?

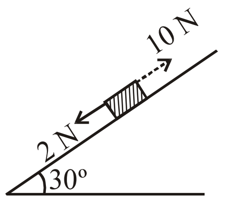


(1) 3μA (2) 2μA (3) zero (4) 1.5μA

Ans. **(3)**

25. A block kept on a rough inclined plane, as shown in the figure, remaias at rest upto a maximum force 2 N down the inclined plane. The maximum external force up the inclined plane that does not move the block is 10 N. The coefficient of static friction between the block and the plane is :

[Take g = 10 m/s²]



(1) $\frac{2}{3}$ (2) $\frac{\sqrt{3}}{2}$ (3) $\frac{\sqrt{3}}{4}$ (4) $\frac{1}{2}$

Ans. **(2)**

Sol. $2 + mg \sin 30 = \mu mg \cos 30°$

$10 = mg\sin 30 + \mu\, mg \cos 30°$

$= 2\mu mg \cos 30 - 2$

$6 = \mu mg \cos 30$

$4 = mg \sin 30$

$\frac{3}{2} = \mu \times \sqrt{3}$

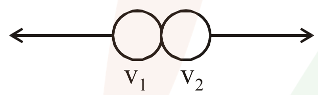
$\mu = \frac{\sqrt{3}}{2}$

26. An alpha-particle of mass m suffers 1-dimensional elastic coolision with a nucleus at rest of unknown mass. It is scattered directly backwards losing, 64% of its initial kinetic energy. The mass of the nucleus is :-

(1) 4 m (2) 3.5 m (3) 2 m (4) 1.5 m

Ans. **(1)**

Sol.



$mv_0 = mv_2 - mv_1$

$\frac{1}{2}mV_1^2 = 0.36 \times \frac{1}{2}mV_0^2$

$v_1 = 0.6v_0$

$\frac{1}{2}MV_2^2 = 0.64 \times \frac{1}{2}mV_0^2$

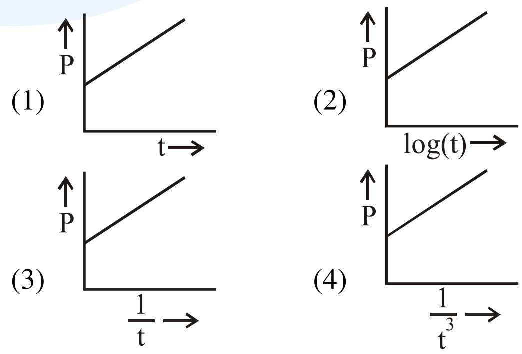
$V_2 = \sqrt{\frac{m}{M}} \times 0.8V_0$

$mV_0 = \sqrt{mM} \times 0.8V_0 - m \times 0.6V_0$

$\Rightarrow 1.6m = 0.8\sqrt{mM}$

$4m^2 = mM$

27. A soap bubble, blown by a mechanical pump at the mough of a tube, increases in volume, with time, at a constant rate. The graph that correctly depicts the time dependence of pressure inside the bubble is given by :-



Ans. **(4)**

28. To double the coverging range of a TV transmittion tower, its height should be multiplied by :-

(1) $\frac{1}{\sqrt{2}}$ (2) 4 (3) $\sqrt{2}$ (4) 2

Ans. (2)

29. A parallel plate capacitor with plates of area 1m^2 each, area t a separation of 0.1 m. If the electric field between the plates is 100 N/C, the magnitude of charge each plate is :-

(Take $\varepsilon_0 = 8.85\times10^{-12}\frac{C^2}{N-m^2}$)

(1) 7.85×10^{-10} C (2) 6.85×10^{-10} C
(3) 9.85×10^{-10} C (4) 8.85×10^{-10} C

Ans. (4)

Sol. $E = \frac{\sigma}{\epsilon_0} = \frac{Q}{A\epsilon_0}$

$Q = AE\epsilon_0$

$Q = (1)(100)(8.85\times10^{-12})$

$Q = 8.85 \times 10^{-10}C$

30. In a Frank-Hertz experiment, an electron of energy 5.6 eV passes through mercury vapour and emerges with an energy 0.7 eV. The minimum wavelength of photons emitted by mercury atoms is close to :-

(1) 2020 nm Y:\node05\JEE-Main 2019-(On line)\12-01-2019\Evening\PDF (2) 220 nm

(3) 250 nm (4) 1700 nm

Ans. (3)

Sol. $\lambda = \frac{1240}{5.6-0.7}$ nm