

20. A diatomic molecule  $X_2$  has a body-centred cubic (bcc) structure with a cell edge of 300 pm. The density of the molecule is  $6.17 \text{ g cm}^{-3}$ . The number of molecules present in 200 g of  $X_2$  is

(Avogadro constant ( $N_A$ ) =  $6 \times 10^{23} \text{ mol}^{-1}$ )

- (1)  $8 N_A$   
 (2)  $40 N_A$   
 (3)  $4 N_A$   
 (4)  $2 N_A$

**Official Ans. by NTA (3)**

**Sol.** 
$$p = \frac{2 \times \frac{M}{N_A}}{a^3} \Rightarrow 6.17 = \frac{2 \times \frac{M}{N_A}}{(3 \times 10^{-8} \text{ cm})^3}$$

$$\Rightarrow M \approx 50 \text{ gm / mol}$$

$$N_o = \frac{w}{M} \times N_A = \frac{200}{50} \times N_A = 4N_A$$

21. an oxidation-reduction reaction in which 3 electrons are transferred has a  $\Delta G^\circ$  of  $17.37 \text{ kJ mol}^{-1}$  at  $25^\circ\text{C}$ . The value of  $E^\circ_{\text{cell}}$  (in V) is \_\_\_\_\_  $\times 10^{-2}$

(1 F =  $96,500 \text{ C mol}^{-1}$ )

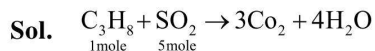
**Official Ans. by NTA (6)**

**Sol.** 
$$\Delta G^\circ = -nFE^\circ = -3 \times 96500 \times E^\circ$$

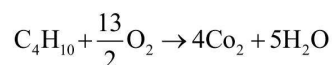
$$\Rightarrow E^\circ = -6 \times 10^{-2} \text{ V}$$

22. The minimum number of moles of  $O_2$  required for complete combustion of 1 mole of propane and 2 moles of butane is \_\_\_\_\_.

**Official Ans. by NTA (18)**



For 1 mole propane combustion 5 mole  $O_2$  required



1 mole            6.5 mole

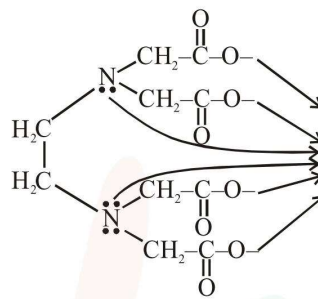
2 mole            13 mole

For 2 moles of butane 13 mole of  $O_2$  is required  
 total moles =  $13 + 5 = 18$

23. The total number of coordination sites in ethylenediaminetetraacetate ( $EDTA^{4-}$ ) is \_\_\_\_\_.

**Official Ans. by NTA (6)**

- Sol.**  $EDTA^{4-}$  is hexadentate ligand, so its donation sites are six.



24. The number of chiral carbon(s) present in peptide, Ile-Arg-Pro, is \_\_\_\_\_.

**Official Ans. by NTA (4)**

25. A soft drink was bottled with a partial pressure of  $CO_2$  of 3 bar over the liquid at room temperature. The partial pressure of  $CO_2$  over the solution approaches a value of 30 bar when 44 g of  $CO_2$  is dissolved in 1 kg of water at room temperature. The approximate pH of the soft drink is \_\_\_\_\_  $\times 10^{-1}$ .

(First dissociation constant of  $H_2CO_3 = 4.0 \times 10^{-7}$ ;  $\log 2 = 0.3$ ; density of the soft drink =  $1 \text{ g mL}^{-1}$ )

**Official Ans. by NTA (37)**

**Sol.** 
$$P_{CO_2} = K_H \times CO_2$$

$$\frac{3}{30} = \frac{K_H \cdot n_{CO_2}}{K_H \cdot 1} \Rightarrow n_{CO_2} = 0.1 \text{ mol}$$

$$pH = \frac{1}{2}(pka_1 - \log c) = \frac{1}{2}(6.4 \times 1) = 3.7$$

$$pH = 37 \times 10^{-1}$$

**FINAL JEE-MAIN EXAMINATION – SEPTEMBER, 2020**

(Held On Saturday 05<sup>th</sup> SEPTEMBER, 2020) TIME : 9 AM to 12 PM

**MATHEMATICS**

**TEST PAPER WITH SOLUTION**

1. If  $3^{2 \sin 2\alpha - 1}$ , 14 and  $3^{4 - 2 \sin 2\alpha}$  are the first three terms of an A.P. for some  $\alpha$ , then the sixth term of this A.P. is :

- (1) 66 (2) 65  
(3) 81 (4) 78

**Official Ans. by NTA (1)**

**Sol.** Given that

$$3^{4 - \sin 2\alpha} + 3^{2 \sin 2\alpha - 1} = 28$$

$$\text{Let } 3^{2 \sin 2\alpha} = t$$

$$\frac{81}{t} + \frac{t}{3} = 28$$

$$t = 81, 3$$

$$3^{2 \sin 2\alpha} = 3^1, 3^4$$

$$2 \sin 2\alpha = 1, 4$$

$$\sin 2\alpha = \frac{1}{2}, 2 \text{ (rejected)}$$

$$\text{First term } a = 3^{2 \sin 2\alpha - 1}$$

$$a = 1$$

$$\text{Second term} = 14$$

$$\therefore \text{common difference } d = 13$$

$$T_6 = a + 5d$$

$$T_6 = 1 + 5 \times 13$$

$$T_6 = 66$$

2. If the function  $f(x) = \begin{cases} k_1(x - \pi)^2 - 1, & x \leq \pi \\ k_2 \cos x, & x > \pi \end{cases}$

is twice differentiable, then the ordered pair  $(k_1, k_2)$  is equal to :

(1)  $(\frac{1}{2}, 1)$  (2) (1, 1)

(3)  $(\frac{1}{2}, -1)$  (4) (1, 0)

**Official Ans. by NTA (1)**

**Sol.**  $f(x)$  is continuous and differentiable

$$f(\pi^-) = f(\pi) = f(\pi^+)$$

$$-1 = -k_2$$

$$\boxed{k_2 = 1}$$

$$f'(x) = \begin{cases} 2k_1(x - \pi); & x \leq \pi \\ -k_2 \sin x; & x > \pi \end{cases}$$

$$f'(\pi^-) = f'(\pi^+)$$

$$0 = 0$$

so, differentiable at  $x = \pi$

$$f''(x) = \begin{cases} 2k_1; & x \leq \pi \\ -k_2 \cos x; & x > \pi \end{cases}$$

$$f''(\pi^-) = f''(\pi^+)$$

$$2k_1 = k_2$$

$$\boxed{k_1 = \frac{1}{2}}$$

$$(k_1, k_2) = \left(\frac{1}{2}, 1\right)$$

3. If the common tangent to the parabolas,  $y^2 = 4x$  and  $x^2 = 4y$  also touches the circle,  $x^2 + y^2 = c^2$ , then  $c$  is equal to :

(1)  $\frac{1}{2}$  (2)  $\frac{1}{2\sqrt{2}}$

(3)  $\frac{1}{\sqrt{2}}$  (4)  $\frac{1}{4}$

**Official Ans. by NTA (3)**

**Sol.**  $y = mx + \frac{1}{m}$  (tangent at  $y^2 = 4x$ )

$$y = mx - m^2 \text{ (tangent at } x^2 = 4y)$$

$$\frac{1}{m} = -m^2 \text{ (for common tangent)}$$

$$m^3 = -1$$

$$\boxed{m = -1}$$

$y = -x - 1$   
 $x + y + 1 = 0$   
 This line touches circle  
 $\therefore$  apply  $p = r$

$$c = \frac{|0+0+1|}{\sqrt{2}} = \frac{1}{\sqrt{2}}$$

4. The negation of the Boolean expression  $x \leftrightarrow \sim y$  is equivalent to :

- (1)  $(\sim x \wedge y) \vee (\sim x \wedge \sim y)$   
 (2)  $(x \wedge \sim y) \vee (\sim x \wedge y)$   
 (3)  $(x \wedge y) \vee (\sim x \wedge \sim y)$   
 (4)  $(x \wedge y) \wedge (\sim x \vee \sim y)$

**Official Ans. by NTA (3)**

**Sol.**  $p \leftrightarrow q \equiv (p \rightarrow q) \wedge (q \rightarrow p)$   
 $x \leftrightarrow \sim y \equiv (x \rightarrow \sim y) \wedge (\sim y \rightarrow x)$   
 $\therefore (p \rightarrow q) \equiv \sim p \vee q$   
 $x \leftrightarrow \sim y \equiv (\sim x \vee \sim y) \wedge (y \vee x)$   
 $\sim(x \leftrightarrow \sim y) \equiv (x \wedge y) \vee (\sim x \wedge \sim y)$

5. If the volume of a parallelepiped, whose coterminal edges are given by the vectors

$\vec{a} = \hat{i} + \hat{j} + n\hat{k}$ ,  $\vec{b} = 2\hat{i} + 4\hat{j} - n\hat{k}$  and  
 $\vec{c} = \hat{i} + n\hat{j} + 3\hat{k}$  ( $n \geq 0$ ), is 158 cu. units, then :

- (1)  $\vec{a} \cdot \vec{c} = 17$                       (2)  $\vec{b} \cdot \vec{c} = 10$   
 (3)  $n = 7$                                 (4)  $n = 9$

**Official Ans. by NTA (2)**

**Sol.**  $v = [\vec{a} \vec{b} \vec{c}]$

$$158 = \begin{vmatrix} 1 & 1 & n \\ 2 & 4 & -n \\ 1 & n & 3 \end{vmatrix}, n \geq 0$$

$$158 = 1(12 + n^2) - (6 + n) + n(2n - 4)$$

$$158 = n^2 + 12 - 6 - n + 2n^2 - 4n$$

$$3n^2 - 5n - 152 = 0$$

$$n = 8, -\frac{38}{6} \text{ (rejected)}$$

$$\vec{a} \cdot \vec{c} = 1 + n + 3n = 1 + 4n = 33$$

$$\vec{b} \cdot \vec{c} = 2 + 4n - 3n = 2 + n = 10$$

6. If  $y = y(x)$  is the solution of the differential

equation  $\frac{5+e^x}{2+y} \cdot \frac{dy}{dx} + e^x = 0$  satisfying

- $y(0) = 1$ , then a value of  $y(\log_e 13)$  is :
- (1) 1                                              (2) -1  
 (3) 2                                              (4) 0

**Official Ans. by NTA (2)**

**Sol.**  $\frac{(5+e^x)}{2+y} \frac{dy}{dx} = -e^x$

$$\int \frac{dy}{2+y} = \int \frac{-e^x}{e^x+5} dx$$

$$\ln(y+2) = -\ln(e^x+5) + k$$

$$(y+2)(e^x+5) = C$$

$\therefore y(0) = 1$   
 $\Rightarrow C = 18$

$$y+2 = \frac{18}{e^x+5}$$

at  $x = \ln 13$

$$y+2 = \frac{18}{13+5} = 1$$

$y = -1$

7. A survey shows that 73% of the persons working in an office like coffee, whereas 65% like tea. If  $x$  denotes the percentage of them, who like both coffee and tea, then  $x$  cannot be:

- (1) 63                                              (2) 38  
 (3) 54                                              (4) 36

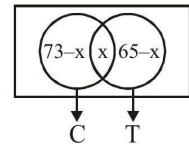
**Official Ans. by NTA (4)**

**Sol.** C  $\rightarrow$  person like coffee

T  $\rightarrow$  person like Tea

$n(C) = 73$   
 $n(T) = 65$

$n(C \cup T) \leq 100$   
 $n(C) + n(T) - n(C \cap T) \leq 100$



$$73 + 65 - x \leq 100$$

$$x \geq 38$$

$$73 - x \geq 0 \Rightarrow x \leq 73$$

$$65 - x \geq 0 \Rightarrow x \leq 65$$

$$\boxed{38 \leq x \leq 65}$$

8. The product of the roots of the equation  $9x^2 - 18|x| + 5 = 0$ , is

(1)  $\frac{25}{9}$

(2)  $\frac{25}{81}$

(3)  $\frac{5}{27}$

(4)  $\frac{5}{9}$

**Official Ans. by NTA (2)**

**Sol.**  $9x^2 - 18|x| + 5 = 0$

$$9|x|^2 - 15|x| - 3|x| + 5 = 0 \quad (\because x^2 = |x|^2)$$

$$3|x| (3|x| - 5) - (3|x| - 5) = 0$$

$$|x| = \frac{1}{3}, \frac{5}{3}$$

$$x = \pm \frac{1}{3}, \pm \frac{5}{3}$$

$$\text{Product of roots} = \frac{25}{81}$$

9. If  $\int (e^{2x} + 2e^x - e^{-x} - 1)e^{(e^x + e^{-x})} dx$

=  $g(x)e^{(e^x + e^{-x})} + c$ , where  $c$  is a constant of integration, then  $g(0)$  is equal to :

(1) 2

(2)  $e^2$

(3)  $e$

(4) 1

**Official Ans. by NTA (1)**

**Sol.**  $e^{2x} + 2e^x - e^{-x} - 1$

$$= e^x (e^x + 1) - e^{-x} (e^x + 1) + e^x$$

$$= [(e^x + 1) (e^x - e^{-x}) + e^x]$$

$$\text{so } I = \int (e^x + 1)(e^x - e^{-x})e^{e^x + e^{-x}} + \int e^x \cdot e^{e^x + e^{-x}} dx$$

$$= (e^x + 1)e^{e^x + e^{-x}} - \int e^x \cdot e^{e^x + e^{-x}} dx + \int e^x \cdot e^{e^x + e^{-x}} dx$$

$$= (e^x + 1)e^{e^x + e^{-x}} + C$$

$$\therefore g(x) = e^x + 1 \Rightarrow g(0) = 2$$

10. If the minimum and the maximum values of the

function  $f : \left[ \frac{\pi}{4}, \frac{\pi}{2} \right] \rightarrow \mathbb{R}$ , defined by :

$$f(\theta) = \begin{vmatrix} -\sin^2 \theta & -1 - \sin^2 \theta & 1 \\ -\cos^2 \theta & -1 - \cos^2 \theta & 1 \\ 12 & 10 & -2 \end{vmatrix}$$

are  $m$  and  $M$  respectively, then the ordered pair  $(m, M)$  is equal to :

(1)  $(0, 4)$

(2)  $(-4, 4)$

(3)  $(0, 2\sqrt{2})$

(4)  $(-4, 0)$

**Official Ans. by NTA (4)**

**Sol.**  $C_3 \rightarrow C_3 - (C_1 - C_2)$

$$f(\theta) = \begin{vmatrix} -\sin^2 \theta & -1 - \sin^2 \theta & 0 \\ -\cos^2 \theta & -1 - \cos^2 \theta & 0 \\ 12 & 10 & -4 \end{vmatrix}$$

$$= -4[(1 + \cos^2 \theta) \sin^2 \theta - \cos^2 \theta (1 + \sin^2 \theta)]$$

$$= -4[\sin^2 \theta + \sin^2 \theta \cos^2 \theta - \cos^2 \theta - \cos^2 \theta \sin^2 \theta]$$

$$f(\theta) = 4 \cos 2\theta$$

$$\theta \in \left[ \frac{\pi}{4}, \frac{\pi}{2} \right]$$

$$2\theta \in \left[ \frac{\pi}{2}, \pi \right]$$

$$f(\theta) \in [-4, 0]$$

$$(m, M) = (-4, 0)$$

**11.** Let  $\lambda \in \mathbb{R}$ . The system of linear equations

$$2x_1 - 4x_2 + \lambda x_3 = 1$$

$$x_1 - 6x_2 + x_3 = 2$$

$$\lambda x_1 - 10x_2 + 4x_3 = 3$$

is inconsistent for :

- (1) exactly one negative value of  $\lambda$ .
- (2) exactly one positive value of  $\lambda$ .
- (3) every value of  $\lambda$ .
- (4) exactly two values of  $\lambda$ .

**Official Ans. by NTA (1)**

**Sol.**  $D = \begin{vmatrix} 2 & -4 & \lambda \\ 1 & -6 & 1 \\ \lambda & -10 & 4 \end{vmatrix}$

$$= 2(3\lambda + 2)(\lambda - 3)$$

$$D_1 = -2(\lambda - 3)$$

$$D_2 = -2(\lambda + 1)(\lambda - 3)$$

$$D_3 = -2(\lambda - 3)$$

When  $\boxed{\lambda = 3}$ , then

$$D = D_1 = D_2 = D_3 = 0$$

$\Rightarrow$  Infinite many solution

when  $\boxed{\lambda = -\frac{2}{3}}$  then  $D_1, D_2, D_3$  none of them is zero so equations are inconsistent

$$\boxed{\therefore \lambda = -\frac{2}{3}}$$

**12.** If  $S$  is the sum of the first 10 terms of the series

$$\tan^{-1}\left(\frac{1}{3}\right) + \tan^{-1}\left(\frac{1}{7}\right) + \tan^{-1}\left(\frac{1}{13}\right) + \tan^{-1}\left(\frac{1}{21}\right) + \dots,$$

then  $\tan(S)$  is equal to :

(1)  $\frac{5}{11}$                       (2)  $-\frac{6}{5}$

(3)  $\frac{10}{11}$                       (4)  $\frac{5}{6}$

**Official Ans. by NTA (4)**

**Sol.**  $S = \tan^{-1}\left(\frac{1}{3}\right) + \tan^{-1}\left(\frac{1}{7}\right) + \tan^{-1}\left(\frac{1}{13}\right) + \dots$

$$S = \tan^{-1}\left(\frac{2-1}{1+1 \cdot 2}\right) + \tan^{-1}\left(\frac{3-2}{1+2 \cdot 3}\right) + \tan^{-1}$$

$$\left(\frac{4-3}{1+3 \cdot 4}\right) + \dots + \tan^{-1}\left(\frac{11-10}{1+10 \cdot 11}\right)$$

$$S = (\tan^{-1}2 - \tan^{-1}1) + (\tan^{-1}3 - \tan^{-1}2) + (\tan^{-1}4 - \tan^{-1}3) + \dots + (\tan^{-1}(11) - \tan^{-1}(10))$$

$$S = \tan^{-1}11 - \tan^{-1}1 = \tan^{-1}\left(\frac{11-1}{1+11}\right)$$

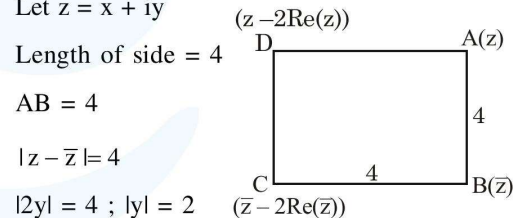
$$\tan(S) = \frac{11-1}{1+11 \cdot 1} = \frac{10}{12} = \frac{5}{6}$$

**13.** If the four complex numbers  $z, \bar{z}, \bar{z} - 2\text{Re}(\bar{z})$  and  $z - 2\text{Re}(z)$  represent the vertices of a square of side 4 units in the Argand plane, then  $|z|$  is equal to :

- (1) 4                              (2) 2
- (3)  $4\sqrt{2}$                       (4)  $2\sqrt{2}$

**Official Ans. by NTA (4)**

**Sol.** Let  $z = x + iy$



$$|z - \bar{z}| = 4$$

$$|2y| = 4 ; |y| = 2$$

$$|2x| = 4 ; |x| = 2$$

$$|z| = \sqrt{x^2 + y^2} = \sqrt{4+4} = 2\sqrt{2}$$





Add (1) & (2)

$$2I = \int_{-\pi/2}^{\pi/2} dx = \pi$$

$$I = \frac{\pi}{2}$$

18. If  $2^{10} + 2^9 \cdot 3^1 + 2^8 \cdot 3^2 + \dots + 2 \cdot 3^9 + 3^{10} = S - 2^{11}$ , then S is equal to :

(1)  $\frac{3^{11}}{2} + 2^{10}$                       (2)  $3^{11} - 2^{12}$

(3)  $3^{11}$                                 (4)  $2 \cdot 3^{11}$

**Official Ans. by NTA (3)**

**Sol.**  $a = 2^{10}$ ;  $r = \frac{3}{2}$ ;  $n = 11$  (G.P.)

$$S' = (2^{10}) \frac{\left(\left(\frac{3}{2}\right)^{11} - 1\right)}{\frac{3}{2} - 1} = 2^{11} \left(\frac{3^{11}}{2^{11}} - 1\right)$$

$$S' = 3^{11} - 2^{11} = S - 2^{11} \text{ (Given)}$$

$$\therefore S = 3^{11}$$

19. If the co-ordinates of two points A and B are  $(\sqrt{7}, 0)$  and  $(-\sqrt{7}, 0)$  respectively and P is any point on the conic,  $9x^2 + 16y^2 = 144$ , then PA + PB is equal to :

(1) 8                                      (2) 6

(3) 16                                    (4) 9

**Official Ans. by NTA (1)**

**Sol.**  $\frac{x^2}{16} + \frac{y^2}{9} = 1$

$$a = 4; b = 3; e = \sqrt{\frac{16-9}{16}} = \frac{\sqrt{7}}{4}$$

A and B are foci

$$\Rightarrow PA + PB = 2a = 2 \times 4 = 8$$

20. If  $\alpha$  is the positive root of the equation,

$$p(x) = x^2 - x - 2 = 0, \text{ then } \lim_{x \rightarrow \alpha^+} \frac{\sqrt{1 - \cos(p(x))}}{x + \alpha - 4}$$

is equal to

(1)  $\frac{3}{\sqrt{2}}$                                 (2)  $\frac{3}{2}$

(3)  $\frac{1}{\sqrt{2}}$                                 (4)  $\frac{1}{2}$

**Official Ans. by NTA (1)**

**Sol.**  $x^2 - x - 2 = 0$   
roots are 2 & -1

$$\Rightarrow \lim_{x \rightarrow 2^+} \frac{\sqrt{1 - \cos(x^2 - x - 2)}}{(x - 2)}$$

$$= \lim_{x \rightarrow 2^+} \frac{\sqrt{2 \sin^2 \left(\frac{x^2 - x - 2}{2}\right)}}{(x - 2)}$$

$$= \lim_{x \rightarrow 2^+} \frac{\sqrt{2} \sin \left(\frac{(x-2)(x+1)}{2}\right)}{(x - 2)}$$

$$= \frac{3}{\sqrt{2}}$$

21. Four fair dice are thrown independently 27 times. Then the expected number of times, at least two dice show up a three or a five, is \_\_\_\_.

**Official Ans. by NTA (11)**

**Sol.** 4 dice are independently thrown. Each die has probability to show 3 or 5 is

$$p = \frac{2}{6} = \frac{1}{3}$$

$$\therefore q = 1 - \frac{1}{3} = \frac{2}{3} \text{ (not showing 3 or 5)}$$

Experiment is performed with 4 dices independently.

$\therefore$  Their binomial distribution is

$$(q + p)^4 = (q)^4 + {}^4C_1 q^3 p + {}^4C_2 q^2 p^2 + {}^4C_3 q p^3 + {}^4C_4 p^4$$

∴ In one throw of each dice probability of showing 3 or 5 at least twice is  
 $= p^4 + {}^4C_3 qp^3 + {}^4C_2 q^2 p^2$   
 $= \frac{33}{81}$   
 ∴ Such experiment performed 27 times  
 ∴ so expected out comes = np  
 $= \frac{33}{81} \times 27$   
 $= 11$

22. If the line,  $2x - y + 3 = 0$  is at a distance  $\frac{1}{\sqrt{5}}$  and  $\frac{2}{\sqrt{5}}$  from the lines  $4x - 2y + \alpha = 0$  and  $6x - 3y + \beta = 0$ , respectively, then the sum of all possible values of  $\alpha$  and  $\beta$  is \_\_\_\_\_

**Official Ans. by NTA (30)**

**Sol.** Apply distance between parallel line formula  
 $4x - 2y + \alpha = 0$   
 $4x - 2y + 6 = 0$   
 $\left| \frac{\alpha - 6}{255} \right| = \frac{1}{55}$   
 $|\alpha - 6| = 2 \Rightarrow \alpha = 8, 4$   
 sum = 12  
 again  
 $6x - 3y + \beta = 0$   
 $6x - 3y + 9 = 0$   
 $\left| \frac{\beta - 9}{3\sqrt{5}} \right| = \frac{2}{\sqrt{5}}$   
 $|\beta - 9| = 6 \Rightarrow \beta = 15, 3$   
 sum = 18  
 sum of all values of  $\alpha$  and  $\beta$  is = 30

23. The natural number m, for which the coefficient of x in the binomial expansion of  $\left(x^m + \frac{1}{x^2}\right)^{22}$  is 1540, is \_\_\_\_\_.

**Official Ans. by NTA (13)**

**Sol.**  $T_{r+1} = {}^{22}C_r (x^m)^{22-r} \left(\frac{1}{x^2}\right)^r = {}^{22}C_r x^{22m-mr-2r}$   
 $= {}^{22}C_r x$

∴  ${}^{22}C_3 = {}^{22}C_{19} = 1540$   
 ∴ r = 3 or 19  
 $22m - mr - 2r = 1$   
 $m = \frac{2r+1}{22-5}$   
 $r = 3, m = \frac{7}{19} \notin \mathbb{N}$   
 $r = 19, m = \frac{38+1}{22-19} = \frac{39}{3} = 13$   
 $m = 13$

24. The number of words, with or without meaning, that can be formed by taking 4 letters at a time from the letters of the word 'SYLLABUS' such that two letters are distinct and two letters are alike, is \_\_\_\_\_.

**Official Ans. by NTA (240)**

**Sol.**  $S_2 Y L_2 A B U$

ABCC type words

$$= \underbrace{{}^2C_1}_{\text{selection of two alike letters}} \times \underbrace{{}^5C_2}_{\text{selection of two distinct letters}} \times \underbrace{\frac{4!}{2!}}_{\text{arrangement of selected letters}}$$

$$= 240$$

25. Let  $f(x) = x \cdot \left[ \frac{x}{2} \right]$ , for  $-10 < x < 10$ , where  $[t]$  denotes the greatest integer function. Then the number of points of discontinuity of f is equal to \_\_\_\_\_.

**Official Ans. by NTA (8)**

**Sol.**  $x \in (-10, 10)$

$$\frac{x}{2} \in (-5, 5) \rightarrow 9 \text{ integers}$$

check continuity at  $x = 0$

$$\left. \begin{aligned} f(0) &= 0 \\ f(0^+) &= 0 \\ f(0^-) &= 0 \end{aligned} \right\} \text{continuous at } x = 0$$

function will be discontinuous when

$$\frac{x}{2} = \pm 4, \pm 3, \pm 2, \pm 1$$

8 points of discontinuity