

FINAL JEE-MAIN EXAMINATION – APRIL, 2023

(Held On Monday 10th April, 2023)

TIME : 3 : 00 PM to 6 : 00 PM

MATHEMATICS

TEST PAPER WITH SOLUTION

SECTION-A

1. Let f be a continuous function satisfying $\int_0^t (f(x)+x^2) dx = \frac{4}{3}t^3, \forall t > 0$. Then $f\left(\frac{\pi^2}{4}\right)$ is

equal to :

(1) $\pi\left(1 - \frac{\pi^3}{16}\right)$

(2) $-\pi^2\left(1 + \frac{\pi^2}{16}\right)$

(3) $-\pi\left(1 + \frac{\pi^3}{16}\right)$

(4) $\pi^2\left(1 - \frac{\pi^2}{16}\right)$

Official Ans. by NTA (1)

Ans. (1)

Sol. $\int_0^t (f(x)+x^2) dx = \frac{4}{3}t^3, \forall t > 0$

$(f(t^2)+t^4) = 2t$

$f(t^2) = 2t - t^4$

$t = \frac{\pi}{2} \Rightarrow f\left(\frac{\pi^2}{4}\right) = \frac{2\pi}{2} - \frac{\pi^4}{16}$

$= \pi - \frac{\pi^4}{16} = \pi\left(1 - \frac{\pi^3}{16}\right)$

2. Eight persons are to be transported from city A to city B in three cars of different makes. If each car can accommodate at most three persons, then the number of ways, in which they can be transported, is:

(1) 3360

(2) 1680

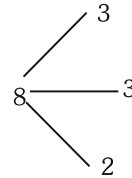
(3) 560

(4) 1120

Official Ans. by NTA (1)

Ans. (2)

Sol.



Ways = $\frac{8!}{3!3!2!} \times 3!$

$= \frac{8 \times 7 \times 6 \times 5 \times 4}{4}$

$= 56 \times 30$

$= 1680$

3. For, $\alpha, \beta, \gamma, \delta \in \mathbb{N}$, if

$\int \left(\left(\frac{x}{e}\right)^{2x} + \left(\frac{e}{x}\right)^{2x} \right) \log_e x dx = \frac{1}{\alpha} \left(\frac{x}{e}\right)^{\beta x} - \frac{1}{\gamma} \left(\frac{e}{x}\right)^{\delta x} + C,$

Where $e = \sum_{n=0}^{\infty} \frac{1}{n!}$ and C is constant of integration,

then $\alpha + 2\beta + 3\gamma - 4\delta$ is equal to:

(1) 1

(2) -4

(3) -8

(4) 4

Official Ans. by NTA (4)

Ans. (4)

Sol. $(x = e^{\ln x})$

$\int \left(\left(\frac{x}{e}\right)^{2x} + \left(\frac{e}{x}\right)^{2x} \right) \log_e x dx = \int [e^{2(x \ln x - x)} + e^{-2(x \ln x - x)}] \ln x dx$

$x \ln x - x = t$

$\ln x \cdot dx = dt$

$\int (e^{2t} + e^{-2t}) dt$

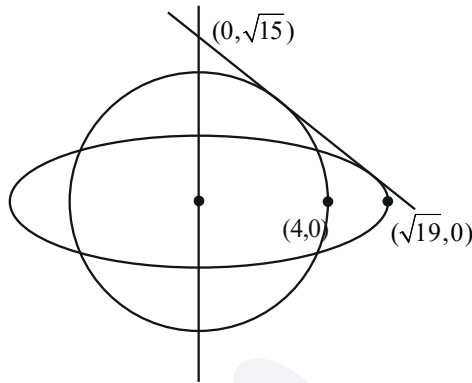
$\frac{e^{2t}}{2} - \frac{e^{-2t}}{2} + C$

$= \frac{1}{2} \left(\frac{x}{e}\right)^{2x} - \frac{1}{2} \left(\frac{e}{x}\right)^{2x} + C$

$\alpha = \beta = \gamma = \delta = 2$

$\alpha + 2\beta + 3\gamma - 4\delta = 4$

Sol. $\frac{x^2}{19} + \frac{y^2}{15} = 1$



Let tang be

$$y = mx \pm \sqrt{19m^2 + 15}$$

$$mx - y \pm \sqrt{19m^2 + 15} = 0$$

Parallel from $(0, 0) = 4$

$$\left| \frac{\pm \sqrt{19m^2 + 15}}{\sqrt{m^2 + 1}} \right| = 4$$

$$19m^2 + 15 = 16m^2 + 16$$

$$3m^2 = 1$$

$$m = \pm \frac{1}{\sqrt{3}}$$

$$\theta = \frac{\pi}{6} \text{ with x-axis}$$

$$\text{Required angle } \frac{\pi}{3}$$

11. Let $\vec{a} = 2\hat{i} + 7\hat{j} - \hat{k}$, $\vec{b} = 3\hat{i} + 5\hat{k}$ and $\vec{c} = \hat{i} - \hat{j} + 2\hat{k}$

. Let \vec{d} be a vector which is perpendicular to both \vec{a} and \vec{b} , and $\vec{c} \cdot \vec{d} = 12$. Then

$$(-\hat{i} + \hat{j} - \hat{k}) \cdot (\vec{c} \times \vec{d}) \text{ is equal to}$$

(1) 48

(2) 42

(3) 44

(4) 24

Official Ans. by NTA (3)

Ans. (3)

Sol. $\vec{a} = 2\hat{i} + 7\hat{j} - \hat{k}$

$$\vec{b} = 3\hat{i} + 5\hat{k}$$

$$\vec{c} = \hat{i} - \hat{j} + 2\hat{k}$$

$$\vec{d} = \lambda(\vec{a} \times \vec{b}) = \lambda \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 2 & 7 & -1 \\ 3 & 0 & 5 \end{vmatrix}$$

$$\vec{d} = \lambda(35\hat{i} - 13\hat{j} - 21\hat{k})$$

$$\lambda(35 + 13 - 42) = 12$$

$$\lambda = 2$$

$$\vec{d} = 2(35\hat{i} - 13\hat{j} - 21\hat{k})$$

$$(\hat{i} + \hat{j} - \hat{k})(\vec{c} \times \vec{d})$$

$$= \begin{vmatrix} -1 & 1 & -1 \\ 1 & -1 & 2 \\ 70 & -26 & -42 \end{vmatrix} = 44$$

12. If $S_n = 4 + 11 + 21 + 34 + 50 + \dots$ to n terms,

then $\frac{1}{60}(S_{29} - S_9)$ is equal to

(1) 226

(2) 220

(3) 223

(4) 227

Official Ans. by NTA (3)

Ans. (3)

Sol. $S_n = 4 + 11 + 21 + 34 + 50 + \dots + n$ terms
Difference are in A.P.

$$\text{Let } T_n = an^2 + bn + c$$

$$T_1 = a + b + c = 4$$

$$T_2 = 4a + 2b + c = 11$$

$$T_3 = 9a + 3b + c = 21$$

By solving these 3 equations

$$a = \frac{3}{2}, b = \frac{5}{2}, c = 0$$

$$\text{So } T_n = \frac{3}{2}n^2 + \frac{5}{2}n$$

$$S_n = \sum T_n$$

$$= \frac{3}{2} \sum n^2 + \frac{5}{2} \sum n$$

$$= \frac{3}{2} \frac{n(n+1)(2n+1)}{6} + \frac{5}{2} \frac{(n)(n+1)}{2}$$

$$= \frac{n(n+1)}{4} [2n+1+5]$$

$$S_n = \frac{n(n+1)}{4} (2n+6) = \frac{n(n+1)(n+3)}{2}$$

$$\frac{1}{60} \left(\frac{29 \times 30 \times 32}{2} - \frac{9 \times 10 \times 12}{2} \right) = 223$$

17. Let the line $\frac{x}{1} = \frac{6-y}{2} = \frac{z+8}{5}$ intersect the lines $\frac{x-5}{4} = \frac{y-7}{3} = \frac{z+2}{1}$ and $\frac{x+3}{6} = \frac{3-y}{3} = \frac{z-6}{1}$ at the points A and B respectively. Then the distance of the mid-point of the line segment AB from the plane $2x - 2y + z = 14$ is

- (1) 4 (2) $\frac{10}{3}$
 (3) 3 (4) $\frac{11}{3}$

Official Ans. by NTA (1)

Ans. (1)

Sol. $\frac{x}{1} = \frac{y-6}{-2} = \frac{z+8}{5} = \lambda$ (1)

$\frac{x-5}{4} = \frac{y-7}{3} = \frac{z+2}{1} = \mu$ (2)

$\frac{x+3}{4} = \frac{y-3}{-3} = \frac{z-6}{1} = \gamma$ (3)

Intersection of (1) & (2) "A"

$(\lambda, -2\lambda + 6, 5\lambda - 8)$ & $(4\mu + 5, 3\mu + 7, \mu - 2)$

$\lambda = 1, \mu = -1$

A(1, 4, -3)

Intersection of (1) & (3) "B"

$(\lambda, -2\lambda + 6, 5\lambda - 8)$ & $(6\gamma - 3, -3\gamma + 3, \gamma + 6)$

$\lambda = 3$

$\gamma = 1$

B(3, 0, 7)

Mid point of A & B $\Rightarrow (2, 2, 2)$

Perpendicular distance from the plane

$2x - 2y + z = 14$

$\Rightarrow \left| \frac{2(2) - 2(2) + 2 - 14}{\sqrt{4 + 4 + 1}} \right| = 4$

18. Let $S = \left\{ z = x + iy : \frac{2z - 3i}{4z + 2i} \text{ is a real number} \right\}$.

Then which of the following is NOT correct?

- (1) $y + x^2 + y^2 \neq -\frac{1}{4}$
 (2) $x = 0$
 (3) $(x, y) = \left(0, -\frac{1}{2} \right)$
 (4) $y \in \left(-\infty, -\frac{1}{2} \right) \cup \left(-\frac{1}{2}, \infty \right)$

Official Ans. by NTA (3)

Ans. (3)

Sol. $\frac{2z - 3i}{4z + 2i} \in \mathbb{R}$

$\frac{2(x + iy) - 3i}{4(x + iy) + 2i} = \frac{2x + (2y - 3)i}{4x + (4y + 2)i} \times \frac{4x - (4y + 2)i}{4x - (4y + 2)i}$

$4x(2y - 3) - 2x(4y + 2) = 0$

$x = 0 \quad y \neq -\frac{1}{2}$

Ans. = 3

19. Let the number $(22)^{2022} + (2022)^{22}$ leave the remainder α when divided by 3 and β when divided by 7. Then $(\alpha^2 + \beta^2)$ is equal to

- (1) 10
 (2) 5
 (3) 20
 (4) 13

Official Ans. by NTA (2)

Ans. (2)

Sol. $(22)^{2022} + (2022)^{22}$

divided by 3

$(21 + 1)^{2022} + (2022)^{22}$

$= 3k + 1 \quad (\alpha = 1)$

Divided by 7

$(21 + 1)^{2022} + (2023 - 1)^{22}$

$7k + 1 + 1 \quad (\beta = 2)$

$7k + 2$

So $\alpha^2 + \beta^2 \Rightarrow 5$

20. Let μ be the mean and σ be the standard deviation of the distribution

x_i	0	1	2	3	4	5
f_i	$k + 2$	$2k$	$k^2 - 1$	$k^2 - 1$	$k^2 + 1$	$k - 3$

where $\sum f_i = 62$. if $[x]$ denotes the greatest integer $\leq x$, then $[\mu^2 + \sigma^2]$ is equal

- (1) 8
 (2) 7
 (3) 6
 (4) 9

Official Ans. by NTA (1)

Ans. (1)

Sol. $\sum f_i = 62$
 $\Rightarrow 3k^2 + 16k - 12k - 64 = 0$
 $\Rightarrow k = \text{or } -\frac{16}{3}$ (rejected)
 $\mu = \frac{\sum f_i x_i}{\sum f_i}$
 $\mu = \frac{8 + 2(15) + 3(15) + 4(17) + 5}{62} = \frac{156}{62}$
 $\sigma^2 = \sum f_i x_i^2 - \left(\sum f_i x_i\right)^2$
 $= \frac{8 \times 1^2 + 15 \times 13 + 17 \times 16 + 25}{62} - \left(\frac{156}{62}\right)^2$
 $\sigma^2 = \frac{500}{62} - \left(\frac{156}{62}\right)^2$
 $\sigma^2 + \mu^2 = \frac{500}{62}$
 $[\sigma^2 + \mu^2] = 8$

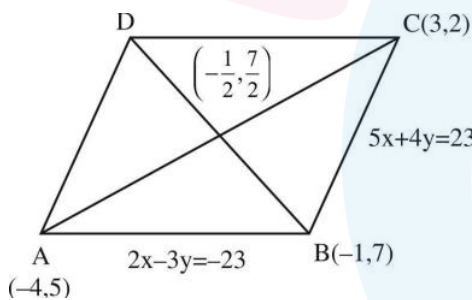
SECTION-B

21. Let the equations of two adjacent sides of a parallelogram ABCD be $2x - 3y = -23$ and $5x + 4y = 23$. If the equation of its one diagonal AC is $3x + 7y = 23$ and the distance of A from the other diagonal is d, then $50 d^2$ is equal to _____.

Official Ans. by NTA (529)

Ans. (529)

Sol.



A & C point will be $(-4, 5)$ & $(3, 2)$

mid point of AC will be $\left(-\frac{1}{2}, \frac{7}{2}\right)$

equation of diagonal BD is

$$y - \frac{7}{2} = \frac{\frac{7}{2} - 5}{-\frac{1}{2} - 3} \left(x + \frac{1}{2}\right)$$

$\Rightarrow 7x + y = 0$

Distance of A from diagonal BD

$$= d = \frac{23}{\sqrt{50}}$$

$\Rightarrow 50d^2 = (23)^2$

$50d^2 = 529$

22. Let S be the set of values of λ , for which the system of equations

$$6\lambda x - 3y + 3z = 4\lambda^2,$$

$$2x + 6\lambda y + 4z = 1,$$

$$3x + 2y + 3\lambda z = \lambda \text{ has no solution. Then } 12 \sum_{\lambda \in S} |\lambda|$$

is equal to _____.

Official Ans. by NTA (24)

Ans. (24)

Sol. $\Delta = \begin{vmatrix} 6\lambda & -3 & 3 \\ 2 & 6\lambda & 4 \\ 3 & 2 & 3\lambda \end{vmatrix} = 0$ (For No Solution)

$$2\lambda(9\lambda^2 - 4) + (3\lambda - 6) + (2 - 9\lambda) = 0$$

$$18\lambda^3 - 14\lambda - 4 = 0$$

$$(\lambda - 1)(3\lambda + 1)(3\lambda + 2) = 0$$

$$\Rightarrow \lambda = 1, -1/3, -2/3$$

For each λ , $\Delta_1 = \begin{vmatrix} 6\lambda & -3 & 4\lambda^2 \\ 2 & 6\lambda & 1 \\ 3 & 2 & \lambda \end{vmatrix} \neq 0$

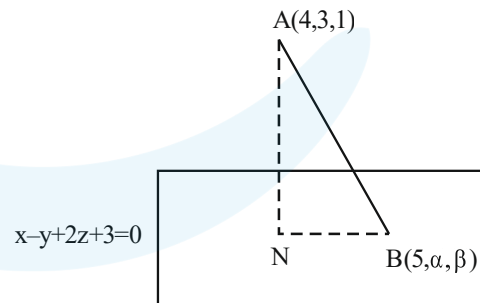
Ans. $12 \left(1 + \frac{1}{3} + \frac{2}{3}\right) = 24$

23. Let the foot of perpendicular from the point A(4, 3, 1) on the plane P : $x - y + 2z + 3 = 0$ be N. If B(5, α , β), $\alpha, \beta \in \mathbb{Z}$ is a point on plane P such that the area of the triangle ABN is $3\sqrt{2}$, then $\alpha^2 + \beta^2 + \alpha\beta$ is equal to _____.

Official Ans. by NTA (7)

Ans. (7)

Sol.



$$AN = \sqrt{6}$$

$$5 - \alpha + 2\beta + 3 = 0$$

$\Rightarrow \alpha = 8 + 2\beta \dots (1)$

N is given by

$$\frac{x-4}{1} = \frac{y-3}{-1} = \frac{z-1}{2} = \frac{-(4-3+2+3)}{1+1+4}$$

$$\Rightarrow x = 3, y = 4, z = -1$$

$$\Rightarrow N \text{ is } (3, 4, -1)$$

$$BN = \sqrt{4 + (\alpha - 4)^2 + (\beta + 1)^2}$$

$$= \sqrt{4 + (2\beta + 4)^2 + (\beta + 1)^2}$$

$$\text{Area of } \triangle ABN = \frac{1}{2} AN \times BN = 3\sqrt{2}$$

$$\Rightarrow \frac{1}{2} \times \sqrt{6} \times BN = 3\sqrt{2}$$

$$BN = 2\sqrt{3}$$

$$\Rightarrow 4 + (2\beta + 4)^2 + (\beta + 1)^2 = 12$$

$$(2\beta + 4)^2 + (\beta + 1)^2 - 8 = 0$$

$$5\beta^2 + 18\beta + 9 = 0$$

$$(5\beta + 3)(\beta + 3) = 0$$

$$\beta = -3$$

$$\Rightarrow \alpha = 2$$

$$\Rightarrow \alpha^2 + \beta^2 + \alpha\beta = 9 + 4 - 6 = 7$$

24. Let quadratic curve passing through the point $(-1, 0)$ and touching the line $y = x$ at $(1, 1)$ be $y = f(x)$. Then the x-intercept of the normal to the curve at the point $(\alpha, \alpha + 1)$ in the first quadrant is _____.

Official Ans. by NTA (11)

Ans. (11)

Sol. $f(x) = (x + 1)(ax + b)$

$$1 = 2a + 2b \quad (1)$$

$$f(x) = (ax + b) + a(x + 1)$$

$$1 = (3a + b) \quad (2)$$

$$\Rightarrow b = 1/4, a = 1/4$$

$$f(x) = \frac{(x+1)^2}{4}$$

$$f'(x) = \frac{x}{2} + \frac{1}{2}$$

$$\alpha + 1 = \frac{(\alpha + 1)^2}{4}, \alpha > -1$$

$$\alpha + 1 = 4$$

$$\alpha = 3$$

normal at $(3, 4)$

$$y - 4 = -\frac{1}{2}(x - 3)$$

$$y = 0$$

$$x = 8 + 3$$

Ans. 11

25. Let the tangent at any point P on a curve passing through the points $(1, 1)$ and $(\frac{1}{10}, 100)$, intersect positive x-axis and y-axis at the points A and B respectively. If $PA : PB = 1 : k$ and $y = y(x)$ is the solution of the differential equation $e^{\frac{dy}{dx}} = kx + \frac{k}{2}$, $y(0) = k$, then $4y(1) - 5\log_e 3$ is equal to _____.

Official Ans. by NTA (6)

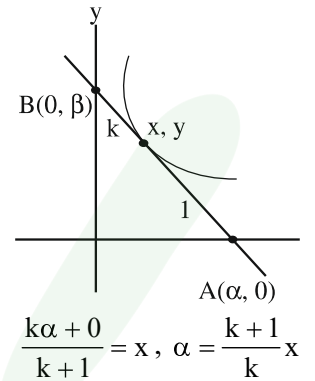
Ans. (5) (answer is $4 + \ln 3$)

Sol. equation of tangent at P (x, y)

$$Y - y = \frac{dy}{dx}(X - x)$$

$$Y = 0$$

$$X = \frac{-y dx}{dy} + x$$



$$\frac{k+1}{k}x = -y \frac{dx}{dy} + x$$

$$x + \frac{x}{k} = -y \frac{dx}{dy} + x$$

$$x \frac{dy}{dx} + ky = 0$$

$$\frac{dy}{dx} + \frac{k}{x}y = 0$$

$$y \cdot x^k = C$$

$$C = 1$$

$$100 \cdot \left(\frac{1}{10}\right)^k = 1$$

$$k = 2$$

$$\frac{dy}{dx} = \ln(2x + 1)$$

$$y = \frac{(2x + 1)}{2} (\ln(2x + 1) - 1) + c$$

$$2 = \frac{1}{2}(0 - 1) + C$$

$$C = 2 + \frac{1}{2} = \frac{5}{2}$$

$$y(1) = \frac{3}{2}(\ln 3 - 1) + \frac{5}{2}$$

$$= \frac{3}{2} \ln 3 + 1$$

$$4y(1) = 6 \ln 3 + 4$$

$$4y(1) - 5 \ln 3 = 4 + \ln 3$$

26. Suppose a_1, a_2, a_3, a_4 be in an arithmetico-geometric progression. If the common ratio of the corresponding geometric progression is 2 and the sum of all 5 terms of the arithmetico-geometric progression is $\frac{49}{2}$, then a_4 is equal to _____.

Official Ans. by NTA (16)

Ans. (16)

Sol. $\frac{(a-2d)}{4}, \frac{(a-d)}{2}, a, 2(a+d), 4(a+2d)$

$a = 2$

$$\left(\frac{1}{4} + \frac{1}{2} + 1 + 6\right) \times 2 + (-1 + 2 + 8)d = \frac{49}{2}$$

$$2\left(\frac{3}{4} + 7\right) + 9d = \frac{49}{2}$$

$$9d = \frac{49}{2} - \frac{62}{4} = \frac{98 - 62}{4} = 9$$

$d = 1$

$$\Rightarrow a_4 = 4(a + 2d) = 16$$

27. If the domain of the function $f(x) = \sec^{-1}\left(\frac{2x}{5x+3}\right)$ is $[\alpha, \beta] \cup (\gamma, \delta]$, then $|3\alpha + 10(\beta + \gamma) + 21\delta|$ is equal to _____.

Official Ans. by NTA (24)

Ans. (24)

Sol. $f(x) = \sec^{-1}\frac{2x}{5x+3}$

$$\left|\frac{2x}{5x+3}\right|$$

$$\left|\frac{2x}{5x+3}\right| \geq 1 \Rightarrow |2x| \geq |5x+3|$$

$$(2x)^2 - (5x+3)^2 \geq |5x+3|$$

$$(7x+3)(-3x-3) \geq 0$$

$$\frac{-}{-1} + \frac{-}{-\frac{3}{7}}$$

\therefore domain $\left[-1, \frac{-3}{5}\right] \cup \left(\frac{-3}{5}, \frac{-3}{7}\right]$

$$\alpha = -1, \beta = \frac{-3}{5}, \gamma = \frac{-3}{5}, \delta = \frac{-3}{7}$$

$$3\alpha + 10(\beta + \gamma) + 21\delta = -3$$

$$-3 + 10\left(\frac{-6}{5}\right) + \left(\frac{-3}{7}\right) 21 = -24$$

28. The sum of all the four-digit numbers that can be formed using all the digits 2, 1, 2, 3 is equal to _____.

Official Ans. by NTA (26664)

Ans. (26664)

Sol. 2, 1, 2, 3

$$_ _ _ _ \quad \underline{1} \quad \frac{3!}{2!} = 3$$

$$_ _ _ _ \quad \underline{2} \quad \frac{3!}{1!} = 6$$

$$_ _ _ _ \quad \underline{3} \quad \frac{3!}{2!} = 3$$

Sum of digits of unit place = $3 \times 1 + 6 \times 2 + 3 \times 3 = 24$

\therefore required sum

$$= 24 \times 1000 + 24 \times 100 + 24 \times 10 + 24 \times 1$$

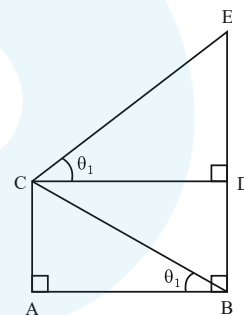
$$= 24 \times 1111$$

Ans ; 26664

29. In the figure, $\theta_1 + \theta_2 = \frac{\pi}{2}$ and $\sqrt{3}(BE) = 4(AB)$.

If the area of ΔCAB is $2\sqrt{3} - 3$ unit², when $\frac{\theta_2}{\theta_1}$ is

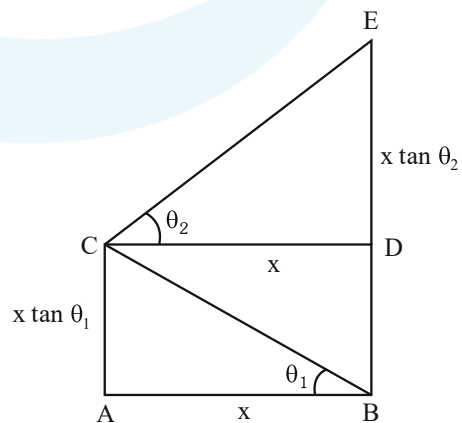
the largest, then the perimeter (in unit) of ΔCED is equal to _____.



Official Ans. by NTA (6)

Ans. (6)

Sol.



$$\sqrt{3} BE = 4 AB$$

$$\text{Ar}(\Delta CAB) = 2\sqrt{3} - 3$$

$$\frac{1}{2}x^2 \tan \theta_1 = 2\sqrt{3} - 3$$

$$BE = BD + DE$$

$$= x (\tan \theta_1 + \tan \theta_2)$$

$$BE = AB (\tan \theta_1 + \cot \theta_1)$$

$$\frac{4}{\sqrt{3}} \tan \theta_1 + \cot \theta_1 \Rightarrow \tan \theta_1 = \sqrt{3}, \frac{1}{\sqrt{3}}$$

$$\theta_1 = \frac{\pi}{6}$$

$$\theta_2 = \frac{\pi}{3}$$

$$\theta_1 = \frac{\pi}{3}$$

$$\theta_2 = \frac{\pi}{6}$$

$$\text{as } \frac{\theta_2}{\theta_1} \text{ is largest } \therefore \theta_1 = \frac{\pi}{6} \quad \theta_2 = \frac{\pi}{3}$$

$$\therefore x^2 = \frac{(2\sqrt{3} - 3) \times 2}{\tan \theta_1} = \frac{\sqrt{3}(2 - \sqrt{3}) \times 2}{\tan \frac{\pi}{6}}$$

$$x^2 = 12 - 6\sqrt{3} = (3 - \sqrt{3})^2$$

$$x = 3 - \sqrt{3}$$

Perimeter of ΔCED

$$= CD + DE + CE$$

$$= 3\sqrt{3} + (3 - \sqrt{3})\sqrt{3} + (3 - \sqrt{3}) \times 2 = 6$$

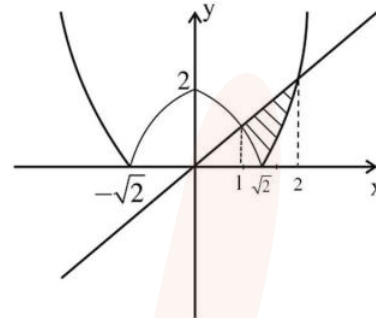
Ans : 6

30. If the area of the region $\{(x, y) : |x^2 - 2| \leq y \leq x\}$ is A, then $6A + 16\sqrt{2}$ is equal to _____ .

Official Ans. by NTA (27)

Ans. (27)

Sol. $|x^2 - 2| \leq y \leq x$



$$A = \int_1^{\sqrt{2}} (x - (2 - x^2)) dx + \int_{\sqrt{2}}^2 (x - (x^2 - 2)) dx$$

$$= \left(1 - 2\sqrt{2} + \frac{2\sqrt{2}}{3}\right) - \left(\frac{1}{2} - 2 + \frac{1}{3}\right) + \left(2 - \frac{8}{3} + 4\right) - \left(1 - \frac{2\sqrt{2}}{3} + 2\sqrt{2}\right)$$

$$= -4\sqrt{2} + \frac{4\sqrt{2}}{3} + \frac{7}{6} + \frac{10}{3} = \frac{-8\sqrt{2}}{3} + \frac{9}{2}$$

$$6A = -16\sqrt{2} + 27 \therefore 6A + 16\sqrt{2} = 27$$

Ans : 27