## Question 1:

Reduce the following equations into slope-intercept form and find their slopes and the yintercepts.

(i) 
$$x + 7y = 0$$
 (ii)  $6x + 3y - 5 = 0$  (iii)  $y = 0$ 

Answer

(i) The given equation is x + 7y = 0.

It can be written as

$$y = -\frac{1}{7}x + 0$$
 ...(1)

This equation is of the form y = mx + c, where  $m = -\frac{1}{7}$  and c = 0Therefore, equation (1)

Therefore, equation (1) is in the slope-intercept form, where the slope and the y-

 $-\frac{1}{7} \text{ and 0 respectively.}$ 

(ii) The given equation is 6x + 3y - 5 = 0.

It can be written as

$$y = \frac{1}{3}(-6x+5)$$
$$y = -2x + \frac{5}{3} \qquad ...(2)$$

This equation is of the form y = mx + c, where m = -2 and  $c = \frac{5}{3}$ .

Therefore, equation (2) is in the slope-intercept form, where the slope and the y-

intercept are -2 and  $\frac{3}{3}$  respectively.

(iii) The given equation is y = 0.

It can be written as

$$y = 0.x + 0 \dots (3)$$

This equation is of the form y = mx + c, where m = 0 and c = 0.

Therefore, equation (3) is in the slope-intercept form, where the slope and the yintercept are 0 and 0 respectively.

#### Question 2:

Reduce the following equations into intercept form and find their intercepts on the axes.

(i) 
$$3x + 2y - 12 = 0$$
 (ii)  $4x - 3y = 6$  (iii)  $3y + 2 = 0$ .

Answer

(i) The given equation is 3x + 2y - 12 = 0.

It can be written as

$$3x + 2y = 12$$

$$\frac{3x}{12} + \frac{2y}{12} = 1$$

i.e., 
$$\frac{x}{4} + \frac{y}{6} = 1$$
 ...(1)

$$\frac{x}{y} + \frac{y}{z} = 1$$

 $\frac{x}{a} + \frac{y}{b} = 1$  This equation is of the form  $\frac{x}{a} + \frac{y}{b} = 1$  , where a = 4 and b = 6.

Therefore, equation (1) is in the intercept form, where the intercepts on the x and y axes are 4 and 6 respectively.

(ii) The given equation is 4x - 3y = 6.

It can be written as

$$\frac{4x}{6} - \frac{3y}{6} = 1$$

$$\frac{2x}{3} - \frac{y}{2} = 1$$

i.e., 
$$\frac{x}{\left(\frac{3}{2}\right)} + \frac{y}{\left(-2\right)} = 1$$
 ...(2)

This equation is of the form  $\frac{x}{a} + \frac{y}{b} = 1$  , where  $a = \frac{3}{2}$  and b = -2.

Therefore, equation (2) is in the intercept form, where the intercepts on the x and y axes

$$\frac{3}{2}$$
 and -2 respectively.

(iii) The given equation is 3y + 2 = 0.

It can be written as

$$3y = -2$$

i.e., 
$$\frac{y}{\left(-\frac{2}{3}\right)} = 1$$
 ...(3)

 $\frac{x}{a} + \frac{y}{b} = 1$  This equation is of the form  $\frac{x}{a} + \frac{y}{b} = 1$  , where a = 0 and  $b = -\frac{2}{3}$  .

Therefore, equation (3) is in the intercept form, where the intercept on the y-axis is  $\frac{1}{3}$  and it has no intercept on the x-axis.

#### Question 3:

Find the distance of the point (-1, 1) from the line 12(x + 6) = 5(y - 2).

Answer

The given equation of the line is 12(x + 6) = 5(y - 2).

$$\Rightarrow 12x + 72 = 5y - 10$$

$$\Rightarrow 12x - 5y + 82 = 0 \dots (1)$$

On comparing equation (1) with general equation of line Ax + By + C = 0, we obtain A = 12, B = -5, and C = 82.

It is known that the perpendicular distance (d) of a line Ax + By + C = 0 from a point

$$(x_1, y_1)$$
 is given by  $d = \frac{\left|Ax_1 + By_1 + C\right|}{\sqrt{A^2 + B^2}}$ .

The given point is  $(x_1, y_1) = (-1, 1)$ .

Therefore, the distance of point (-1, 1) from the given line

$$= \frac{\left|12(-1)+(-5)(1)+82\right|}{\sqrt{(12)^2+(-5)^2}} \text{ units} = \frac{\left|-12-5+82\right|}{\sqrt{169}} \text{ units} = \frac{\left|65\right|}{13} \text{ units} = 5 \text{ units}$$

#### Question 4:

Find the points on the x-axis, whose distances from the line  $\frac{x}{3} + \frac{y}{4} = 1$  are 4 units. Answer

The given equation of line is

$$\frac{x}{3} + \frac{y}{4} = 1$$
  
or,  $4x + 3y - 12 = 0$  ...(1)

On comparing equation (1) with general equation of line Ax + By + C = 0, we obtain A = 4, B = 3, and C = -12.

Let (a, 0) be the point on the x-axis whose distance from the given line is 4 units.

It is known that the perpendicular distance (d) of a line Ax + By + C = 0 from a point

$$(x_1, y_1)$$
 is given by  $d = \frac{\left|Ax_1 + By_1 + C\right|}{\sqrt{A^2 + B^2}}$ .

Therefore,

$$4 = \frac{|4a + 3 \times 0 - 12|}{\sqrt{4^2 + 3^2}}$$

$$\Rightarrow 4 = \frac{|4a - 12|}{5}$$

$$\Rightarrow |4a - 12| = 20$$

$$\Rightarrow \pm (4a - 12) = 20 \text{ or } -(4a - 12) = 20$$

$$\Rightarrow 4a = 20 + 12 \text{ or } 4a = -20 + 12$$

$$\Rightarrow a = 8 \text{ or } -2$$

Thus, the required points on the x-axis are (-2, 0) and (8, 0).

#### **Question 5:**

Find the distance between parallel lines

(i) 
$$15x + 8y - 34 = 0$$
 and  $15x + 8y + 31 = 0$ 

(ii) 
$$I(x + y) + p = 0$$
 and  $I(x + y) - r = 0$ 

Answer

It is known that the distance (d) between parallel lines  $Ax + By + C_1 = 0$  and  $Ax + By + C_2 = 0$ 

$$d = \frac{\left|C_1 - C_2\right|}{\sqrt{A^2 + B^2}}$$

(i) The given parallel lines are 15x + 8y - 34 = 0 and 15x + 8y + 31 = 0.

Here, 
$$A = 15$$
,  $B = 8$ ,  $C_1 = -34$ , and  $C_2 = 31$ .

Therefore, the distance between the parallel lines is

$$d = \frac{|C_1 - C_2|}{\sqrt{A^2 + B^2}} = \frac{|-34 - 31|}{\sqrt{(15)^2 + (8)^2}} \text{ units} = \frac{|-65|}{17} \text{ units} = \frac{65}{17} \text{ units}$$

(ii) The given parallel lines are I(x + y) + p = 0 and I(x + y) - r = 0.

$$lx + ly + p = 0$$
 and  $lx + ly - r = 0$ 

Here, 
$$A = I$$
,  $B = I$ ,  $C_1 = p$ , and  $C_2 = -r$ .

Therefore, the distance between the parallel lines is

$$d = \frac{|C_1 - C_2|}{\sqrt{A^2 + B^2}} = \frac{|p + r|}{\sqrt{I^2 + I^2}} \text{ units} = \frac{|p + r|}{\sqrt{2I^2}} \text{ units} = \frac{|p + r|}{I\sqrt{2}} \text{ units} = \frac{1}{\sqrt{2}} \left| \frac{p + r}{I} \right| \text{ units}$$

#### Question 6:

Find equation of the line parallel to the line 3x - 4y + 2 = 0 and passing through the point (-2, 3).

Answer

The equation of the given line is

$$3x - 4y + 2 = 0$$

or 
$$y = \frac{3x}{4} + \frac{2}{4}$$

or 
$$y = \frac{3}{4}x + \frac{1}{2}$$
, which is of the form  $y = mx + c$ 

$$\therefore \text{ Slope of the given line} = \frac{3}{4}$$

It is known that parallel lines have the same slope.

$$\therefore \text{ Slope of the other line} = \frac{m = \frac{3}{4}}{4}$$

Now, the equation of the line that has a slope of  $\frac{1}{4}$  and passes through the point (-2, 3) is

$$(y-3) = \frac{3}{4} \{x-(-2)\}$$

$$4y-12=3x+6$$

i.e., 
$$3x-4y+18=0$$

#### Question 7:

Find equation of the line perpendicular to the line x - 7y + 5 = 0 and having x intercept 3.

Answer

The given equation of line is x-7y+5=0.

Or, 
$$y = \frac{1}{7}x + \frac{5}{7}$$
, which is of the form  $y = mx + c$ 

∴Slope of the given line  $=\frac{1}{7}$ 

$$m = -\frac{1}{\left(\frac{1}{7}\right)} = -7$$

 $m=-\frac{1}{\left(\frac{1}{7}\right)}=-7$  The slope of the line perpendicular to the line having a slope of  $\frac{1}{7}$  is The equation of the line with slope -7 and values  $v=m^{2}$ 

$$y = m (x - d)$$
$$\Rightarrow y = -7 (x - 3)$$

$$\Rightarrow y = -7x + 21$$

$$\Rightarrow 7x + y = 21$$

## Question 8:

Find angles between the lines  $\sqrt{3}x + y = 1$  and  $x + \sqrt{3}y = 1$ Answer

The given lines are  $\sqrt{3}x + y = 1$  and  $x + \sqrt{3}y = 1$ 

$$y = -\sqrt{3}x + 1$$
 ...(1) and  $y = -\frac{1}{\sqrt{3}}x + \frac{1}{\sqrt{3}}$  ...(2)

The slope of line (1) is  $m_{\rm l}=-\sqrt{3}$  , while the slope of line (2) is  $m_{\rm l}=-\frac{1}{\sqrt{3}}$  . The acute angle i.e.,  $\theta$  between the two lines is given by

$$\tan \theta = \left| \frac{m_1 - m_2}{1 + m_1 m_2} \right|$$

$$\tan \theta = \left| \frac{-\sqrt{3} + \frac{1}{\sqrt{3}}}{1 + \left(-\sqrt{3}\right)\left(-\frac{1}{\sqrt{3}}\right)} \right|$$

$$\tan \theta = \left| \frac{\frac{-3 + 1}{\sqrt{3}}}{1 + 1} \right| = \left| \frac{-2}{2 \times \sqrt{3}} \right|$$

$$\tan \theta = \frac{1}{\sqrt{3}}$$

Thus, the angle between the given lines is either  $30^{\circ}$  or  $180^{\circ} - 30^{\circ} = 150^{\circ}$ .

## Question 9:

The line through the points (h, 3) and (4, 1) intersects the line 7x - 9y - 19 = 0. at right angle. Find the value of h.

Answer

The slope of the line passing through points (h, 3) and (4, 1) is

$$m_1 = \frac{1-3}{4-h} = \frac{-2}{4-h}$$

The slope of line 7x - 9y - 19 = 0 or  $y = \frac{7}{9}x - \frac{19}{9}$  is  $m_2 = \frac{7}{9}$ .

It is given that the two lines are perpendicular.

$$\therefore m_1 \times m_2 = -1$$

$$\Rightarrow \left(\frac{-2}{4-h}\right) \times \left(\frac{7}{9}\right) = -1$$

$$\Rightarrow \frac{-14}{36-9h} = -1$$

$$\Rightarrow 14 = 36-9h$$

$$\Rightarrow 9h = 36-14$$

$$\Rightarrow h = \frac{22}{9}$$

Thus, the value of h is  $\frac{22}{9}$ .

## Question 10:

Prove that the line through the point  $(x_1, y_1)$  and parallel to the line Ax + By + C = 0 is A  $(x - x_1) + B(y - y_1) = 0$ .

Answer

The slope of line Ax + By + C = 0 or  $y = \left(\frac{-A}{B}\right)x + \left(\frac{-C}{B}\right)_{is} m = -\frac{A}{B}$ 

It is known that parallel lines have the same slope.

∴ Slope of the other line = 
$$m = -\frac{A}{B}$$

The equation of the line passing through point  $(x_1, y_1)$  and having a slope  $m = -\frac{A}{B}$  is

$$y - y_{1} = m(x - x_{1})$$

$$y - y_{1} = -\frac{A}{B}(x - x_{1})$$

$$B(y - y_{1}) = -A(x - x_{1})$$

$$A(x - x_{1}) + B(y - y_{1}) = 0$$

Hence, the line through point  $(x_1, y_1)$  and parallel to line Ax + By + C = 0 is  $A(x-x_1) + B(y-y_1) = 0$ 

#### Question 11:

Two lines passing through the point (2, 3) intersects each other at an angle of 60°. If slope of one line is 2, find equation of the other line.

Answer

It is given that the slope of the first line,  $m_1 = 2$ .

Let the slope of the other line be  $m_2$ .

The angle between the two lines is 60°.

The equation of the line passing through point (2, 3) and having a slope of  $\frac{(2\sqrt{3}+1)}{(2\sqrt{3}+1)}$  is

$$(y-3) = \frac{2-\sqrt{3}}{2\sqrt{3}+1}(x-2)$$

$$(2\sqrt{3}+1)y-3(2\sqrt{3}+1) = (2-\sqrt{3})x-2(2-\sqrt{3})$$

$$(\sqrt{3}-2)x+(2\sqrt{3}+1)y = -4+2\sqrt{3}+6\sqrt{3}+3$$

$$(\sqrt{3}-2)x+(2\sqrt{3}+1)y = -1+8\sqrt{3}$$

In this case, the equation of the other line is  $(\sqrt{3}-2)x+(2\sqrt{3}+1)y=-1+8\sqrt{3}$ 

Case II: 
$$m_2 = \frac{-(2+\sqrt{3})}{(2\sqrt{3}-1)}$$

 $\frac{-\left(2+\sqrt{3}\right)}{\left(2\sqrt{3}-1\right)}$  The equation of the line passing through point (2, 3) and having a slope of

$$(y-3) = \frac{-(2+\sqrt{3})}{(2\sqrt{3}-1)}(x-2)$$

$$(2\sqrt{3}-1)y-3(2\sqrt{3}-1) = -(2+\sqrt{3})x+2(2+\sqrt{3})$$

$$(2\sqrt{3}-1)y+(2+\sqrt{3})x = 4+2\sqrt{3}+6\sqrt{3}-3$$

$$(2+\sqrt{3})x+(2\sqrt{3}-1)y = 1+8\sqrt{3}$$

In this case, the equation of the other line is  $(2+\sqrt{3})x+(2\sqrt{3}-1)y=1+8\sqrt{3}$ 

Thus, the required equation of the other line is  $(\sqrt{3}-2)x+(2\sqrt{3}+1)y=-1+8\sqrt{3}$  or  $(2+\sqrt{3})x+(2\sqrt{3}-1)y=1+8\sqrt{3}$ 

### Question 12:

Find the equation of the right bisector of the line segment joining the points (3, 4) and (-1, 2).

**Answer** 

The right bisector of a line segment bisects the line segment at 90°.

The end-points of the line segment are given as A (3, 4) and B (-1, 2).

Accordingly, mid-point of AB  $= \left(\frac{3-1}{2}, \frac{4+2}{2}\right) = \left(1,3\right)$ 

Slope of AB 
$$=$$
  $\frac{2-4}{-1-3} = \frac{-2}{-4} = \frac{1}{2}$ 

$$-\frac{1}{\left(\frac{1}{2}\right)} = -2$$

∴Slope of the line perpendicular to AB =

The equation of the line passing through (1, 3) and having a slope of -2 is

$$(y-3) = -2(x-1)$$

$$y - 3 = -2x + 2$$

$$2x + y = 5$$

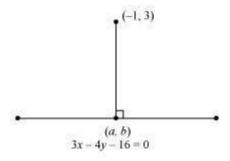
Thus, the required equation of the line is 2x + y = 5.

#### Question 13:

Find the coordinates of the foot of perpendicular from the point (-1, 3) to the line 3x - 4y - 16 = 0.

Answer

Let (a, b) be the coordinates of the foot of the perpendicular from the point (-1, 3) to the line 3x - 4y - 16 = 0.



Slope of the line joining (-1, 3) and (a, b),  $m_1 = \frac{b-3}{a+1}$ 

Slope of the line 3x - 4y - 16 = 0 or  $y = \frac{3}{4}x - 4$ ,  $m_2 = \frac{3}{4}$ 

Since these two lines are perpendicular,  $m_1m_2 = -1$ 

$$\therefore \left(\frac{b-3}{a+1}\right) \times \left(\frac{3}{4}\right) = -1$$

$$\Rightarrow \frac{3b-9}{4a+4} = -1$$

$$\Rightarrow 3b-9 = -4a-4$$

$$\Rightarrow 4a+3b=5 \qquad \dots(1)$$

Point (a, b) lies on line 3x - 4y = 16.

$$3a - 4b = 16 \dots (2)$$

On solving equations (1) and (2), we obtain

$$a = \frac{68}{25}$$
 and  $b = -\frac{49}{25}$ 

Thus, the required coordinates of the foot of the perpendicular are

## Question 14:

The perpendicular from the origin to the line y = mx + c meets it at the point (-1, 2). Find the values of m and c.

Answer

The given equation of line is y = mx + c.

It is given that the perpendicular from the origin meets the given line at (-1, 2).

Therefore, the line joining the points (0, 0) and (-1, 2) is perpendicular to the given line.

∴Slope of the line joining (0, 0) and (-1, 2)  $= \frac{2}{-1} = -2$ The slope of the

The slope of the given line is m.

$$\therefore m \times -2 = -1$$
 [The two lines are perpendicular]

$$\Rightarrow m = \frac{1}{2}$$

Since point (-1, 2) lies on the given line, it satisfies the equation y = mx + c.

$$\therefore 2 = m(-1) + c$$

$$\Rightarrow 2 = \frac{1}{2}(-1) + c$$

$$\Rightarrow c = 2 + \frac{1}{2} = \frac{5}{2}$$

Thus, the respective values of m and c are  $\frac{1}{2}$  and  $\frac{5}{2}$ 

# Question 15:

If p and q are the lengths of perpendiculars from the origin to the lines  $x \cos \theta - y \sin \theta = k \cos 2\theta$  and  $x \sec \theta + y \csc \theta = k$ , respectively, prove that  $p^2 + 4q^2 = k^2$ Answer

The equations of given lines are

$$x \cos \theta - y \sin \theta = k \cos 2\theta \dots (1)$$

$$x \sec \theta + y \csc \theta = k \dots (2)$$

The perpendicular distance (d) of a line Ax + By + C = 0 from a point  $(x_1, y_1)$  is given by

$$d = \frac{|Ax_1 + By_1 + C|}{\sqrt{A^2 + B^2}}$$

On comparing equation (1) to the general equation of line i.e., Ax + By + C = 0, we obtain  $A = \cos\theta$ ,  $B = -\sin\theta$ , and  $C = -k\cos 2\theta$ .

It is given that p is the length of the perpendicular from (0, 0) to line (1).

$$\therefore p = \frac{|A(0) + B(0) + C|}{\sqrt{A^2 + B^2}} = \frac{|C|}{\sqrt{A^2 + B^2}} = \frac{|-k\cos 2\theta|}{\sqrt{\cos^2 \theta + \sin^2 \theta}} = |-k\cos 2\theta| \qquad ...(3)$$

On comparing equation (2) to the general equation of line i.e., Ax + By + C = 0, we obtain  $A = \sec\theta$ ,  $B = \csc\theta$ , and C = -k.

It is given that q is the length of the perpendicular from (0, 0) to line (2).

$$\therefore q = \frac{|A(0) + B(0) + C|}{\sqrt{A^2 + B^2}} = \frac{|C|}{\sqrt{A^2 + B^2}} = \frac{|-k|}{\sqrt{\sec^2 \theta + \csc^2 \theta}} \qquad ...(4)$$

From (3) and (4), we have

$$p^{2} + 4q^{2} = (|-k\cos 2\theta|)^{2} + 4\left(\frac{|-k|}{\sqrt{\sec^{2}\theta + \csc^{2}\theta}}\right)^{2}$$

$$= k^{2}\cos^{2}2\theta + \frac{4k^{2}}{(\sec^{2}\theta + \csc^{2}\theta)}$$

$$= k^{2}\cos^{2}2\theta + \frac{4k^{2}}{\left(\frac{1}{\cos^{2}\theta} + \frac{1}{\sin^{2}\theta}\right)}$$

$$= k^{2}\cos^{2}2\theta + \frac{4k^{2}}{\left(\frac{\sin^{2}\theta + \cos^{2}\theta}{\sin^{2}\theta\cos^{2}\theta}\right)}$$

$$= k^{2}\cos^{2}2\theta + \frac{4k^{2}}{\left(\frac{1}{\sin^{2}\theta\cos^{2}\theta}\right)}$$

$$= k^{2}\cos^{2}2\theta + 4k^{2}\sin^{2}\theta\cos^{2}\theta$$

$$= k^{2}\cos^{2}2\theta + 4k^{2}\sin^{2}\theta\cos^{2}\theta$$

$$= k^{2}\cos^{2}2\theta + k^{2}(2\sin\theta\cos\theta)^{2}$$

$$= k^{2}\cos^{2}2\theta + k^{2}\sin^{2}2\theta$$

$$= k^{2}(\cos^{2}2\theta + \sin^{2}2\theta)$$

$$= k^{2}$$

Hence, we proved that  $p^2 + 4q^2 = k^2$ .

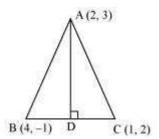
## **Question 16:**

In the triangle ABC with vertices A (2, 3), B (4, -1) and C (1, 2), find the equation and length of altitude from the vertex A.

Answer

Let AD be the altitude of triangle ABC from vertex A.

Accordingly, AD<sub>+</sub>BC



The equation of the line passing through point (2, 3) and having a slope of 1 is

$$(y-3)=1(x-2)$$

$$\Rightarrow x - y + 1 = 0$$

$$\Rightarrow y - x = 1$$

Therefore, equation of the altitude from vertex A = y - x = 1.

Length of AD = Length of the perpendicular from A (2, 3) to BC

The equation of BC is

$$(y+1) = \frac{2+1}{1-4}(x-4)$$

$$\Rightarrow (y+1) = -1(x-4)$$

$$\Rightarrow y+1 = -x+4$$

$$\Rightarrow x+y-3 = 0 \qquad ...(1)$$

The perpendicular distance (d) of a line Ax + By + C = 0 from a point  $(x_1, y_1)$  is given by

$$d = \frac{|Ax_1 + By_1 + C|}{\sqrt{A^2 + B^2}}$$

On comparing equation (1) to the general equation of line Ax + By + C = 0, we obtain A = 1, B = 1, and C = -3.

$$= \frac{\left|1 \times 2 + 1 \times 3 - 3\right|}{\sqrt{1^2 + 1^2}} \text{ units} = \frac{\left|2\right|}{\sqrt{2}} \text{ units} = \frac{2}{\sqrt{2}} \text{ units} = \sqrt{2} \text{ units}$$

$$\therefore \text{Length of AD}$$

Thus, the equation and the length of the altitude from vertex A are y - x = 1 and  $\sqrt{2}$  units respectively.

#### **Question 17:**

If p is the length of perpendicular from the origin to the line whose intercepts on the

$$\frac{1}{p^2} = \frac{1}{a^2} + \frac{1}{b^2}$$

 $\frac{1}{p^2} = \frac{1}{a^2} + \frac{1}{b^2}$  axes are a and b, then show that  $\frac{1}{p^2} = \frac{1}{a^2} + \frac{1}{b^2}$ 

**Answer** 

It is known that the equation of a line whose intercepts on the axes are a and b is

$$\frac{x}{a} + \frac{y}{b} = 1$$
or  $bx + ay = ab$ 
or  $bx + ay - ab = 0$  ...(1)

The perpendicular distance (d) of a line Ax + By + C = 0 from a point  $(x_1, y_1)$  is given by

$$d = \frac{|Ax_1 + By_1 + C|}{\sqrt{A^2 + B^2}}$$

On comparing equation (1) to the general equation of line Ax + By + C = 0, we obtain A= b, B = a, and C = -ab.

Therefore, if p is the length of the perpendicular from point  $(x_1, y_1) = (0, 0)$  to line (1),

$$p = \frac{\left| A(0) + B(0) - ab \right|}{\sqrt{b^2 + a^2}}$$

$$\Rightarrow p = \frac{\left| -ab \right|}{\sqrt{a^2 + b^2}}$$

On squaring both sides, we obtain

$$p^{2} = \frac{(-ab)^{2}}{a^{2} + b^{2}}$$

$$\Rightarrow p^{2} (a^{2} + b^{2}) = a^{2}b^{2}$$

$$\Rightarrow \frac{a^{2} + b^{2}}{a^{2}b^{2}} = \frac{1}{p^{2}}$$

$$\Rightarrow \frac{1}{p^{2}} = \frac{1}{a^{2}} + \frac{1}{b^{2}}$$