

CLASS X: MATHS
Chapter 7: Coordinate Geometry

Questions and Solutions | Exercise 7.1 - NCERT Books

Q1. Find the distance between the following pairs of points :

- (a) (2,3), (4, 1)
- (b) (-5, 7), (-1,3)
- (c) (a, b), (- a, - b)

Sol.(a) The given points are : A (2, 3), B (4, 1).

$$\text{Required distance} = AB = BA = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$AB = \sqrt{(4 - 2)^2 + (1 - 3)^2} = \sqrt{2^2 + (-2)^2}$$

$$= \sqrt{4 + 4} = \sqrt{8} = 2\sqrt{2} \text{ units}$$

(b) Here $x_1 = -5$, $y_1 = 7$ and $x_2 = -1$, $y_2 = 3$

\therefore The required distance

$$= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \sqrt{[-1 - (-5)]^2 + (3 - 7)^2}$$

$$= \sqrt{(-1 + 5)^2 + (-4)^2}$$

$$= \sqrt{16 + 16} = \sqrt{32} = \sqrt{2 \times 16}$$

$$= 4\sqrt{2} \text{ units}$$

(c) Here $x_1 = a$, $y_1 = b$ and $x_2 = -a$, $y_2 = -b$

\therefore The required distance

$$= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \sqrt{(-a - a)^2 + (-b - b)^2}$$

$$= \sqrt{(-2a)^2 + (-2b)^2} = \sqrt{4a^2 + 4b^2}$$

$$= \sqrt{4(a^2 + b^2)} = 2\sqrt{a^2 + b^2} \text{ units}$$

Q2. Find the distance between the points (0,0) and (36,15). Can you now find the distance between the tow towns A and B discussed in section 7.2.

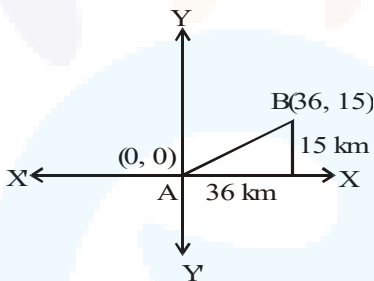
Sol. Part-I

Let the points be A(0, 0) and B(36, 15)

$$\begin{aligned} \therefore AB &= \sqrt{(36-0)^2 + (15-0)^2} \\ &= \sqrt{(36)^2 + (15)^2} = \sqrt{1296 + 225} \\ &= \sqrt{1521} = \sqrt{39^2} = 39 \end{aligned}$$

Part-II

We have A(0, 0) and B(36, 15) as the positions of two towns



Here $x_1 = 0$, $x_2 = 36$ and $y_1 = 0$, $y_2 = 15$

$$\therefore AB = \sqrt{(36-0)^2 + (15-0)^2} = 39 \text{ km}$$

Q3. Determine if the points (1,5), (2,3) and (-2, -11) are collinear.

Sol. The given points are :

A(1, 5), B(2, 3) and C(-2, -11).

Let us calculate the distance : AB, BC and CA by using distance formula.

$$\begin{aligned} AB &= \sqrt{(2-1)^2 + (3-5)^2} = \sqrt{(1)^2 + (-2)^2} \\ &= \sqrt{1+4} = \sqrt{5} \text{ units} \end{aligned}$$

$$\begin{aligned} BC &= \sqrt{(-2-2)^2 + (-11-3)^2} = \sqrt{(-4)^2 + (-14)^2} \\ &= \sqrt{16+196} = \sqrt{212} = 2\sqrt{53} \text{ units} \end{aligned}$$

$$\begin{aligned} CA &= \sqrt{(-2-1)^2 + (-11-5)^2} \\ &= \sqrt{(-3)^2 + (-16)^2} = \sqrt{9+256} = \sqrt{265} \\ &= \sqrt{5} \times \sqrt{53} \text{ units} \end{aligned}$$

From the above we see that : $AB + BC \neq CA$

Hence the above stated points $A(1, 5)$, $B(2, 3)$ and $C(-2, -11)$ are not collinear.

Q4. Check whether $(5, -2)$, $(6, 4)$ and $(7, -2)$ are the vertices of an isosceles triangle.

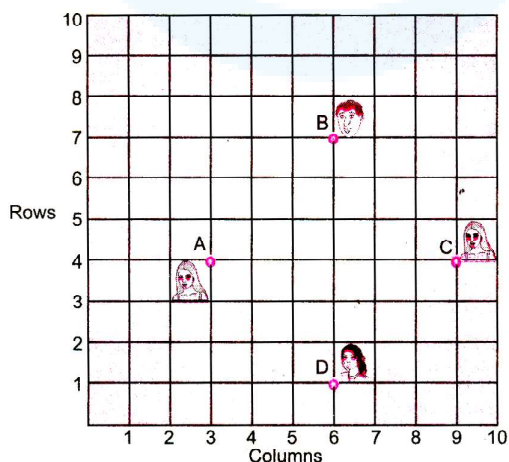
Sol. Let the points be $A(5, -2)$, $B(6, 4)$ and $C(7, -2)$.

$$\begin{aligned} \therefore AB &= \sqrt{(6-5)^2 + [4-(-2)]^2} \\ &= \sqrt{(1)^2 + (6)^2} = \sqrt{1+36} = \sqrt{37} \\ BC &= \sqrt{(7-6)^2 + (-2-4)^2} \\ &= \sqrt{(1)^2 + (-6)^2} = \sqrt{1+36} = \sqrt{37} \\ AC &= \sqrt{(7-5)^2 + (-2-(-2))^2} \\ &= \sqrt{(2)^2 + (0)^2} = \sqrt{4+0} = 2 \end{aligned}$$

We have $AB = BC \neq AC$.

$\therefore \triangle ABC$ is an isosceles triangle.

Q5. In a classroom, 4 friends are seated at the points A, B, C and D as shown in fig. Champa and Chameli walk into the class and after observing for a few minutes Champa asks Chameli, "Don't you think ABCD is a rectangle?" Chameli disagrees. Using distance formula, find which of them is correct.



Sol. Let the number of horizontal columns represent the x-coordinates whereas the vertical rows represent the y-coordinates.

∴ The points are : A(3, 4), B(6, 7), C(9, 4) and D(6, 1)

$$\begin{aligned}\therefore AB &= \sqrt{(6-3)^2 + (7-4)^2} \\ &= \sqrt{(3)^2 + (3)^2} = \sqrt{9+9} = \sqrt{18} = 3\sqrt{2}\end{aligned}$$

$$\begin{aligned}BC &= \sqrt{(9-6)^2 + (4-7)^2} \\ &= \sqrt{3^2 + (-3)^2} = \sqrt{9+9} = \sqrt{18} = 3\sqrt{2}\end{aligned}$$

$$\begin{aligned}CD &= \sqrt{(6-9)^2 + (1-4)^2} \\ &= \sqrt{(-3)^2 + (-3)^2} = \sqrt{9+9} = \sqrt{18} = 3\sqrt{2}\end{aligned}$$

$$\begin{aligned}AD &= \sqrt{(6-3)^2 + (1-4)^2} \\ &= \sqrt{(3)^2 + (-3)^2} = \sqrt{9+9} = \sqrt{18} = 3\sqrt{2}\end{aligned}$$

Since, $AB = BC = CD = AD$ i.e., All the four sides are equal

$$\begin{aligned}\text{Also } AC &= \sqrt{(9-3)^2 + (4-4)^2} \\ &= \sqrt{(+6)^2 + (0)^2} = 6 \text{ and}\end{aligned}$$

$$BD = \sqrt{(6-6)^2 + (1-7)^2} = \sqrt{(0)^2 + (-6)^2} = 6$$

i.e., $BD = AC$

⇒ Both the diagonals are also equal.

∴ ABCD is a square.

Thus, Chameli is correct as ABCD is not a rectangle.

Q6. Name the quadrilateral formed, if any, by the following points, and give reasons for your answer.

(i) (-1, -2), (1, 0), (-1, 2), (-3, 0)

(ii) (-3, 5), (3, 1), (0, 3), (-1, -4)

(iii) (4, 5), (7, 6), (4, 3), (1, 2)

Sol. (i) A(-1, -2), B(1, 0), C(-1, 2), D(-3, 0)

Determine distances : AB, BC, CD, DA, AC and BD.

$$AB = \sqrt{(1+1)^2 + (0+2)^2} = \sqrt{4+4} = \sqrt{8} = 2\sqrt{2}$$

$$BC = \sqrt{(-1-1)^2 + (2-0)^2} = \sqrt{4+4} = \sqrt{8} = 2\sqrt{2}$$

$$CD = \sqrt{(-3+1)^2 + (0-2)^2} = \sqrt{4+4} = \sqrt{8} = 2\sqrt{2}$$

$$DA = \sqrt{(-1+3)^2 + (-2-0)^2} = \sqrt{4+4} = \sqrt{8} = 2\sqrt{2}$$

$$AB = BC = CD = DA$$

The sides of the quadrilateral are equal(1)

$$AC = \sqrt{(-1+1)^2 + (2+2)^2} = \sqrt{0+16} = 4$$

$$BD = \sqrt{(-3-1)^2 + (0-0)^2} = \sqrt{16+0} = 4$$

$$\text{Diagonal AC} = \text{Diagonal BD}.....(2)$$

From (1) and (2) we conclude that ABCD is a square.

(ii) Let the points be A(-3, 5), B(3, 1), C(0, 3) and D(-1, -4).

$$\therefore AB = \sqrt{[3 - (-3)]^2 + (1 - 5)^2}$$

$$= \sqrt{6^2 + (-4)^2} = \sqrt{36 + 16}$$

$$= \sqrt{52} = 2\sqrt{13}$$

$$BC = \sqrt{(0 - 3)^2 + (3 - 1)^2} = \sqrt{9 + 4} = \sqrt{13}$$

$$CD = \sqrt{(-1 - 0)^2 + (-4 - 3)^2} = \sqrt{(-1)^2 + (-7)^2}$$

$$= \sqrt{1 + 49} = \sqrt{50}$$

$$DA = \sqrt{[-3 - (-1)]^2 + [5 - (-4)]^2}$$

$$= \sqrt{(-2)^2 + (9)^2}$$

$$= \sqrt{4 + 81} = \sqrt{85}$$

$$AC = \sqrt{[0 - (-3)]^2 + (3 - 5)^2} = \sqrt{(3)^2 + (-2)^2}$$

$$= \sqrt{9 + 4} = \sqrt{13}$$

$$BD = \sqrt{(-1 - 3)^2 + (-4 - 1)^2} = \sqrt{(-4)^2 + (-5)^2}$$

$$= \sqrt{16 + 25} = \sqrt{41}$$

We see that $\sqrt{13} + \sqrt{13} = 2\sqrt{13}$

i.e., $AC + BC = AB$

\Rightarrow A, B and C are collinear. Thus, ABCD is not a quadrilateral.

(iii) Let the points be A(4, 5), B(7, 6), C(4, 3) and D(1, 2).

$$\therefore AB = \sqrt{(7-4)^2 + (6-5)^2} = \sqrt{3^2 + 1^2} = \sqrt{10}$$

$$\begin{aligned} BC &= \sqrt{(4-7)^2 + (3-6)^2} \\ &= \sqrt{(-3)^2 + (-3)^2} = \sqrt{18} \end{aligned}$$

$$\begin{aligned} CD &= \sqrt{(1-4)^2 + (2-3)^2} \\ &= \sqrt{(-3)^2 + (-1)^2} = \sqrt{10} \end{aligned}$$

$$DA = \sqrt{(1-4)^2 + (2-5)^2} = \sqrt{9+9} = \sqrt{18}$$

$$AC = \sqrt{(4-4)^2 + (3-5)^2} = \sqrt{0+(-2)^2} = 2$$

$$BD = \sqrt{(1-7)^2 + (2-6)^2} = \sqrt{36+16} = \sqrt{52}$$

Since, $AB = CD$, $BC = DA$ [opposite sides of the quadrilateral are equal]

And $AC \neq BD \Rightarrow$ Diagonals are unequal.

\therefore ABCD is a parallelogram.

Q7. Find the point on the x-axis which is equidistant from (2, -5) and (-2, 9).

Sol. We know that any point on x-axis has its ordinate = 0

Let the required point be P(x, 0).

Let the given points be A(2, -5) and B(-2, 9)

$$\begin{aligned} \therefore AP &= \sqrt{(x-2)^2 + 5^2} = \sqrt{x^2 - 4x + 4 + 25} \\ &= \sqrt{x^2 - 4x + 29} \end{aligned}$$

$$\begin{aligned} BP &= \sqrt{[x-(-2)]^2 + (-9)^2} = \sqrt{(x+2)^2 + (-9)^2} \\ &= \sqrt{x^2 + 4x + 4 + 81} = \sqrt{x^2 + 4x + 85} \end{aligned}$$

Since, A and B are equidistant from P,

$$\therefore AP = BP$$

$$\Rightarrow \sqrt{x^2 - 4x + 29} = \sqrt{x^2 + 4x + 85}$$

$$\Rightarrow x^2 - 4x + 29 = x^2 + 4x + 85$$

$$\Rightarrow x^2 - 4x - x^2 - 4x = 85 - 29$$

$$\Rightarrow -8x = 56 \Rightarrow x = \frac{56}{-8} = -7$$

\therefore The required point is $(-7, 0)$

Q8. Find the values of y for which the distance between the points $P(2, -3)$ and $Q(10, y)$ is 10 units.

Sol. Distance between $P(2, -3)$ and $Q(10, y) = 10$ units

$$\Rightarrow \sqrt{(10 - 2)^2 + (y + 3)^2} = 10$$

$$\Rightarrow 64 + (y + 3)^2 = 100$$

$$\Rightarrow (y + 3)^2 = 36$$

$$\Rightarrow y^2 + 6y + 9 = 36$$

$$y^2 + 6y - 27 = 0$$

$$\Rightarrow y^2 + 9y - 3y - 27 = 0$$

$$\Rightarrow y(y + 9) - 3(y + 9) = 0$$

$$\Rightarrow (y + 9)(y - 3) = 0$$

$$\Rightarrow y + 9 = 0 \text{ or } y - 3 = 0$$

$$\Rightarrow y = -9 \text{ or } 3$$

Hence, there can be two values of y which are -9 and 3 .

Q9. If $Q(0, 1)$ is equidistant from $P(5, -3)$ and $R(x, 6)$, find the values of x . Also find the distances QR and PR .

Sol. Here, $QP = \sqrt{(5 - 0)^2 + [(-3) - 1]^2} = \sqrt{5^2 + (-4)^2}$

$$= \sqrt{25 + 16} = \sqrt{41}$$

$$QR = \sqrt{(x - 0)^2 + (6 - 1)^2} = \sqrt{x^2 + 5^2} = \sqrt{x^2 + 25}$$

$$\therefore QP = QR$$

$$\therefore \sqrt{41} = \sqrt{x^2 + 25}$$

Squaring both sides, we have $x^2 + 25 = 41$

$$\Rightarrow x^2 + 25 - 41 = 0$$

$$\Rightarrow x^2 - 16 = 0 \Rightarrow x = \pm \sqrt{16} = \pm 4$$

Thus, the point R is (4, 6) or (-4, 6)

Now,

$$QR = \sqrt{[(\pm 4) - (0)]^2 + (6 - 1)^2} = \sqrt{16 + 25} = \sqrt{41}$$

$$\text{and } PR = \sqrt{(\pm 4 - 5)^2 + (6 + 3)^2}$$

$$\Rightarrow PR = \sqrt{(-4 - 5)^2 + (6 + 3)^2}$$

$$\text{or } \sqrt{(4 - 5)^2 + (6 + 3)^2}$$

$$\Rightarrow PR = \sqrt{(-9)^2 + 9^2} \text{ or } \sqrt{1 + 81}$$

$$\Rightarrow PR = \sqrt{2 \times 9^2} \text{ or } \sqrt{82}$$

$$\Rightarrow PR = 9\sqrt{2} \text{ or } \sqrt{82}$$

Q10. Find a relation between x and y such that the point (x,y) is equidistant from the point (3, 6) and (-3, 4).

Sol. A(3,6) and B(-3, 4) are the given points. Point P (x, y) is equidistant from the points A and B.

$$\Rightarrow PA = PB$$

$$\Rightarrow \sqrt{(x-3)^2 + (y-6)^2} = \sqrt{(x+3)^2 + (y-4)^2}$$

$$\Rightarrow (x-3)^2 + (y-6)^2 = (x+3)^2 + (y-4)^2$$

$$\Rightarrow (x^2 - 6x + 9) + (y^2 - 12y + 36)$$

$$= (x^2 + 6x + 9) + (y^2 - 8y + 16)$$

$$\Rightarrow -6x - 12y + 45 = 6x - 8y + 25$$

$$\Rightarrow 12x + 4y - 20 = 0 \Rightarrow 3x + y - 5 = 0$$

 Questions and Solutions | Exercise 7.2 - NCERT Books

Q1. Find the co-ordinates of the point which divides the line joining of $(-1, 7)$ and $(4, -3)$ in the ratio $2 : 3$.

Sol. Let the required point be $P(x, y)$.

Here the end points are $(-1, 7)$ and $(4, -3)$

$$\therefore \text{Ratio} = 2 : 3 = m_1 : m_2$$

$$\therefore x = \frac{m_1 x_2 + m_2 x_1}{m_1 + m_2} = \frac{(2 \times 4) + 3(-1)}{2 + 3}$$

$$= \frac{8 - 3}{5} = \frac{5}{5} = 1$$

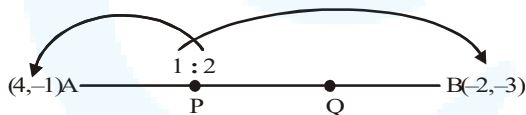
$$\text{And } y = \frac{m_1 y_2 + m_2 y_1}{m_1 + m_2}$$

$$= \frac{2 \times (-3) + 3 \times 7}{2 + 3} = \frac{-6 + 21}{5} = \frac{15}{5} = 3$$

Thus, the required point is $(1, 3)$.

Q2. Find the coordinates of the points of trisection of the line segment joining $(4, -1)$ and $(-2, -3)$.

Sol.



Points P and Q trisect the line segment joining the points $A(4, -1)$ and $B(-2, -3)$, i.e., $AP = PQ = QB$.

Here, P divides AB in the ratio $1 : 2$ and Q divides AB in the ratio $2 : 1$.

$$\text{x-coordinate of P} = \frac{1 \times (-2) + 2 \times (4)}{1 + 2} = \frac{6}{3} = 2 ;$$

$$\text{y-coordinate of P} = \frac{1 \times (-3) + 2 \times (-1)}{1 + 2} = \frac{-5}{3}$$

Thus, the coordinates of P are $\left(2, -\frac{5}{3}\right)$.

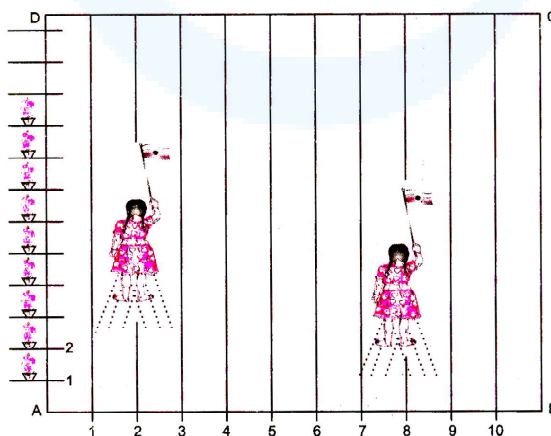
Now, x coordinate of Q = $\frac{2 \times (-2) + 1 \times (4)}{2 + 1} = 0$;

y-coordinate of Q = $\frac{2 \times (-3) + 1 \times (-1)}{2 + 1} = -\frac{7}{3}$

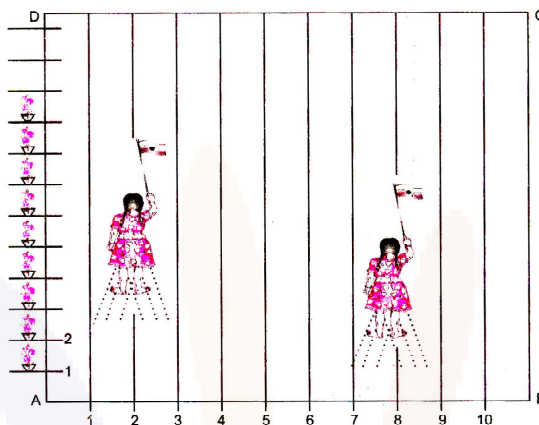
Thus, the coordinates of Q are $\left(0, -\frac{7}{3}\right)$.

Hence, the points of trisection are P $\left(2, -\frac{5}{3}\right)$ and Q $\left(0, -\frac{7}{3}\right)$.

- Q3.** To conduct Sports Day activities, in your rectangular shaped school ground ABCD, lines have been drawn with chalk powder at a distance of 1 m each. 100 flower pots have been placed at a distance of 1 m from each other along AD, as shown in fig. Niharika runs $\frac{1}{4}$ th the distance AD on the 2nd line and posts a green flag. Preet runs $\frac{1}{5}$ th the distance AD on the eighth line and posts a red flag. What is the distance between both the flags? If Rashmi has to post a blue flag exactly halfway between the line segment joining the two flags, where should she post her flag?



Sol. Let us consider 'A' as origin, then



AB is the x-axis.

AD is the y-axis.

Now, the position of green flag-post is

$$\left(2, \frac{100}{4}\right) \text{ or } (2, 25)$$

And, the position of red flag-post is

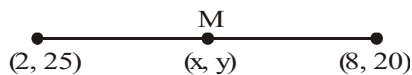
$$\left(8, \frac{100}{5}\right) \text{ or } (8, 20)$$

⇒ Distance between both the flags

$$= \sqrt{(8-2)^2 + (20-25)^2}$$

$$= \sqrt{6^2 + (-5)^2} = \sqrt{36+25} = \sqrt{61}$$

Let the mid-point of the line segment joining the two flags be M(x, y).



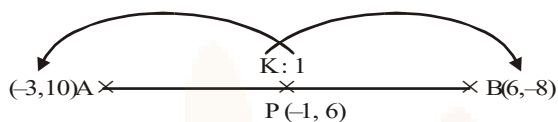
$$\therefore x = \frac{2+8}{2} \text{ and } y = \frac{25+20}{2}$$

or $x = 5$ and $y = 22.5$

Thus, the blue flag is on the 5th line at a distance 22.5 m above AB.

Q4. Find the ratio in which the line segment joining the points $(-3, 10)$ and $(6, -8)$ is divided by $(-1, 6)$.

Sol. Let the required ratio be $K : 1$



Comparing x-coordinate

$$\frac{k \times (6) + 1 \times (-3)}{k+1} = -1$$

$$\Rightarrow 6k - 3 = -k - 1$$

$$\Rightarrow 7k = 2$$

$$\Rightarrow k = \frac{2}{7}$$

Comparing y-coordinate

$$\frac{k \times (-8) + 1 \times (10)}{k+1} = 6$$

$$\Rightarrow -8k + 10 = 6k + 6$$

$$\Rightarrow -8K - 6K = 6 - 10$$

$$\Rightarrow -14K = -4$$

$$\Rightarrow k = \frac{2}{7}$$

Q5. Find the ratio in which the line segment joining $A(1, -5)$ and $B(-4, 5)$ is divided by the x-axis. Also find the coordinates of the point of division.

Sol. The given points are : $A(1, -5)$ and $B(-4, 5)$. Let the required ratio = $k : 1$ and the required point be $P(x, y)$

Part-I : To find the ratio

Since, the point P lies on x-axis,

\therefore Its y-coordinate is 0.

$$x = \frac{m_1 x_2 + m_2 x_1}{m_1 + m_2} \text{ and } 0 = \frac{m_1 y_2 + m_2 y_1}{m_1 + m_2}$$

$$\Rightarrow x = \frac{-4k + 1}{k + 1} \text{ and } 0 = \frac{5k - 5}{k + 1}$$

$$\Rightarrow x(k + 1) = -4k + 1$$

$$\text{and } 5k - 5 = 0 \Rightarrow k = 1$$

$$\Rightarrow x(k + 1) = -4k + 1$$

$$\Rightarrow x(1 + 1) = -4 + 1 \quad [\because k = 1]$$

$$\Rightarrow 2x = -3$$

$$\Rightarrow x = -\frac{3}{2}$$

\therefore The required ratio $k : 1 = 1 : 1$

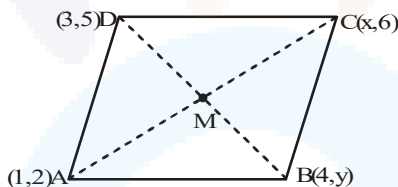
$$\text{Coordinates of P are } (x, 0) = \left(\frac{-3}{2}, 0\right)$$

Q6. If $(1, 2)$, $(4, y)$, $(x, 6)$ and $(3, 5)$ are the vertices of a parallelogram taken in order, find x and y .

Sol. Mid-point of the diagonal AC has x-coordinate

$$= \frac{x+1}{2} \text{ and y-coordinate} = \frac{6+2}{2} = 4$$

i.e., $\left(\frac{x+1}{2}, 4\right)$ is the mid-point of AC.



Similarly, mid-point of the diagonal BD is

$$\left(\frac{4+3}{2}, \frac{y+5}{2}\right), \text{ i.e., } \left(\frac{7}{2}, \frac{y+5}{2}\right)$$

We know that the two diagonals AC and BD bisect each other at M. Therefore,

$$\left(\frac{x+1}{2}, 4\right) \text{ and } \left(\frac{7}{2}, \frac{y+5}{2}\right). \text{ Coincide}$$

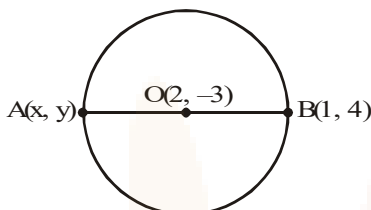
$$\Rightarrow \frac{x+1}{2} = \frac{7}{2} \text{ and } \frac{y+5}{2} = 4$$

$$\Rightarrow x = 6 \text{ and } y = 3$$

Q7. Find the coordinates of a point A, where AB is the diameter of a circle whose centre is $(2, -3)$ and B is $(1, 4)$.

Sol. Here, centre of the circle is $O(2, -3)$

Let the end points of the diameter be $A(x, y)$ and $B(1, 4)$



The centre of a circle bisects the diameter.

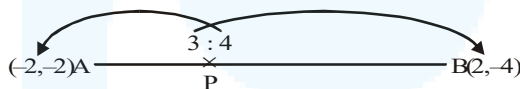
$$\therefore 2 = \frac{x+1}{2} \Rightarrow x + 1 = 4 \text{ or } x = 3$$

$$\text{And } -3 = \frac{y+4}{2} \Rightarrow y + 4 = -6 \text{ or } y = -10$$

Here, the coordinates of A are $(3, -10)$

Q8. If A and B are $(-2, -2)$ and $(2, -4)$, respectively, find the coordinates of P such that $AP = \frac{3}{7} AB$ and P lies on the line segment AB.

Sol.



$$AP = \frac{3}{7} AB,$$

$$BP = AB - AP = AB - \frac{3}{7} AB = \frac{4}{7} AB$$

$$\frac{AP}{BP} = \frac{\frac{3}{7} AB}{\frac{4}{7} AB} = \frac{3}{4}$$

Thus, P divides AB in the ratio 3 : 4.

$$\text{x-coordinate of P} = \frac{3 \times (2) + 4 \times (-2)}{3 + 4} = -\frac{2}{7}$$

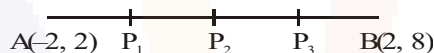
$$y\text{-coordinate of } P = \frac{3 \times (-4) + 4 \times (-2)}{3 + 4} = -\frac{20}{7}$$

Hence, the coordinates of P are $\left(-\frac{2}{7}, -\frac{20}{7}\right)$.

Q9. Find the coordinates of the points which divide the line segment joining A (-2, 2) and B (2, 8) into four equal parts.

Sol. Here, the given points are A(-2, 2) and B(2, 8)

Let P_1 , P_2 and P_3 divide AB in four equal parts.



$$\therefore AP_1 = P_1P_2 = P_2P_3 = P_3B$$

Obviously, P_2 is the mid-point of AB

\therefore Coordinates of P_2 are

$$\left(\frac{-2+2}{2}, \frac{2+8}{2}\right) \text{ or } (0, 5)$$

Again, P_1 is the mid-point of AP_2 .

\therefore Coordinates of P_1 are

$$\left(\frac{-2+0}{2}, \frac{2+5}{2}\right) \text{ or } \left(-1, \frac{7}{2}\right)$$

Also P_3 is the mid-point of P_2B .

\therefore Coordinates of P_3 are

$$\left(\frac{0+2}{2}, \frac{5+8}{2}\right) \text{ or } \left(1, \frac{13}{2}\right)$$

Thus, the coordinates of P_1 , P_2 and P_3 are $\left(-1, \frac{7}{2}\right)$, $(0, 5)$ and $\left(1, \frac{13}{2}\right)$ respectively.

Q10. Find the area of a rhombus if its vertices are (3, 0), (4, 5), (-1, 4) and (-2, -1) taken in order.

Sol. Diagonals AC and BD bisect each other at right angle to each other at O.

$$\begin{aligned} AC &= \sqrt{(-1-3)^2 + (4-0)^2} \\ &= \sqrt{16+16} = \sqrt{32} = 4\sqrt{2} \end{aligned}$$

$$BD = \sqrt{(4+2)^2 + (5+1)^2} = \sqrt{36+36} = 6\sqrt{2}$$

$$\text{Then } OA = \frac{1}{2}AC = \frac{1}{2} \times 4\sqrt{2} = 2\sqrt{2}$$

$$OB = \frac{1}{2}BD = \frac{1}{2} \times 6\sqrt{2} = 3\sqrt{2}$$

$$\text{Area of } \triangle AOB = \frac{1}{2} (OA) \times (OB) = \frac{1}{2} \times 2\sqrt{2} \times 3\sqrt{2} = 6 \text{ sq. units}$$

Hence, the area of the rhombus ABCD
= $4 \times$ area of $\triangle AOB = 4 \times 6 = 24$ sq. units.