

Physics Mega Revision **#6**



- ▶ Rotation Motion ✓
- ▶ Gravitation ✓
- ▶ SHM ✓
- ▶ Wave on String ✓
- ▶ Sound Wave ✓

Superfast Revision



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Complete Physics Mega Revision Timetable

15 Feb

Electrostatics

Current electricity

Capacitor

 **Surprise Gift** 

16 Feb

Calorimetry

Elasticity

Thermal Expansion

Heat Transfer

KTG

Thermodynamics

Fluid Mechanics

17 Feb

Magnetic effect of current

Magnetism and matter

Emi

AC

18 Feb

UD

Vector

Kinematics 1D

Kinematics 2D

NLM

Friction

Circular motion

Work power energy

COM

19 Feb

Ray optics

Optical Instruments

Wave optics

EM Waves

Errors in measurement

20 Feb

Rotation motion

Gravitation

SHM

Wave on string

Sound wave

21 Feb

Atomic structure

Dual nature of radiation

X-rays

Nuclear physics

Radioactivity

Semi conductor

Communication system



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N.K. Gupta Sir eSaral Math Faculty & Master Planner



- IIT Kanpur, Mechanical
- Ex Vice President & Academic Head, Allen, Kota
- Mentored many of Rank 1 & Top 100 Students
- 30+ years of Teaching Experience
- Mentored over 3,00,000 Students





Saransh Gupta Sir eSaral Physics HoD

- IIT Bombay, CS
- AIR-41 IIT-JEE
- Air-71 AIEEE (JEE Main)
- AIR-4 NSO
- 1% In Top INPHO
- 8+ Years of Teaching Experience
- Mentored Lakhs of Students





Prateek Gupta Sir eSara Chemistry Faculty



- IIT Bombay, Metallurgy
- **Online Creativity & Visualization Expert**
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Course Details

Lectures



Practice



Tests

Sheets

Prev. Yr.

Topic-Wise

Review

Study Plan

Doubt Solving

Mentorship

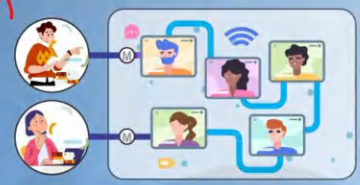


3 Layered Personalised Mentorship

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PERSONAL ACADEMIC MENTOR



PROGRESS MENTOR FOR TRACKING PROGRESS



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Mentorship Session
For eSaralites
15/10/20
08:00 PM
SARANSH SIR, Physics-HoD
AIR-41, IIT Bombay, CS

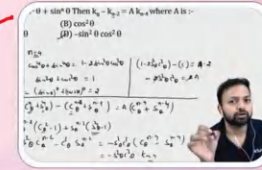


4 Layered DOUBT SOLVING

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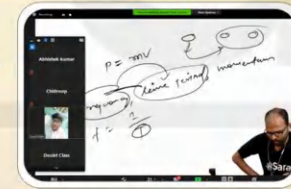
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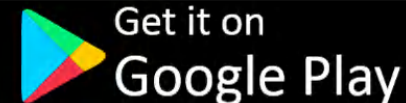
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Rotation Motion

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Rotation Motion

Kinematics of Pure rotation motion

$$S = R\theta$$

$$|v| = R\omega$$

If $\alpha = \text{constant}$

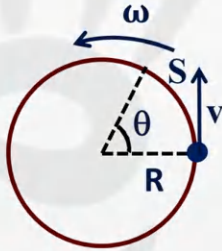
$$\omega_f = \omega_i + \alpha t$$

$$\theta = \omega_0 t + \frac{1}{2} \alpha t^2$$

$$\omega_f^2 = \omega_i^2 + 2\alpha\theta$$

$$\theta = \left(\frac{\omega_i + \omega_f}{2} \right) t$$

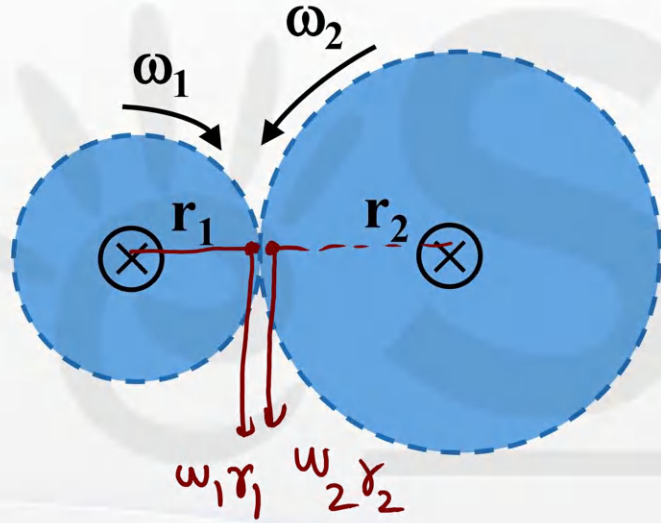
$$\theta = \omega_f t - \frac{1}{2} \alpha t^2$$



Rigid Body

Body in which distance between its constituent particles do not change with time is called rigid body.

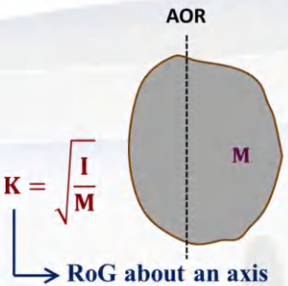
No slipping



$\omega_1 r_1 = \omega_2 r_2$ for no slipping between disks

$$I = \int r^2 dm$$

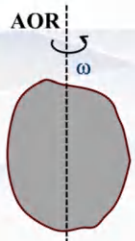

Radius of Gyration



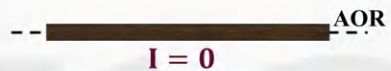
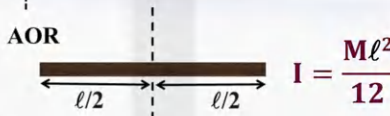
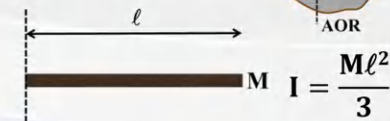
$$K = \sqrt{\frac{I}{M}}$$

RoG about an axis

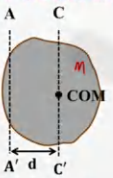
$$I = MK^2$$



$$KE_{sys} = \frac{1}{2} I \omega^2$$



Parallel - axis theorem:

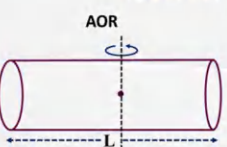


Among the given parallel axis MOI will be minimum about the axis passing through COM.

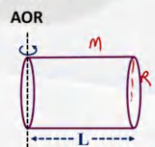
MOI about the parallel axis having same distance from COM is equal.

$$I_{AA'} = I_{CC'} + Md^2$$

Hollow Cylinder



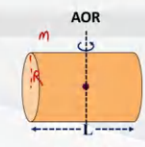
$$I = \frac{MR^2}{2} + \frac{ML^2}{12}$$



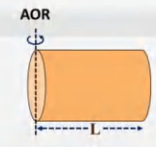
$$I = \frac{MR^2}{2} + \frac{ML^2}{3}$$

TRICK

Solid Cylinder

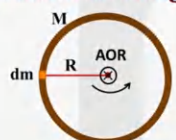


$$I = \frac{MR^2}{4} + \frac{ML^2}{12}$$



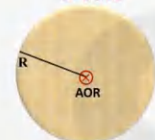
$$I = \frac{MR^2}{4} + \frac{ML^2}{3}$$

Uniform Ring



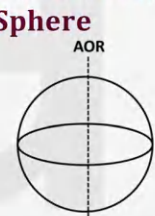
$$I = MR^2$$

Disk



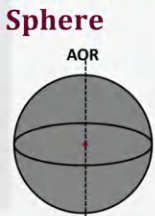
$$I = \frac{MR^2}{2}$$

Uniform Hollow Sphere



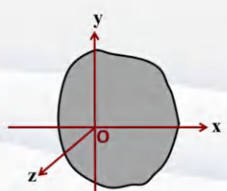
$$I = \frac{2}{3} MR^2$$

Uniform Solid Sphere

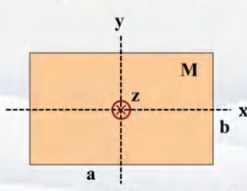


$$I = \frac{2}{5} MR^2$$

Perpendicular axis theorem:



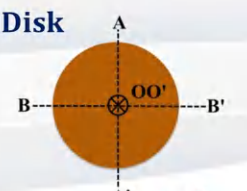
$$I_z = I_x + I_y$$



$$I_z = \frac{Mb^2}{12} + \frac{Ma^2}{12}$$



$$I_{AA'} = \frac{MR^2}{2}$$



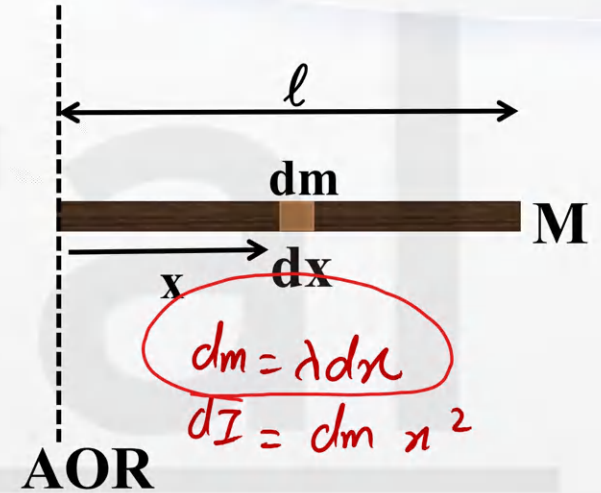
$$I_{AA'} = \frac{MR^2}{4}$$

Q) $\lambda = \lambda_0 \left(1 + \frac{x}{L}\right)$. Find MOI about an AOR at end perpendicular to rod.

Sol. $\int dI = \int x^2 dm$

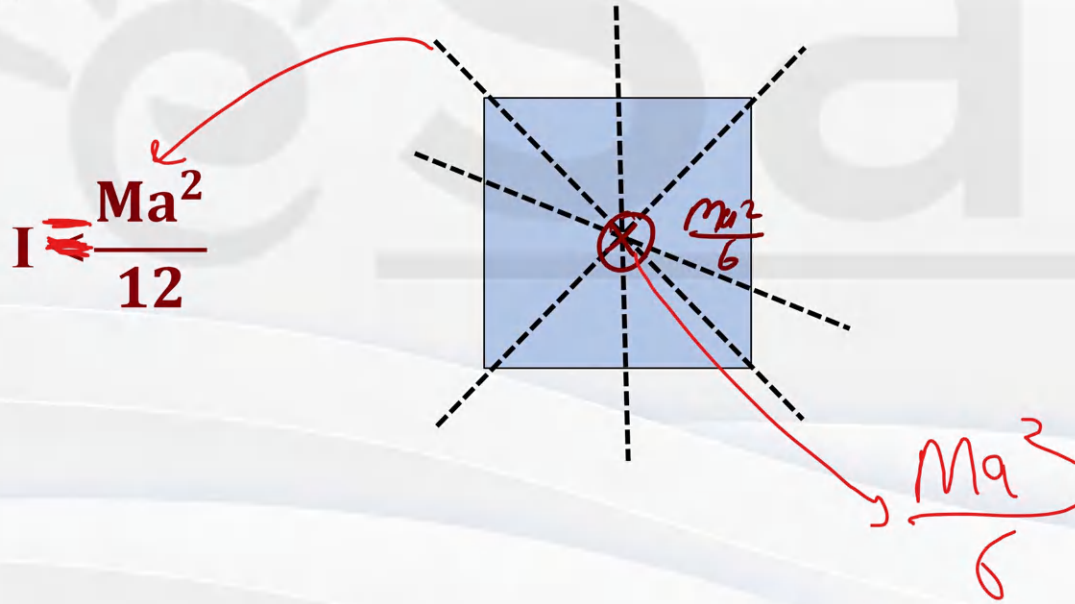
$$I = \int_0^L x^2 \lambda dx \Rightarrow \int_0^L x^2 \lambda_0 \left(1 + \frac{x}{L}\right) dx$$

$$= \lambda_0 \left[\int_0^L x^2 dx + \int_0^L \frac{x^3}{L} dx \right] = \left[\frac{L^3}{3} + \frac{L^3}{4} \right] = \lambda_0 \frac{7L^3}{12}$$



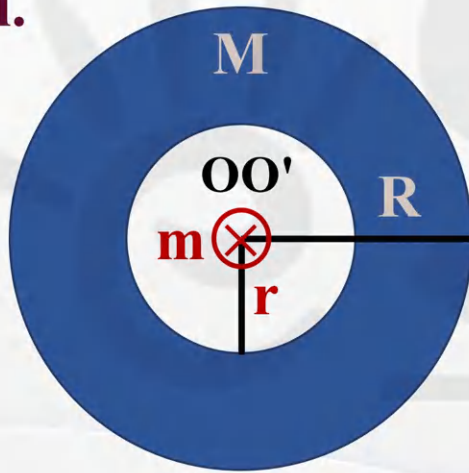
Key Point

In uniform square plate, I about each axis through centre in plane of plate is given by



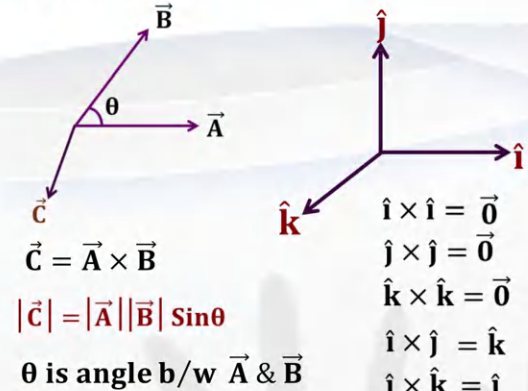
Q) A disk of mass m and radius r is cut out from a disk of mass M and radius R . Find $I_{OO'}$.

Sol.



$$I = I_{BD} - I_{CD} = \frac{MR^2}{2} - \frac{mr^2}{2}$$

Cross Product



Properties

$$\vec{A} \times \vec{B} \neq \vec{B} \times \vec{A}$$

$$\vec{A} \times \vec{B} = -(\vec{B} \times \vec{A})$$

$$\vec{A} \times \vec{A} = \vec{0}$$

$$\hat{i} \times \hat{i} = \vec{0}$$

$$\hat{j} \times \hat{j} = \vec{0}$$

$$\hat{k} \times \hat{k} = \vec{0}$$

$$\hat{i} \times \hat{j} = \hat{k}$$

$$\hat{j} \times \hat{k} = \hat{i}$$

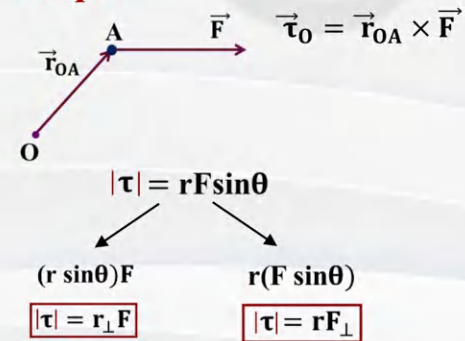
$$\hat{k} \times \hat{i} = \hat{j}$$

$$\hat{j} \times \hat{i} = -\hat{k}$$

$$\hat{k} \times \hat{j} = -\hat{i}$$

$$\hat{i} \times \hat{k} = -\hat{j}$$

Torque



Step To Follow In Pure Rotation

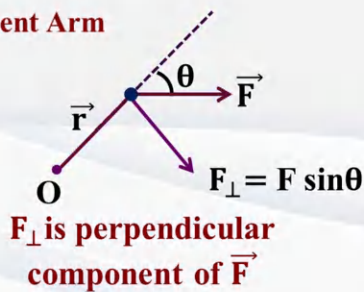
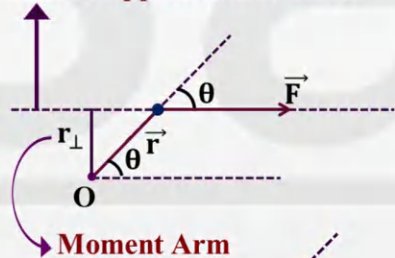
Step-1 : Identify AOR

Step-2 : Take torque of all forces acting on the system.

Step-3 : Apply $\tau_{net} = I\alpha$ about the AOR.

To calculate work & torque of gravitational force, whole mass of body can be assumed to be concentrated at its Center of Gravity.

Line of application of force



Condition of Equilibrium

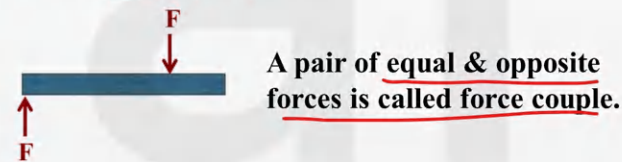
Translation Equilibrium

Rotational Equilibrium

$$1) \sum \vec{F} = 0 \begin{cases} \sum F_x = 0 \\ \sum F_y = 0 \\ \sum F_z = 0 \end{cases} \quad 2) \sum \vec{\tau} = 0$$

If $\vec{F}_{net} = 0$ on a rigid body then $\vec{\tau}_{net}$ is same about every point of space.

Force Couple

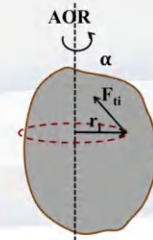


Torque of force couple is same about any point of the space.

$$\sum \tau_{int} = 0$$

$$\left(\sum \tau_{ext} \right)_{AOR} = (I)_{AOR} \alpha$$

Valid only in inertial frame.



①

COM AXIS

②

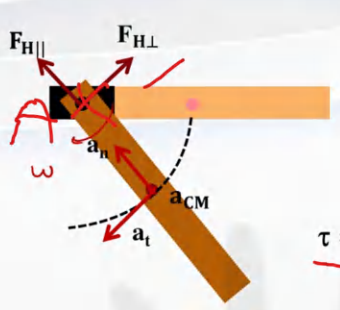
OR Inertial Point

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Calculation of Hinge Force



Rotation Motion



$$F_H = \sqrt{F_{H||}^2 + F_{H\perp}^2}$$

(F_{H⊥}) Perpendicular to rod

$$\sum F_{\perp} = m(a_{CM})_t = m\alpha \frac{L}{2}$$

$$\tau = I\alpha \rightarrow \alpha \rightarrow (a_{CM})_t \rightarrow F_{H\perp}$$

(F_{H||}) Parallel i.e. along the rod

$$\sum F_{||} = m(a_{CM})_n = m\omega^2 \frac{L}{2}$$

$$\text{W-E Theorem} \rightarrow \omega \rightarrow (a_{CM})_n \rightarrow F_{H||}$$

Inertial Pulley

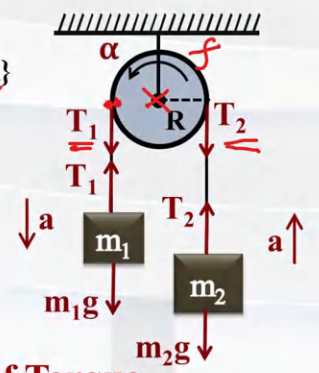
{No slipping of rope on disk}

$$T_1 R - T_2 R = I\alpha \quad \dots(1)$$

$$m_1 g - T_1 = m_1 a \quad \dots(2)$$

$$T_2 - m_2 g = m_2 a \quad \dots(3)$$

$$\alpha R = a \quad \dots(4)$$



Work done in terms of Torque

$$W = \int \tau d\theta \quad P = \tau \omega$$

Q) Find F_H by support if the rod is released from rest. Δ in f position

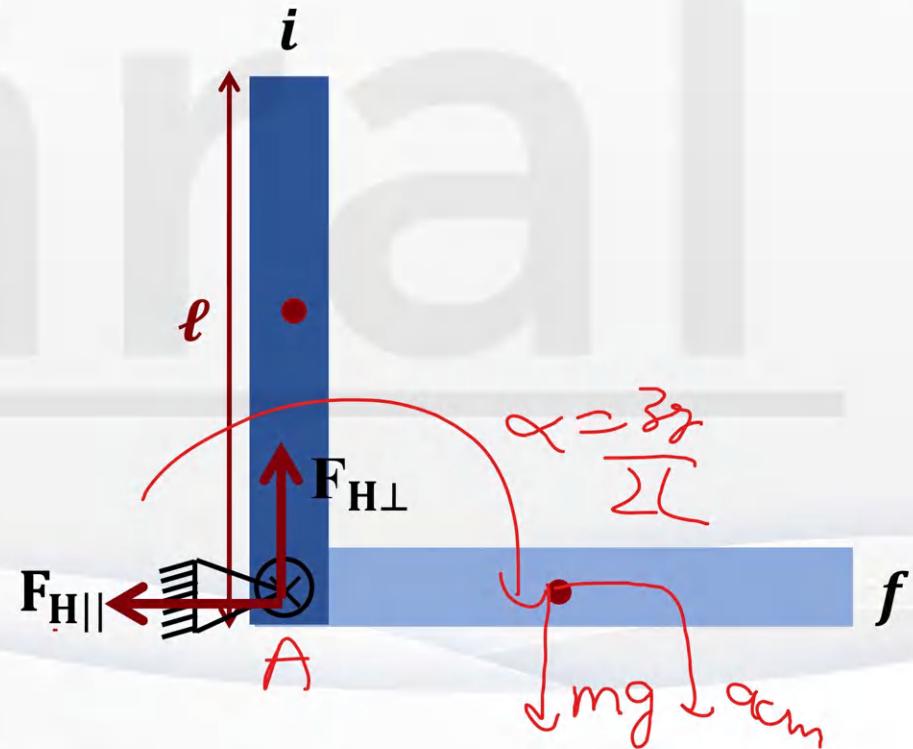
Sol. $\tau = I\alpha \rightarrow \alpha \rightarrow (a_{CM})_t \rightarrow F_{H\perp}$

$\tau = I \times \alpha$ about A

$$\frac{mgL}{2} = \frac{mL^2}{3} \times \alpha \quad \therefore \alpha = \frac{3g}{2L}$$

$$mg - F_{H\perp} = ma_t = m \times \frac{L}{2} \times \frac{3g}{2L}$$

$$F_{H\perp} = \frac{mg}{4}$$



W-E Theorem $\rightarrow \omega \rightarrow (a_{CM})_n \rightarrow F_{H\parallel}$

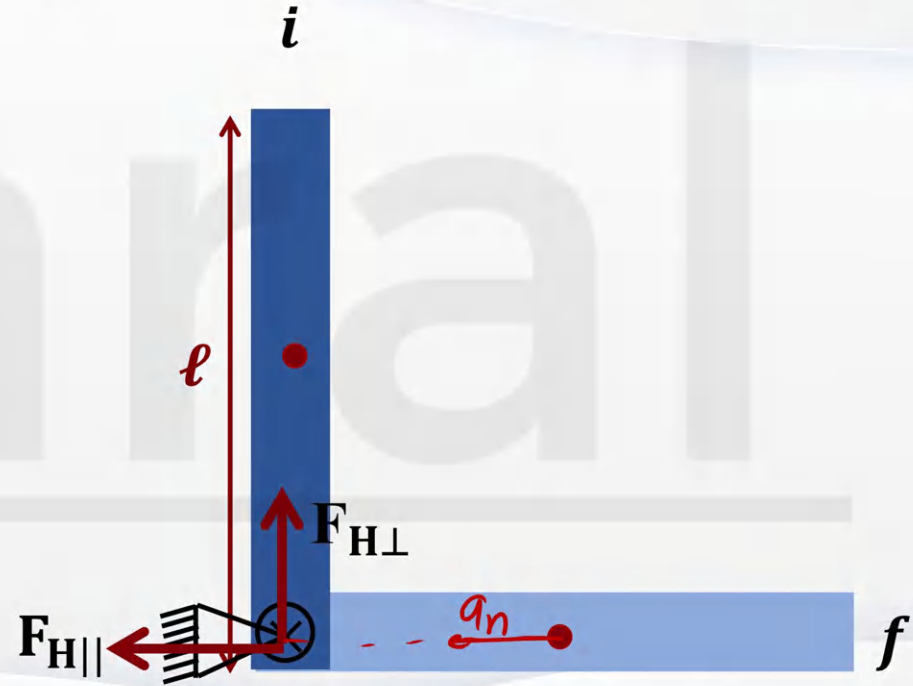
$$W_g + W_H = KE_f - KE_i$$

$$\frac{mgL}{2} + 0 = \frac{1}{2} \frac{mL^2}{3} \omega^2 - 0$$

$$\omega = \sqrt{\frac{3g}{L}}$$

$$F_{H\parallel} = m(a_{CM})_n = m\omega^2 \frac{L}{2}$$

$$F_{H\parallel} = \frac{3mg}{2}$$

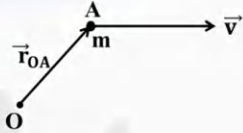


Angular Momentum of Particle

Angular Momentum of Particle about point O is defined as

$$\vec{L}_O = \vec{r}_{OA} \times \vec{P}$$

$$= m \vec{r}_{OA} \times \vec{v}$$



where \vec{P} is linear momentum of the particle present at A.

$$\vec{L} = \vec{r} \times \vec{P}$$

AM is also known as moment of LM.

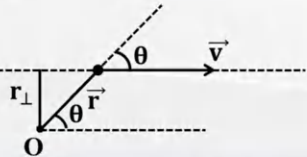
$$m(r \sin\theta)v \Rightarrow \vec{L} = \text{Constant}$$

$$|L| = mr \sin\theta$$

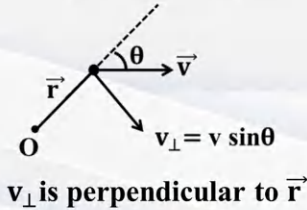
$$|L| = mr_{\perp} v$$

$$|L| = mr(v \sin\theta)$$

$$|L| = mrv_{\perp}$$

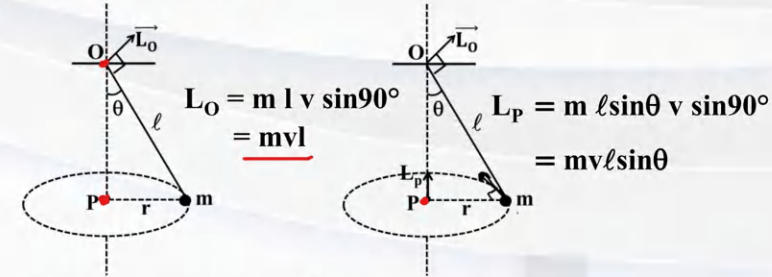


r_{\perp} is the shortest distance from O to line of velocity.



v_{\perp} is perpendicular to \vec{r}

Conical Pendulum



\vec{L}_O is not constant but its magnitude is constant.

\vec{L}_P is constant

Angular Momentum of System of Particles

$$\vec{L}_{\text{sys}} = \sum \vec{L}_i$$

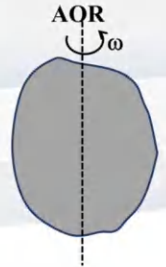
Angular Momentum Conservation Principle

$$\vec{\tau}_{\text{net}} = \frac{d\vec{L}}{dt} \quad \text{If } \vec{\tau}_{\text{net}} = 0 \Rightarrow \vec{L} = \text{Constant}$$

If $\vec{\tau}_{\text{net}}$ is zero then its A.M. is conserved.

A.M. of Rigid Body Performing Pure Rotation About Fixed Axis

$$(L_{\text{sys}})_{\text{AOR}} = I_{\text{AOR}} \omega$$



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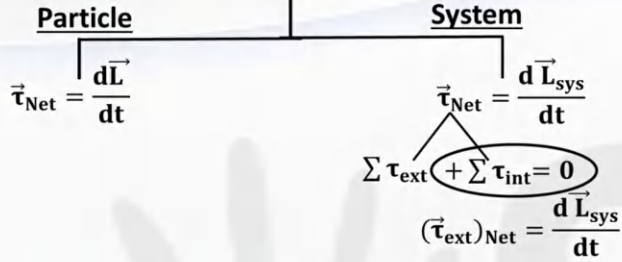


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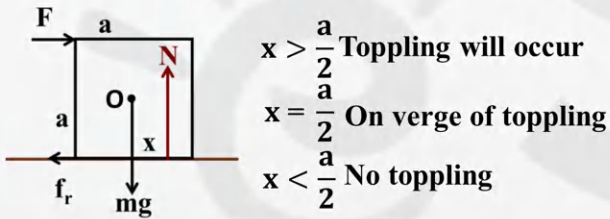
Relation Between Torque and Angular Momentum

$$\vec{\tau}_{\text{Net}} = \frac{d\vec{L}}{dt} \quad \text{valid only in inertial frame.}$$

$$\vec{\tau}_{\text{Net}} = \frac{d\vec{L}}{dt}$$



Condition of Toppling



Angular Impulse

Linear Impulse (\vec{I})

$$\vec{I} = \int \vec{F} dt$$

Unit - Ns

$$\vec{I}_{\text{net}} = \vec{P}_f - \vec{P}_i$$

$$\vec{J} = \vec{r} \times \vec{I}$$

Angular Impulse (\vec{J})

$$\vec{J} = \int \vec{\tau} dt$$

Unit - Nms

$$\vec{J}_{\text{net}} = \vec{L}_f - \vec{L}_i$$

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Q) Particle sticks to rod. Find ω of rod just after collision.

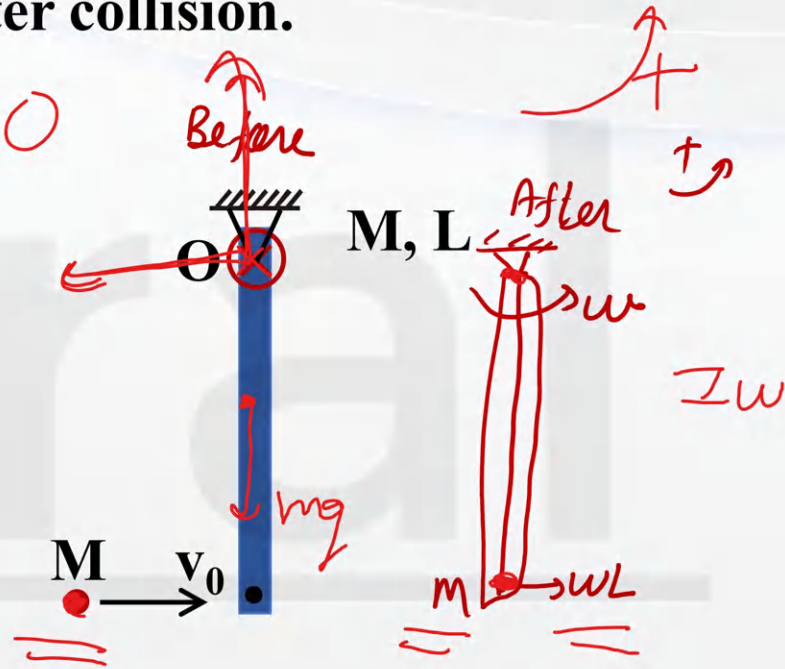
Sol. $(\tau_{\text{Net}})_{\text{rod} + \text{particle}} = 0$

$$\vec{L}_i = \vec{L}_f$$

$$Mv_0L + 0 = M(\omega L)L + \frac{ML^2}{3}\omega$$

$$\omega = \frac{3v_0}{4L}$$

$\tau_{\text{net } O} = 0$



Q) Particle stops after collision. Find ω of Rod.

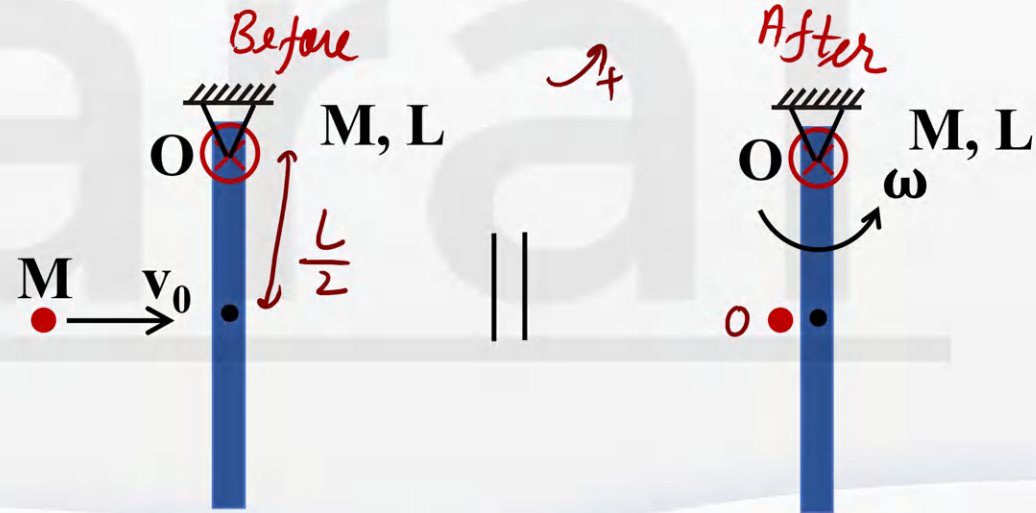
Sol. $(\tau_{\text{Net}})_o = 0$

$$\vec{L}_i = \vec{L}_f$$

for Rod for Rod

$$Mv_0 \frac{L}{2} + 0 = 0 + \frac{ML^2}{3} \omega$$

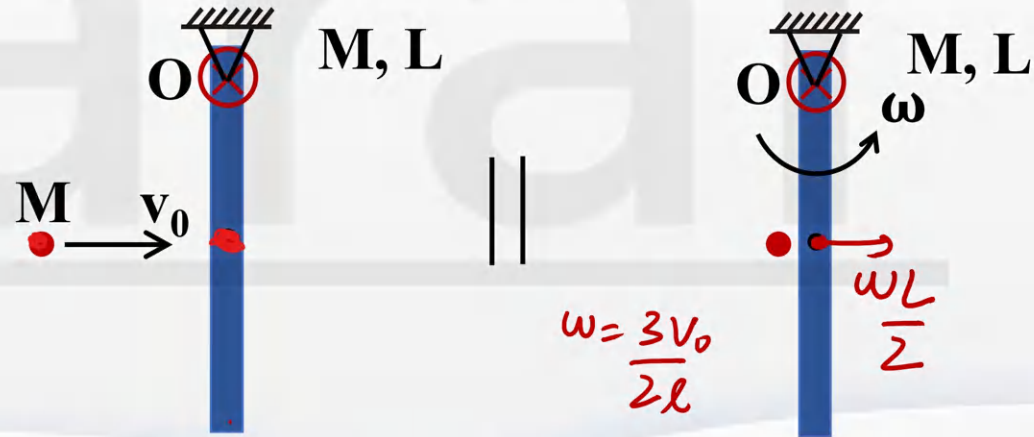
$$\omega = \frac{3v_0}{2L}$$



b) Find value of coefficient of restitution 'e'.

Sol. $e = \frac{\text{velocity of separation}}{\text{velocity of approach}}$

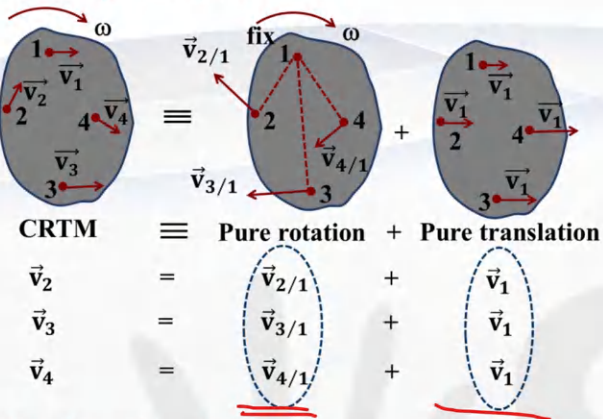
$$e = \frac{\frac{\omega L}{2}}{v_0} = \boxed{\frac{3}{4}}$$



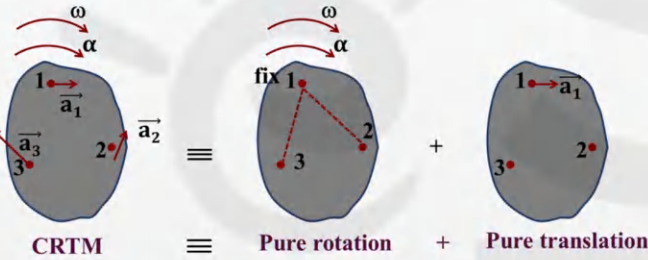
Rotation Motion

Combined Rotation + Translational Motion [CRTM]

Velocity Analysis



Acceleration Analysis



Dynamics of CRTM

For analysing its motion we apply two equation

$$\sum \vec{F}_{\text{ext}} = M\vec{a}_{\text{CM}}$$

$$\sum \vec{\tau}_{\text{ext}} = I\vec{\alpha}$$

Dynamics of CRTM

Second equation is valid in inertial frame.

$$1) \sum \vec{F} = M\vec{a}_{\text{CM}} \quad 2) \sum \vec{\tau} = I\vec{\alpha}$$

$$\sum \vec{F}_{\text{ext}} = M\vec{a}_{\text{CM}} \quad \sum \vec{\tau}_{\text{ext}} = I\vec{\alpha}$$

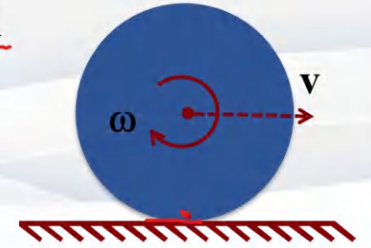
Most suitable point to apply Torque equation is about COM of the body because τ of pseudo force about COM is "zero".

To apply second equation about non-inertial point, Pseudo force is applied at COM of body & τ of Pseudo force is also taken into account.

Rolling Motion

If during the motion, there is no relative slipping between the points of contact, then motion is called Rolling.

$$\underline{v = \omega R}$$



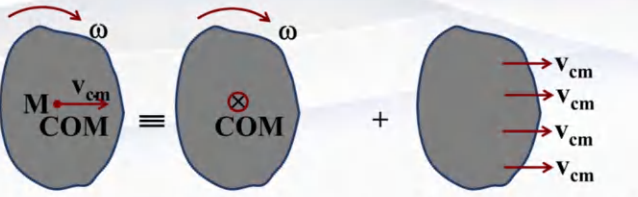
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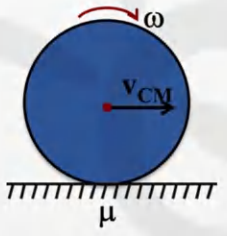
Kinetic Energy of Rigid Body Performing CRTM



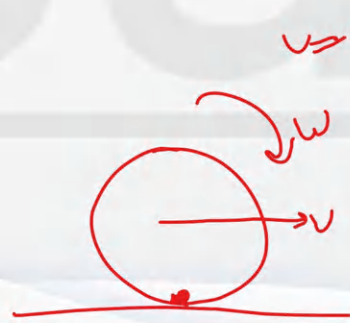
CRTM \equiv Rotational KE + Translational KE

$$KE = \frac{1}{2} I_{CM} \omega^2 + \frac{1}{2} M v_{CM}^2$$

Keypoint



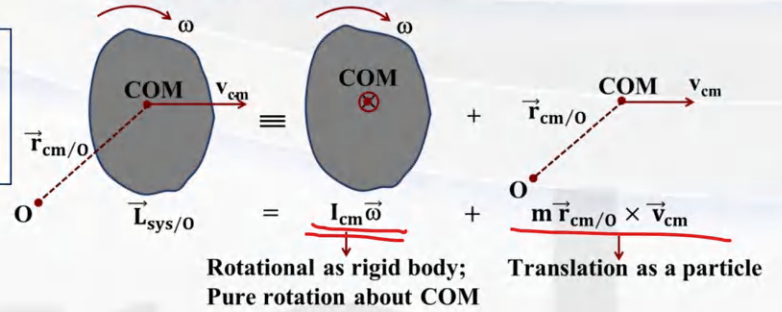
For a body performing rolling motion over a fixed surface, work done by friction force on the body will be zero as velocity of point of application of friction always zero.



Rotation Motion

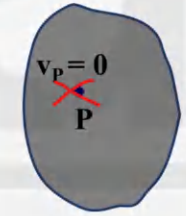
Combined Rotation + Translational Motion [CRTM]

Angular Momentum of R.B. Performing CRTM



$$\vec{L}_{sys/O} = I_{cm} \vec{\omega} + m \vec{r}_{cm/O} \times \vec{v}_{cm}$$

Instantaneous Center of Rotation (I_{COR}) & Axis of Rotation (I_{AOR})



- ❖ Let at an instant of time velocity of point P is zero.
- ❖ To calculate velocity of other points of rigid body, rigid body can be assumed to perform pure rotation about an axis passing through point P at that instant. This point is called I_{COR} and axis passing through it is called I_{AOR} .

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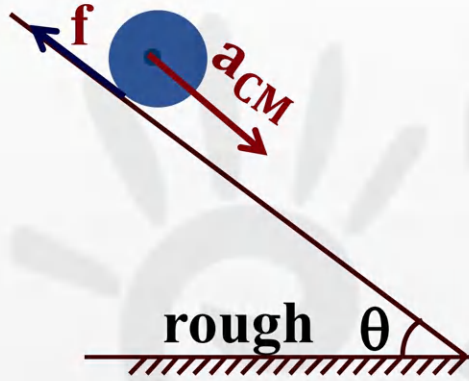
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Rolling

(M, R, I)



$$a_{CM} = \frac{g \sin \theta}{1 + \frac{I}{MR^2}}$$

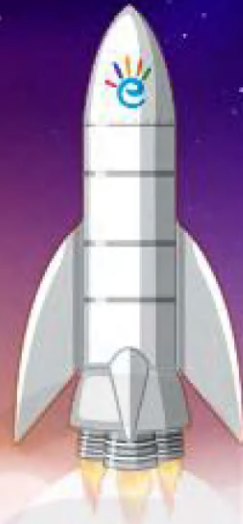
For Rolling

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- IIT Kanpur, Mechanical
- Ex Vice President & Academic Head, Allen, Kota
- Mentored many of **Rank 1 & Top 100** Students
- **30+ years** of Teaching Experience
- **Mentored** over 3,00,000 Students





Saransh Gupta Sir eSaral Physics HoD

- IIT Bombay, CS
- AIR-41 IIT-JEE
- Air-71 AIEEE (JEE Main)
- AIR-4 NSO
- 1% In Top INPHO
- 8+ Years of Teaching Experience
- Mentored Lakhs of Students





Prateek Gupta Sir eSara Chemistry Faculty

- **IIT Bombay, Metallurgy**
- **Online Creativity & Visualization Expert**
- **Mentored Lakhs of Students**



Course Details

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Mentorship

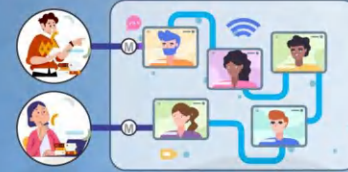


3 Layered Personalised Mentorship

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PERSONAL ACADEMIC
MENTOR



PROGRESS MENTOR
FOR TRACKING PROGRESS



LIVE MENTORSHIP SESSIONS

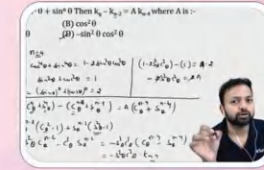


4 Layered DOUBT SOLVING

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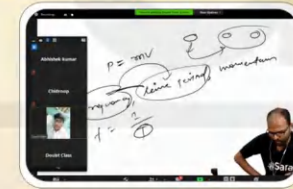
SOULTION OF PRACTICE SHEETS



DEDICATED DOUBT HOTLINE



LIVE DOUBT SOLVING CLASSES

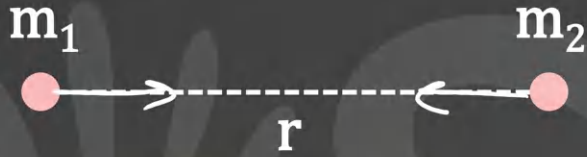


PERSONALISED CONNECT WITH FACILTIES



Gravitation

Superfast Revision



$$F = \frac{Gm_1m_2}{r^2}$$

$$G = 6.67 \times 10^{-11} \text{ Nm}^2/\text{kg}^2$$

↓
Universal Gravitational Constant

Electrostatics

$$\frac{kq_1q_2}{r^2}$$

q

$$k = \frac{1}{4\pi\epsilon_0}$$

$\lambda \sigma \rho$

\vec{E}

Gravitation

$$\frac{Gm_1m_2}{r^2}$$

m

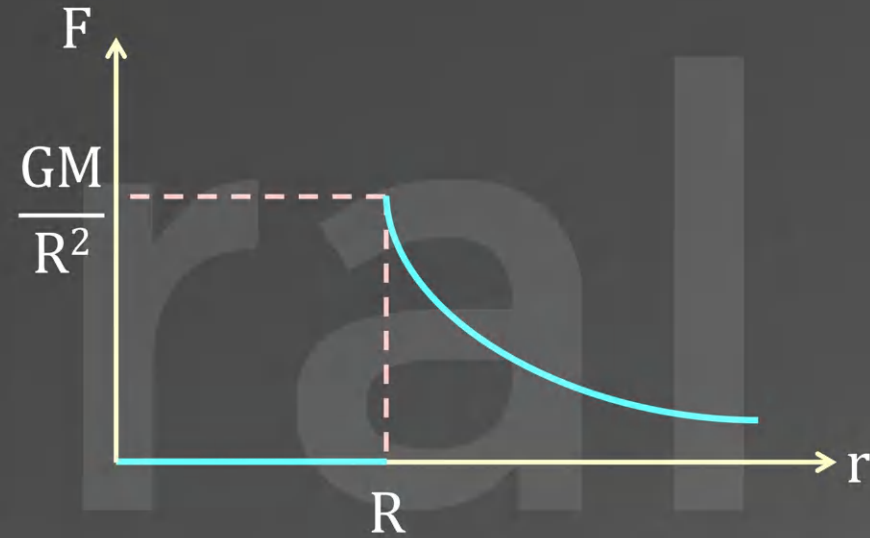
G

$\lambda \sigma \rho$

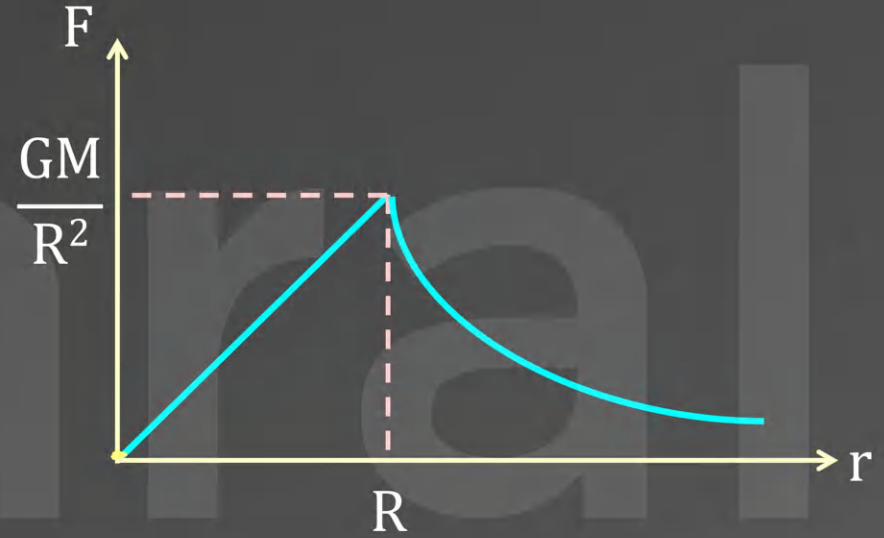
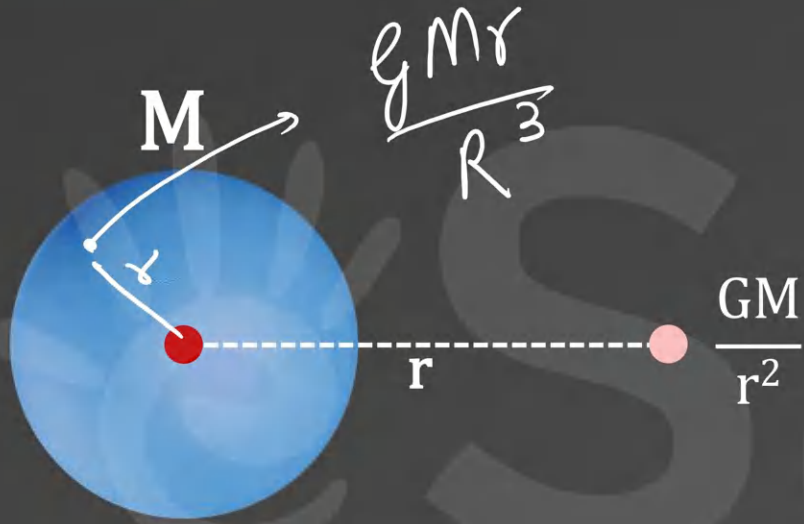
\vec{G}



$$\text{Gravitational Field Intensity} = \frac{GM}{r^2}$$
$$= \frac{RQ}{r^2}$$

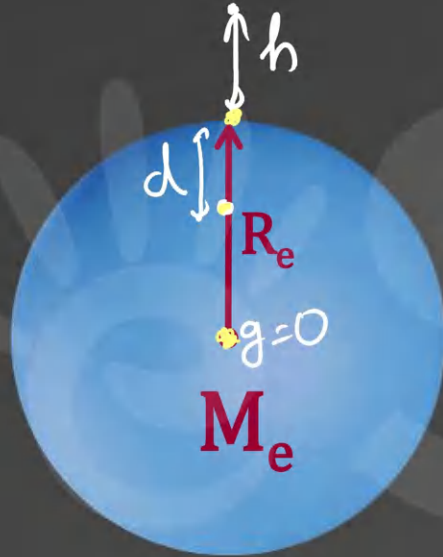


Solid Sphere





Acceleration due to Gravity



At surface

$$g_0 = \frac{G M_e}{R_e^2} = \underline{9.8 \text{ m/s}^2}$$

At height

$$g = \frac{g_0}{\left(1 + \frac{h}{R_e}\right)^2} \approx g_0 \left(1 - \frac{2h}{R_e}\right) \quad \text{for } h \ll R_e$$

At depth

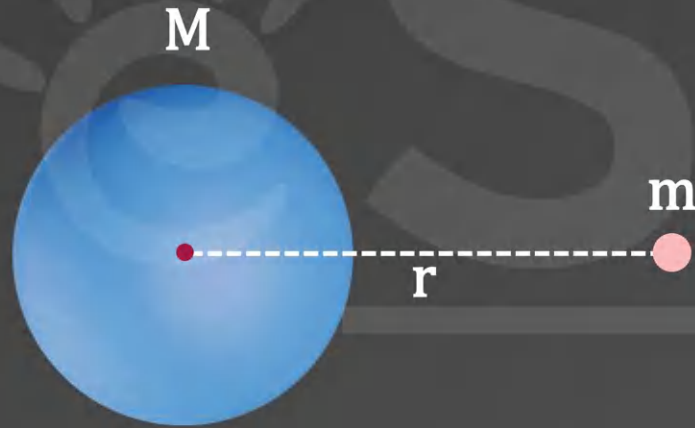
$$g = g_0 \left(1 - \frac{d}{R_e}\right)$$



Gravitational Potential Energy



$$U = \frac{-G m_1 m_2}{r}$$



Handwritten notes:
Kav₁v₂
γ



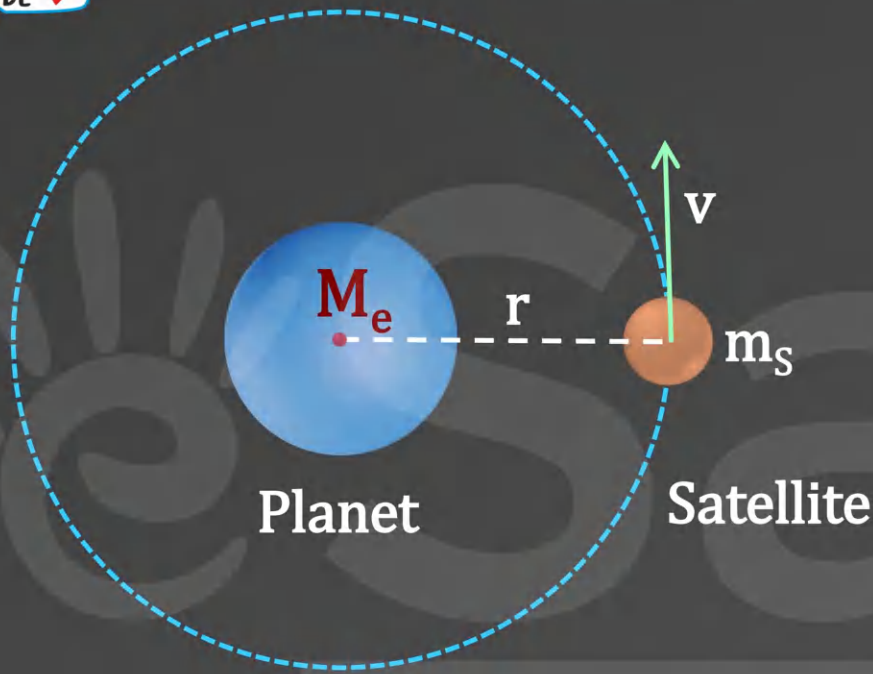
$$V = \frac{U}{m}$$

$$U = \frac{-GMm}{r}$$

$$\Rightarrow V = \frac{-GM}{r}$$

Scalar

Motion of Satellite (Circular Orbit)



$$v = \sqrt{\frac{GM_e}{r}}$$

Orbital Speed

Distance between center of earth and Satellite

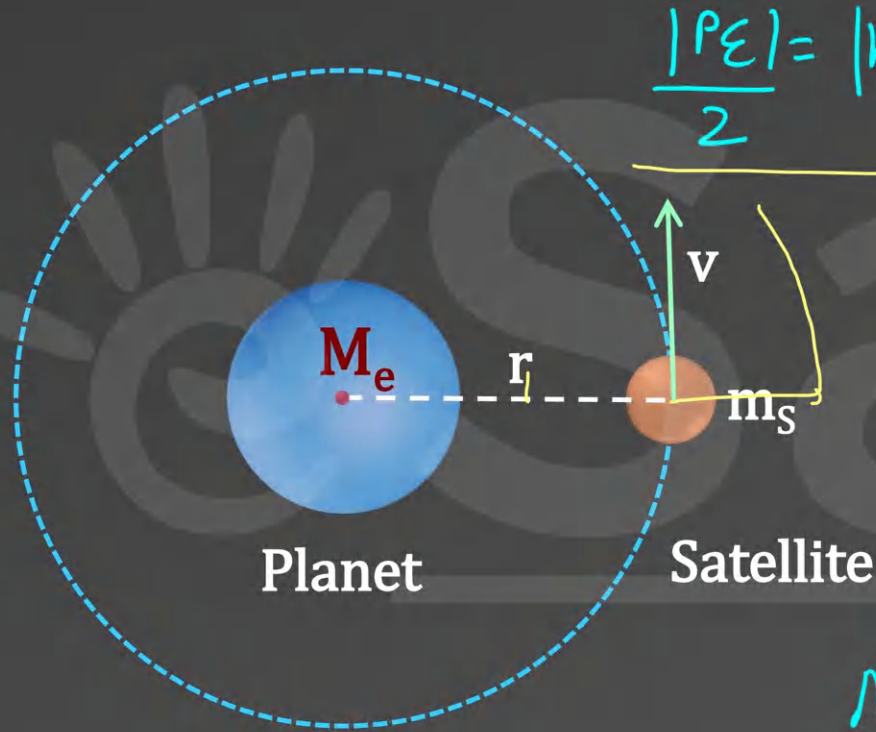
$$\frac{GM_e m_s}{r^2} = \frac{m_s v^2}{r}$$

$$T = \frac{2\pi r}{v}$$

$$T = 2\pi \sqrt{\frac{r^3}{GM_e}}$$

$$T \propto r^{\frac{3}{2}}$$





$$\frac{|PE|}{2} = |KE| = \frac{|ME|}{2}$$

$$U = PE = -\frac{g m_e m_s}{r}$$

$$KE = \frac{1}{2} m_s v^2 = \frac{g m_e m_s}{2r}$$

$$ME = PE + KE = -\frac{g m_e m_s}{2r}$$



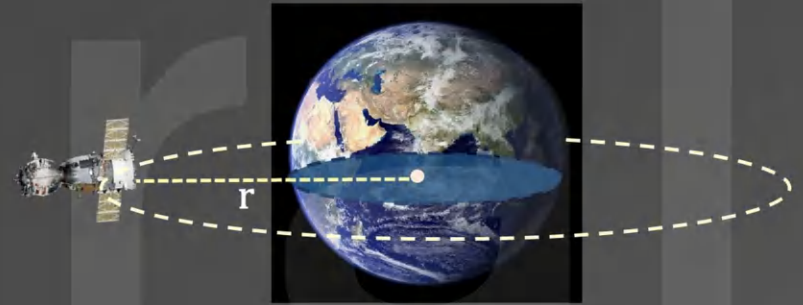
Satellites in a circular orbit around earth in equatorial plane with $T=24$ hours are called **Geostationary Satellite**.

It revolves in equatorial plane from west to east in same sense as earth.

Its angular velocity with respect to earth is Zero.

Its orbit is called **Parking Orbit**.

It is used for telecommunication, weather forecasting, etc.



24 hrs

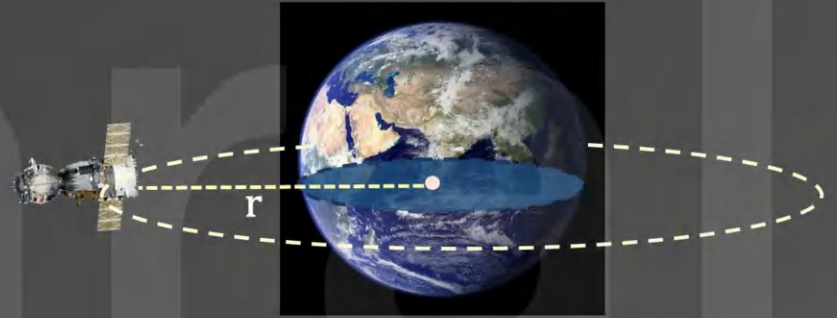
$$T = 2\pi \sqrt{\frac{r^3}{GM_e}}$$

$r = 42170 \text{ km}$

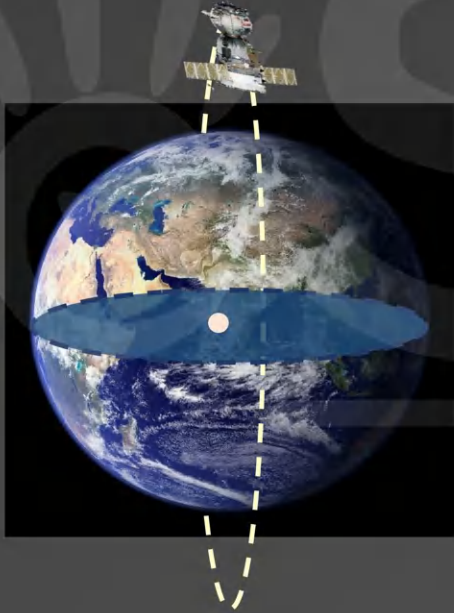
From surface = $42170 - 6370$

$= 35800 \text{ km} \approx 36000 \text{ km}$

Orbital Velocity = 3.08 km/sec.

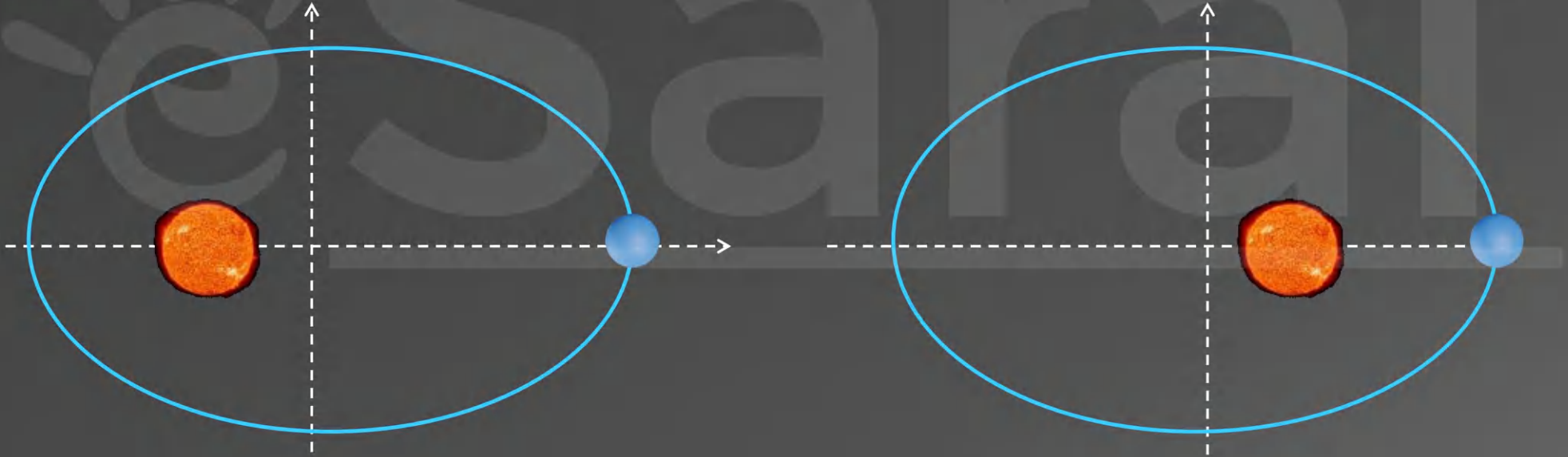


It is used for remote sensing,
environmental studies.



1-Law of Orbits

All planets move in elliptical orbits with the Sun situated at one of the foci.

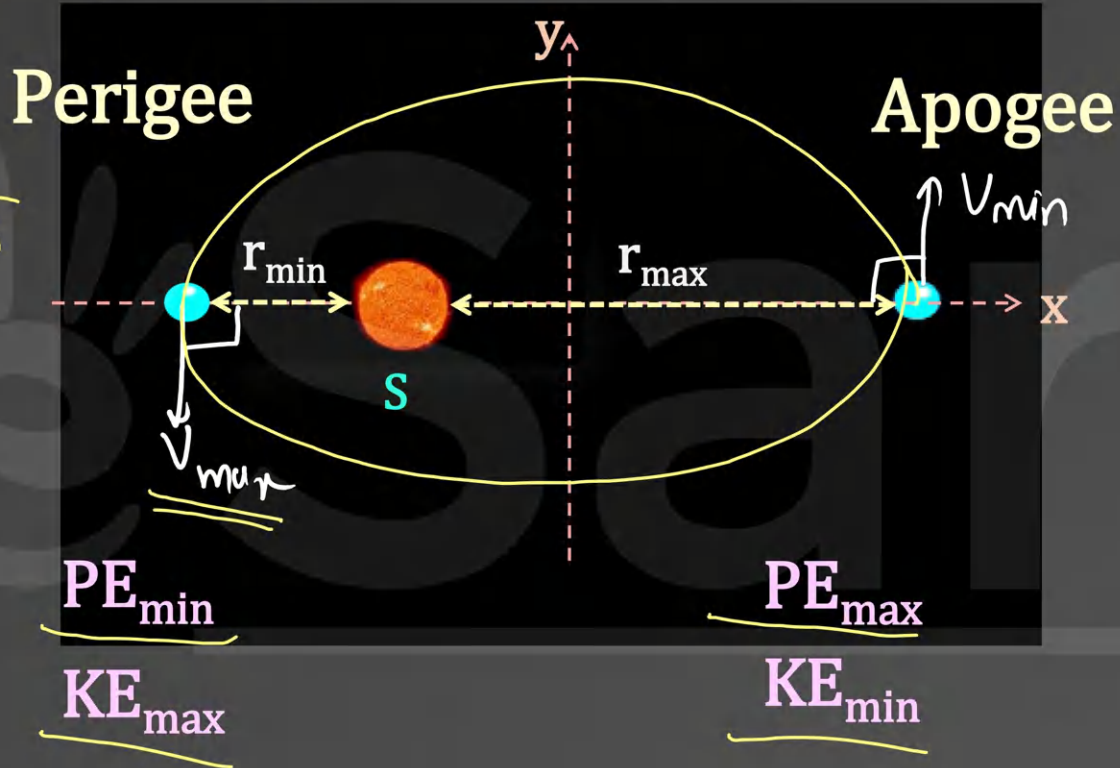


Kepler's Laws



TRICK

TRICK



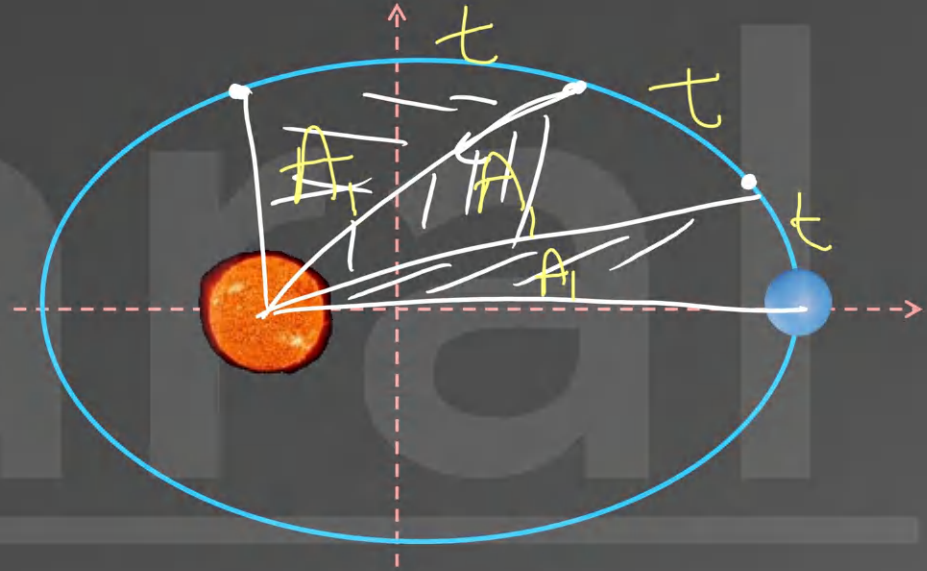


2-Law of Areas

Position vector from Sun to the planet sweeps out equal area in equal time intervals.

Areal velocity of planet around Sun always remains constant.

This law is based on angular momentum conservation.



2-Law of Areas



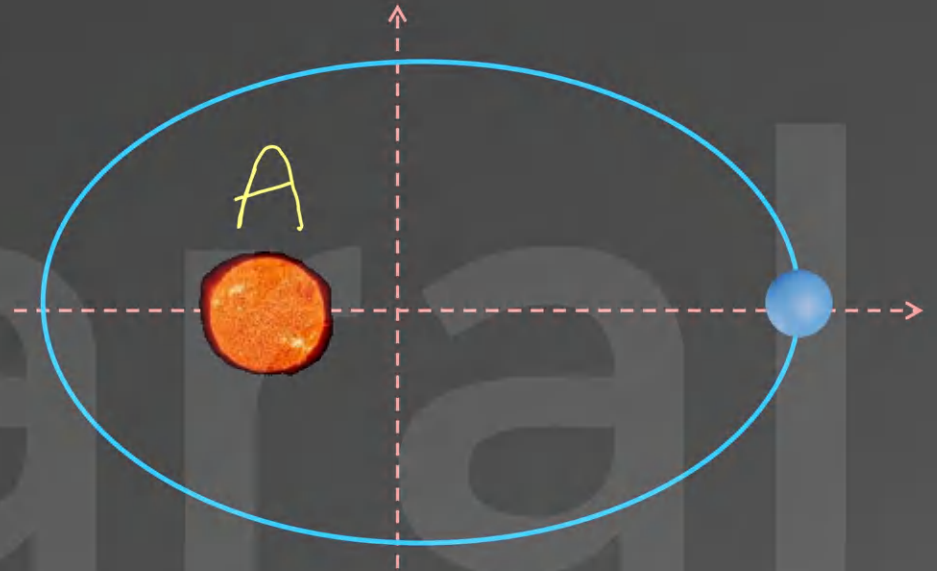
$$A = \frac{L T}{2M_p}$$

Constant

$$\underbrace{\frac{dA}{dt}}_{\text{Areal Velocity}} = \frac{L}{2M_p} \longrightarrow \text{Angular Momentum about Sun}$$

Areal Velocity

$$\frac{A}{T} = \frac{L}{2M_p}$$



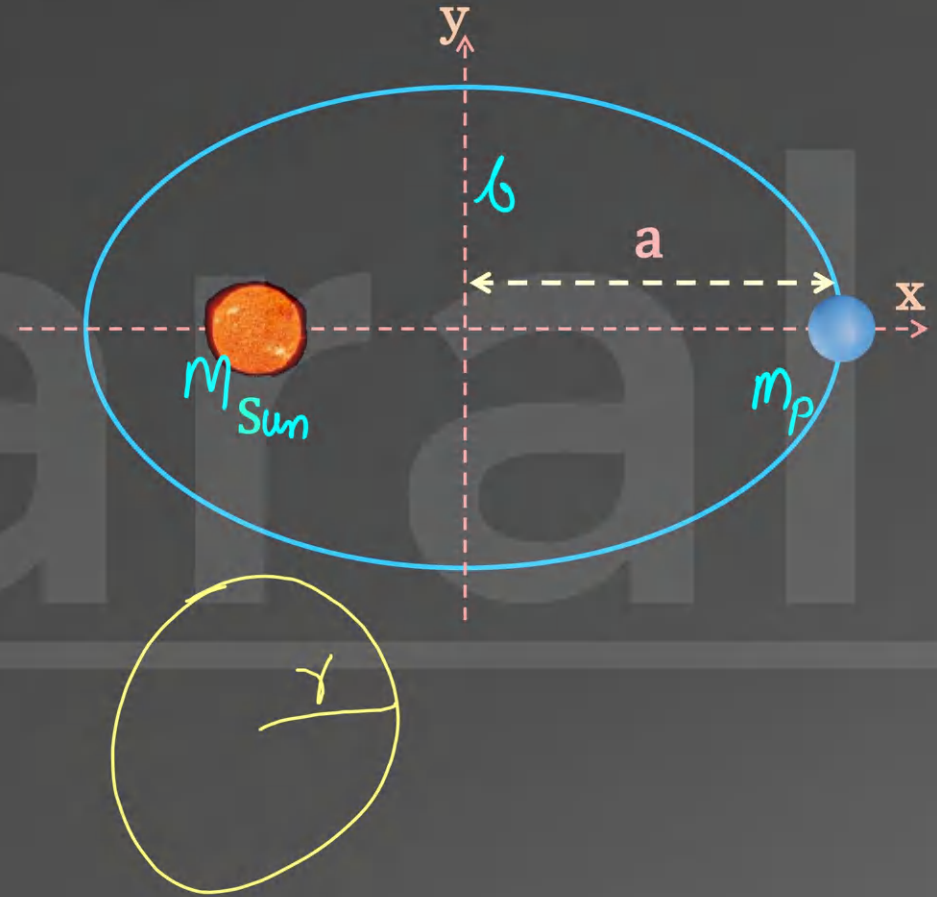
3-Law of Periods

The square of the time period of revolution of a planet is proportional to the cube of the semi-major axis of the ellipse traced out by the planet.

$$T^2 \propto a^3$$

$$\Rightarrow T \propto a^{3/2}$$

$$T = 2\pi \sqrt{\frac{a^3}{GM_{\text{sun}}}}$$



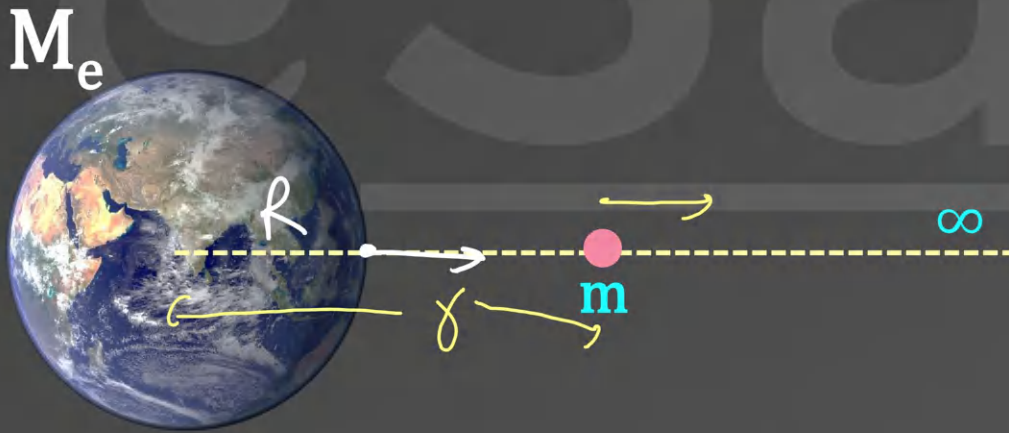
Escape Velocity



$$v_e = \sqrt{\frac{2GM_e}{r}}$$

$$\sqrt{2g_m r}$$

At Earth's Surface, $v_e = \sqrt{2g_0 R} = 11.2 \text{ km/s}$



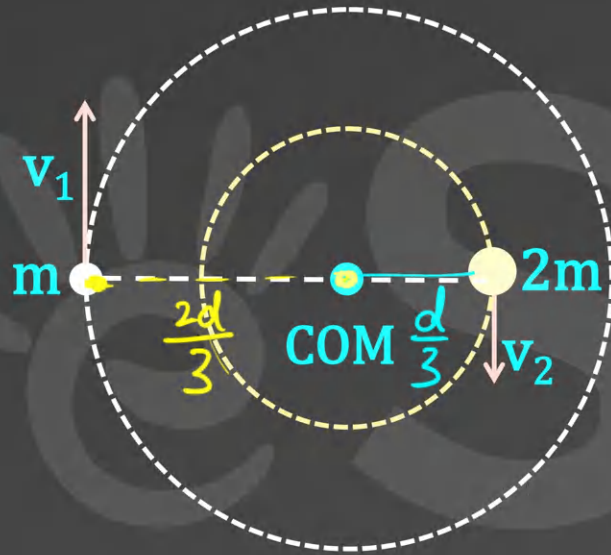


$v = \frac{v_e}{\sqrt{2}}$ Circular

If $v < v_e$ $TE < 0$ Path: Bounded and Elliptical

If $v = v_e$ $TE = 0$ Path : Unbounded and Parabolic

If $v > v_e$ $TE > 0$ Path : Unbounded and Hyperbolic



A pair of stars rotating about their COM (centre of mass).

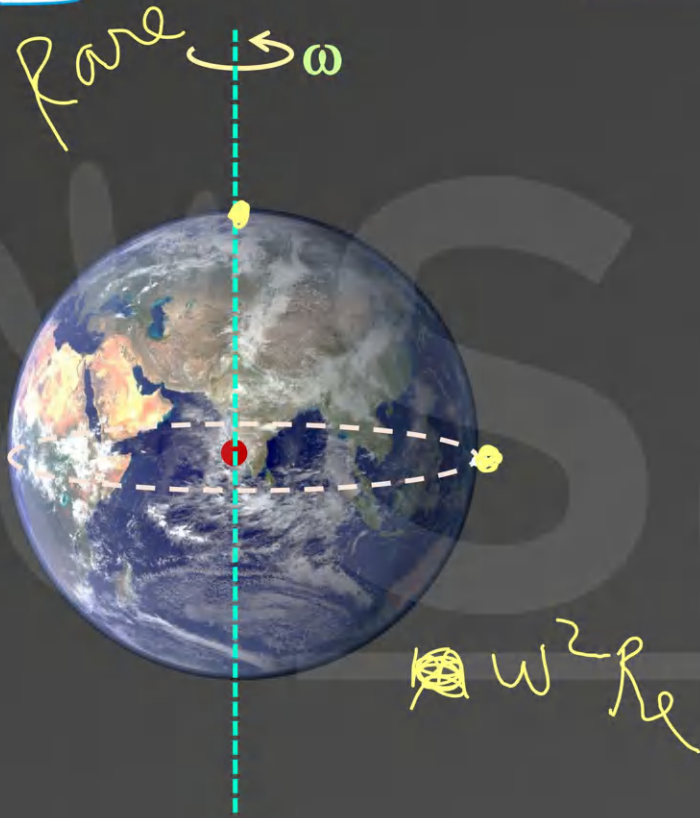
$$\frac{v_1}{v_2} = \frac{2}{1}$$

$$\frac{KE_1}{KE_2} = \frac{2}{1}$$

$$\frac{T_1}{T_2} = \frac{1}{1}$$

$$\frac{L_1}{L_2} = \frac{2}{1}$$

Variation of g_{app} due to Rotation of Earth



max

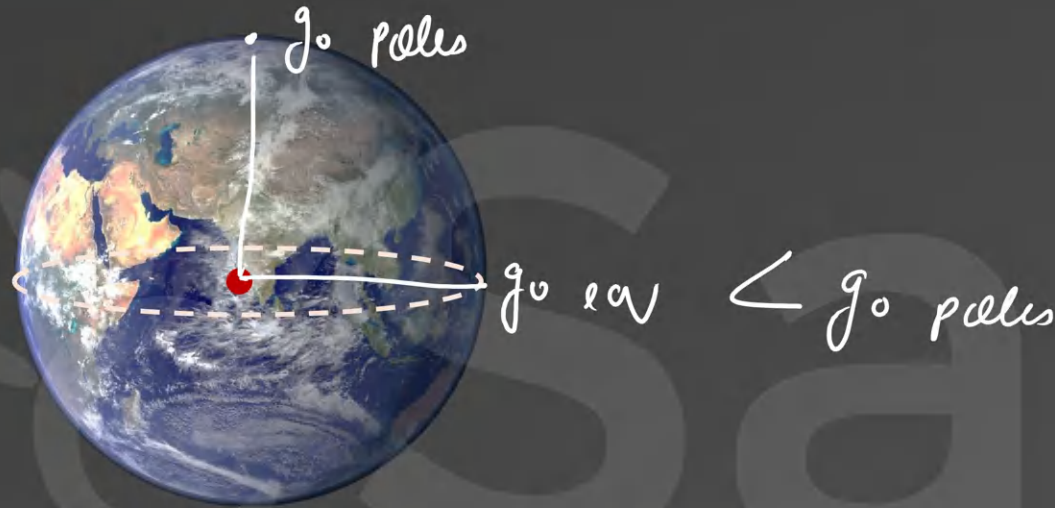
$$g_{app} = g_0$$

at Poles

min

$$g_{app} = g_0 - \omega^2 R_e \quad \text{at equator}$$

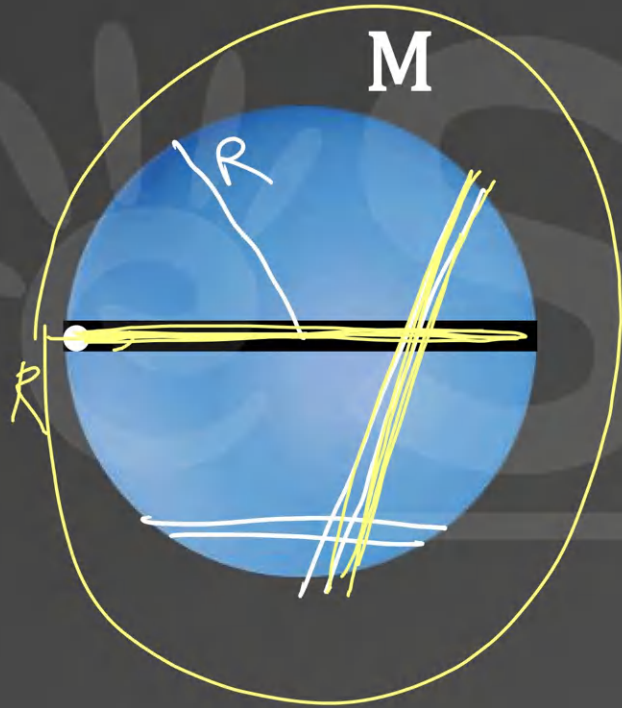




Earth is bulged at equator

g_0 is more at poles than at equator.

Time period of particle in tunnel in Solid Sphere



TRICK

$$T = 2\pi \sqrt{\frac{R^3}{GM}}$$



Lets
Meditate !!

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Simple Harmonic Motion

Superfast Revision

Equation of SHM

$$x = A \sin (\omega t + \phi)$$

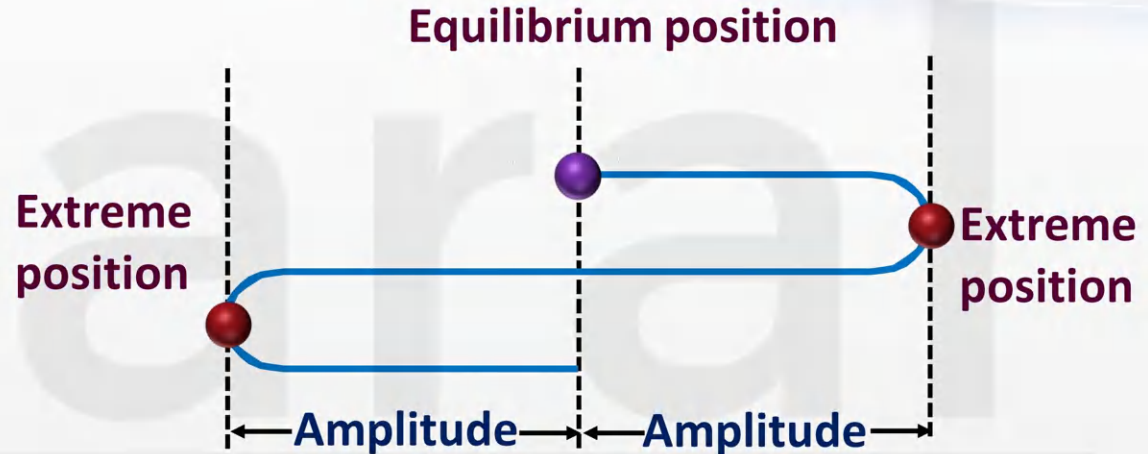
$$F_{\text{net}} = -kx$$

$$ma = -kx$$

$$a = -\omega^2 x$$

$$\omega = \sqrt{\frac{k}{m}}$$

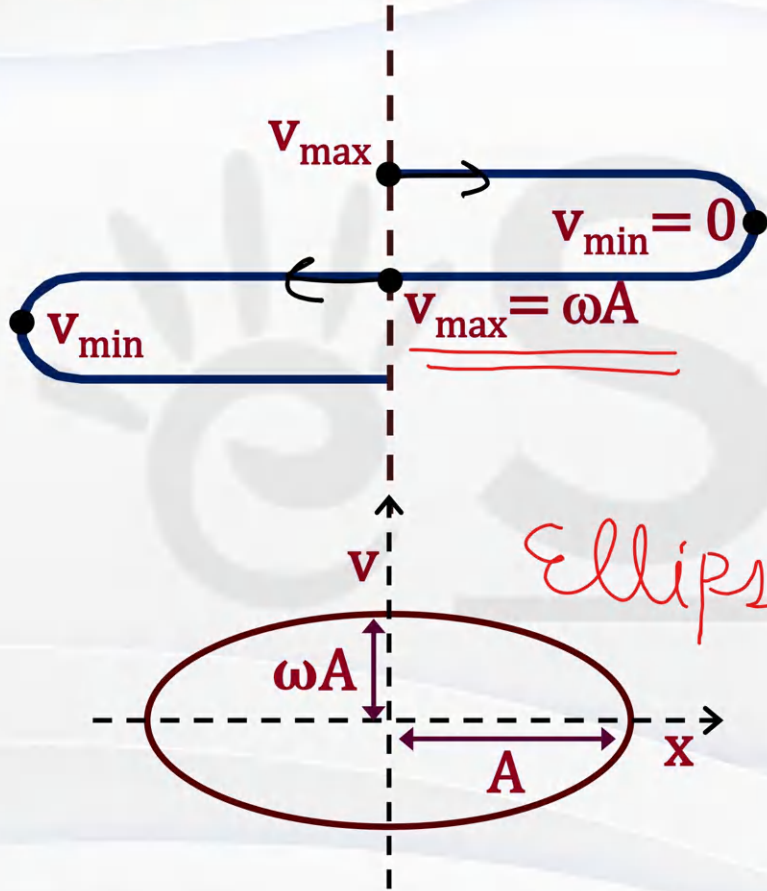
Angular Frequency



$$T = \frac{2\pi}{\omega}$$

$$f = \frac{1}{T} = \frac{\omega}{2\pi}$$

Velocity Analysis



$$x = A \sin(\omega t + \phi) \quad \dots(1)$$

$$v = \frac{dx}{dt} = A\omega \cos(\omega t + \phi) \quad \dots(2)$$

$$v = \omega \sqrt{(A^2 - x^2)}$$

$$\frac{x^2}{A^2} + \frac{v^2}{(\omega A)^2} = 1$$

Acceleration Analysis



$$x = A \sin(\omega t + \phi)$$

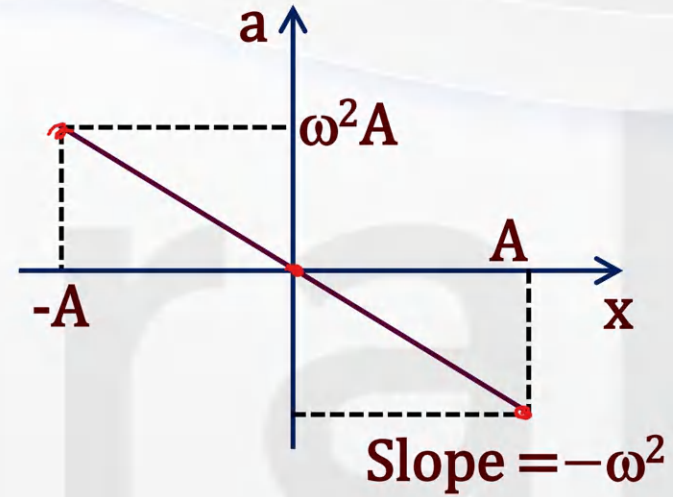
$$v = A\omega \cos(\omega t + \phi)$$

$$a = -A\omega^2 \sin(\omega t + \phi)$$

$$a = -\omega^2 x$$

$$a_{\max} = \omega^2 A$$

at extreme position

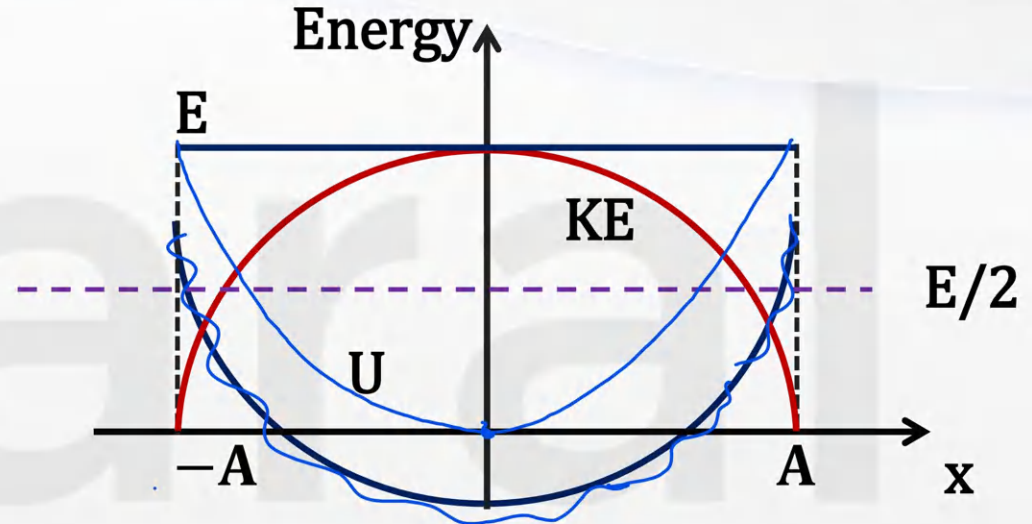


Energies v/s 'x'

$$U = \frac{1}{2} kx^2$$

$$KE = \frac{1}{2} k(A^2 - x^2)$$

$$KE + U = E = \frac{1}{2} kA^2$$

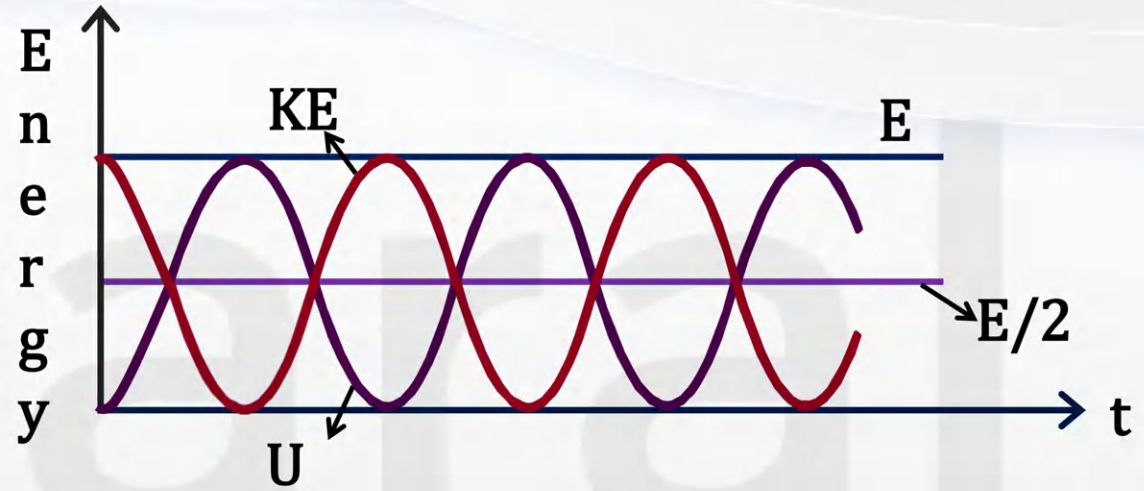


Energies v/s 't'

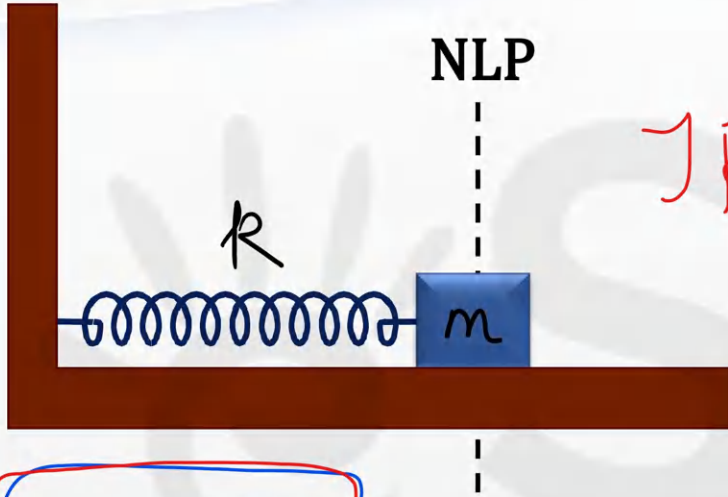


$$U = \frac{1}{2} kA^2 \sin^2(\omega t + \phi)$$

$$KE = \frac{1}{2} kA^2 \cos^2(\omega t + \phi)$$



Spring Block System



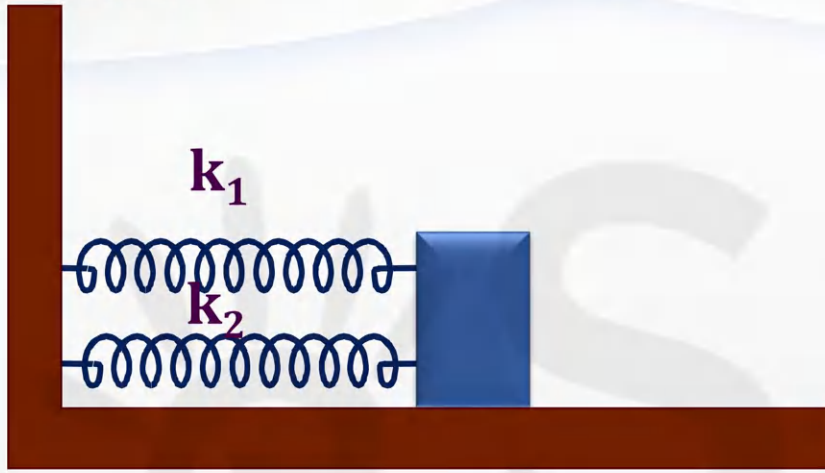
TRICK

In a spring block system, if an additional constant force (along line of SHM) is applied on the block then time period remains same.

$$T = 2\pi \sqrt{\frac{m}{k}}$$

~~$2\pi \sqrt{\frac{m}{k}}$~~





$$\underline{k_{eq} = k_1 + k_2}$$

$$T = 2\pi \sqrt{\frac{m}{k_{eq}}} = 2\pi \sqrt{\frac{m}{k_1 + k_2}}$$



$$T = 2\pi \sqrt{\frac{m}{k_{eq}}}$$

$$k_{eq} = \frac{k_1 k_2}{k_1 + k_2}$$

$$\frac{1}{k_{eq}} = \frac{1}{k_1} + \frac{1}{k_2}$$



k



natural length = ℓ

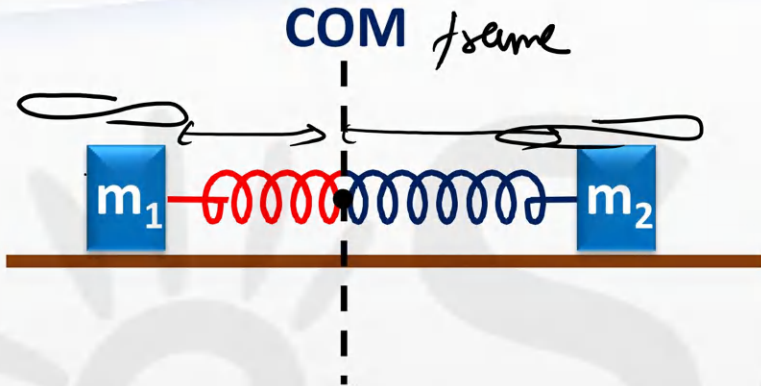
$k\ell = \text{Constant}$

2k



natural length = $\ell/2$

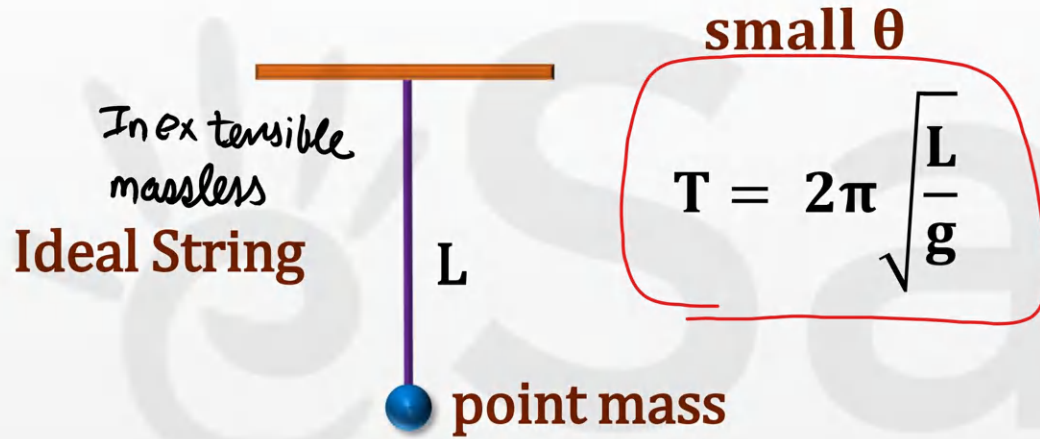
$k\ell = 2k \frac{\ell}{2}$



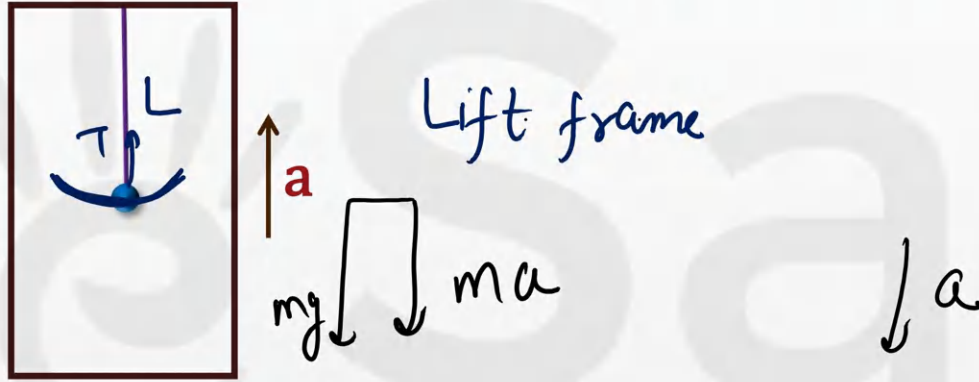
$$\mu = \frac{m_1 m_2}{m_1 + m_2} \rightarrow \text{reduced mass}$$

$$T_1 = 2\pi \sqrt{\frac{m_1 m_2}{k(m_1 + m_2)}} = 2\pi \sqrt{\frac{\mu}{k}}$$

Simple Pendulum



Q) A pendulum is attached to the top wall of a lift which is going up with acceleration 'a'. Find its time period in this situation.



Sol. $g_{\text{eff}} = (g+a)$

$$T = 2\pi \sqrt{\frac{L}{g_{\text{eff}}}} = 2\pi \sqrt{\frac{L}{g+a}} \quad T = 2\pi \sqrt{\frac{L}{g-a}}$$

Physical Pendulum



$$T = 2\pi \sqrt{\frac{I}{mgd}}$$



TRICK



I : MOI of system about hinge.

m : Mass of system

d : distance between COM and hinge.

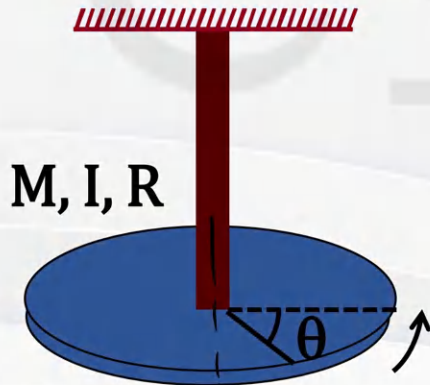


$$\tau \propto -\theta$$

$$\tau = -C\theta \quad (C = \text{Torsional constant})$$

$$T = 2\pi \sqrt{\frac{I}{C}}$$

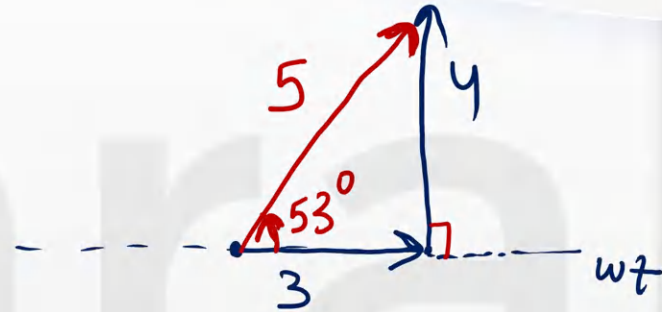
$$2\pi \sqrt{\frac{m}{k}}$$



Composition of SHMs

$$x = 3 \sin(\omega t) + 4 \sin\left(\omega t + \frac{\pi}{2}\right)$$

$$x = 5 \sin(\omega t + 53^\circ)$$



$$A_{res}^2 = A_1^2 + A_2^2 + 2A_1A_2 \cos \phi$$



$$F_{\text{drag}} = -bv$$

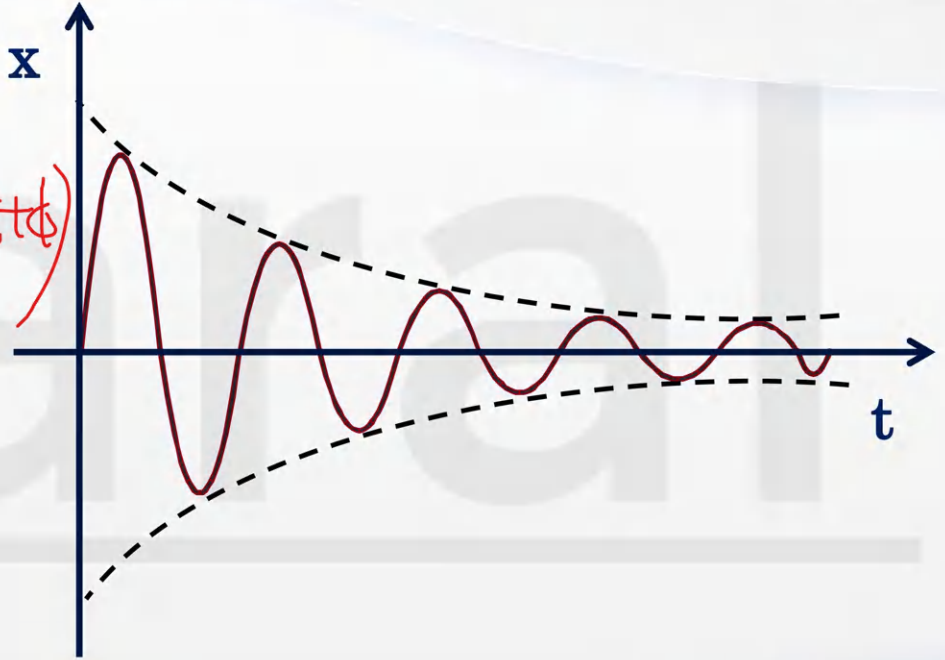
$$F = -kx - bv$$

$$x = Ae^{-bt/2m} \sin(\omega't + \phi)$$

$$\omega' = \sqrt{\frac{k}{m} - \frac{b^2}{4m^2}}$$

$$E = \frac{1}{2}kA^2e^{-bt/m}$$

$$x = A \sin(\omega t + \phi)$$



Forced Oscillations and Resonance

$$F_{\text{driving}} = F_0 \sin(\omega_d t)$$

$$ma = -kx - bv + F_0 \sin(\omega_d t)$$

$$x = A \sin(\omega_d t + \phi)$$

$$A = \frac{F_0/m}{\sqrt{(\omega^2 - \omega_d^2)^2 + (b\omega_d/m)^2}}$$

If small damping, (b very small)

$$A = \frac{F_0/m}{(\omega^2 - \omega_d^2)}$$

$\omega_d \approx \omega$ Resonance

3 min Break

QUIZ
TIME

SIMPLE HARMONIC MOTION

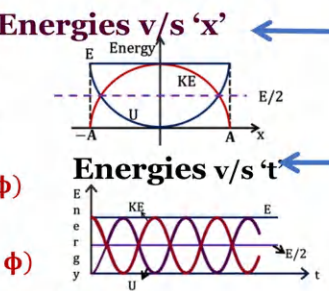
$$U = \frac{1}{2}kx^2$$

$$KE = \frac{1}{2}k(A^2 - x^2)$$

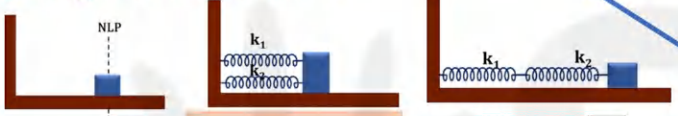
$$KE + U = E = \frac{1}{2}kA^2$$

$$U = \frac{1}{2}kA^2 \sin^2(\omega t + \phi)$$

$$KE = \frac{1}{2}kA^2 \cos^2(\omega t + \phi)$$



Spring Block System



$$T = 2\pi \sqrt{\frac{m}{k}}$$

$$T = 2\pi \sqrt{\frac{m}{k_{eq}}}$$

$$k_{eq} = \frac{k_1 k_2}{k_1 + k_2}$$

$$T = 2\pi \sqrt{\frac{m}{k_1 + k_2}}$$

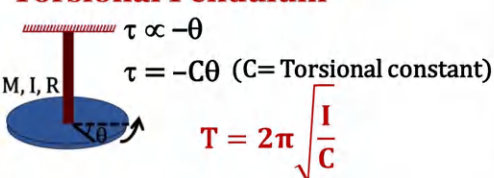
Two Blocks SHM



$$\mu = \frac{m_1 m_2}{m_1 + m_2}$$

$$T_1 = 2\pi \sqrt{\frac{m_1 m_2}{k(m_1 + m_2)}} = 2\pi \sqrt{\frac{\mu}{k}}$$

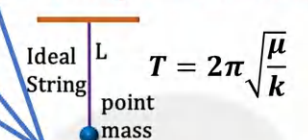
Torsional Pendulum



$$\tau = -C\theta$$

$$T = 2\pi \sqrt{\frac{I}{C}}$$

Simple Pendulum



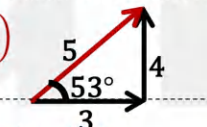
$$T = 2\pi \sqrt{\frac{\mu}{k}}$$

Composition of Two SHM's of same ω along mutually perpendicular directions

$$x = 3 \sin(\omega t) + 4 \sin(\omega t + \frac{\pi}{2})$$

$$x = 5 \sin(\omega t + 53^\circ)$$

$$\vec{x} = A_1 \sin(\omega t) \hat{i} \quad \vec{y} = A_2 \sin(\omega t + \phi) \hat{j}$$



When $\phi = 0$	When $\phi = \pi$	When $\phi = \frac{\pi}{2}$	When $\phi \neq 0, \frac{\pi}{2}, \pi$
$y = \frac{A_2}{A_1} x$	$y = -\frac{A_2}{A_1} x$	$\frac{x^2}{A_1^2} + \frac{y^2}{A_2^2} = 1$	

- (1) Periodic $F_{net} = -kx$ $\omega = \sqrt{\frac{k}{m}}$
- (2) Oscillatory $a = -\omega^2 x$ $f = \frac{1}{T} = \frac{\omega}{2\pi}$
- (3) $|F| \propto |x|$ $x = A \sin(\omega t + \phi)$

Time Period & Frequency $T = \frac{2\pi}{\omega}$ $f = \frac{1}{T} = \frac{\omega}{2\pi}$

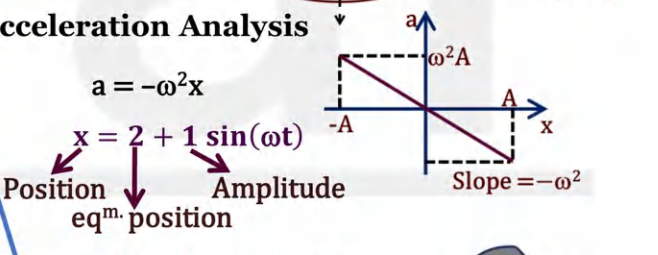
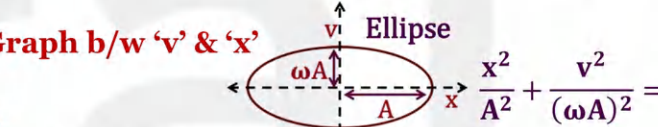
Velocity Analysis $x = A \sin(\omega t + \phi)$

$$v = \frac{dx}{dt} = A\omega \cos(\omega t + \phi)$$

$$v = \omega \sqrt{A^2 - x^2}$$

Max velocity $v_{max} = \omega A$ at $x = 0$ (Mean Position)

Min velocity $v_{min} = 0$ at $x = \pm A$ (Extreme Position)



Physical Pendulum

2

I : MOI of system about hinge.
 m : Mass of system
 d : distance between COM and hinge.

SIMPLE HARMONIC MOTION

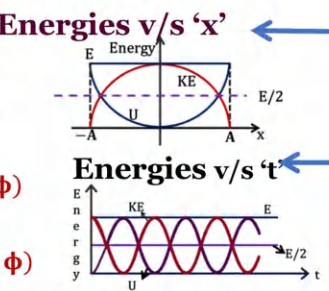
$$U = \frac{1}{2}kx^2$$

$$KE = \frac{1}{2}k(A^2 - x^2)$$

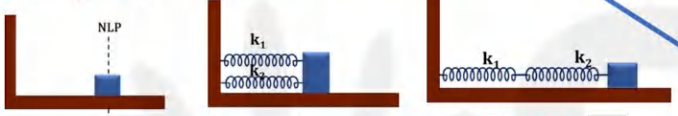
$$KE + U = E = \frac{1}{2}kA^2$$

$$U = \frac{1}{2}kA^2 \sin^2(\omega t + \phi)$$

$$KE = \frac{1}{2}kA^2 \cos^2(\omega t + \phi)$$



Spring Block System



$$T = 2\pi \sqrt{\frac{m}{k}}$$

$$k_{eq} = k_1 + k_2$$

$$T = 2\pi \sqrt{\frac{m}{k_{eq}}}$$

$$= 2\pi \sqrt{\frac{m}{k_1 + k_2}}$$

$$T = 2\pi \sqrt{\frac{m}{k_{eq}}}$$

$$k_{eq} = \frac{k_1 k_2}{k_1 + k_2}$$

In a spring block system, if an additional constant force (along line of SHM) is applied on the block then time period remains same.

Two Blocks SHM

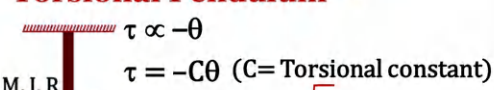


$$\mu = \frac{m_1 m_2}{m_1 + m_2}$$

Reduced Mass

$$T_1 = 2\pi \sqrt{\frac{m_1 m_2}{k(m_1 + m_2)}} = 2\pi \sqrt{\frac{\mu}{k}}$$

Torsional Pendulum

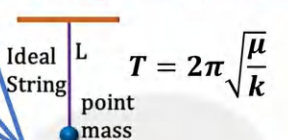


$$\tau \propto -\theta$$

$$\tau = -C\theta \quad (C = \text{Torsional constant})$$

$$T = 2\pi \sqrt{\frac{I}{C}}$$

Simple Pendulum

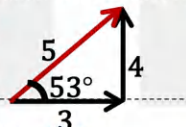


$$T = 2\pi \sqrt{\frac{\mu}{k}}$$

Composition of Two SHM's of same ω along mutually perpendicular directions

$$x = 3 \sin(\omega t) + 4 \sin(\omega t + \frac{\pi}{2})$$

$$x = 5 \sin(\omega t + 53^\circ)$$



$$\vec{x} = A_1 \sin(\omega t) \hat{i} \quad \vec{y} = A_2 \sin(\omega t + \phi) \hat{j}$$

When $\phi = 0$	When $\phi = \pi$	When $\phi = \frac{\pi}{2}$	When $\phi \neq 0, \frac{\pi}{2}, \pi$
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- (3) $|F| \propto |x|$ $x = A \sin(\omega t + \phi)$

Time Period & Frequency $T = \frac{2\pi}{\omega}$ $f = \frac{1}{T} = \frac{\omega}{2\pi}$

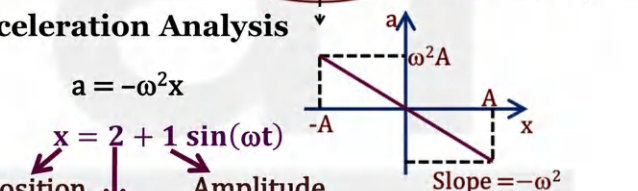
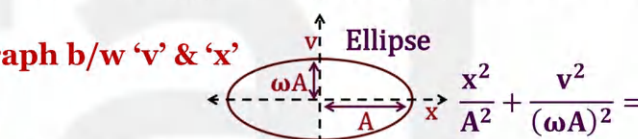
Velocity Analysis $x = A \sin(\omega t + \phi)$

$$v = \frac{dx}{dt} = A\omega \cos(\omega t + \phi)$$

$$v = \omega \sqrt{A^2 - x^2}$$

Max velocity $v_{max} = \omega A$ at $x = 0$ (Mean Position)

Min velocity $v_{min} = 0$ at $x = \pm A$ (Extreme Position)



Position eq^m. position $x = 2 + 1 \sin(\omega t)$

Amplitude

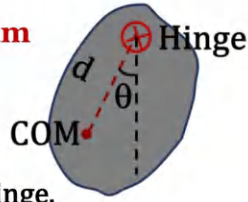
Physical Pendulum

$$T = 2\pi \sqrt{\frac{I}{mgd}}$$

I : MOI of system about hinge.

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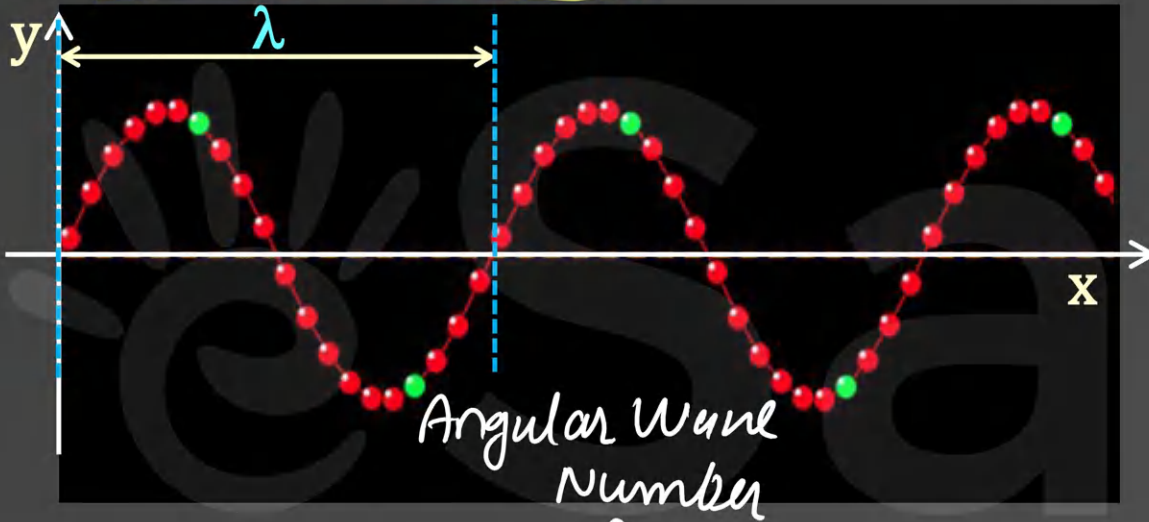
Wave on String

Superfast Revision

Sinusoidal Wave Equation



$$y = A \sin(\omega t - kx + \phi)$$



Each Particle doing SHM

$$T = \frac{2\pi}{\omega} \quad f = \frac{\omega}{2\pi}$$

$$v_w = f \lambda$$

$$\lambda = \frac{2\pi}{k}$$

$$; k = \frac{2\pi}{\lambda}$$

Velocity of wave

$$v_w = - \frac{\text{Coefficient of } t}{\text{Coefficient of } x}$$

$$y = A \sin(kx - \omega t) \quad v_w = - \frac{-\omega}{k} = \frac{\omega}{k}$$

Wave travelling in + dir.

$$y = A \sin(kx + \omega t) \quad v_w = - \frac{\omega}{k} = - \frac{\omega}{k}$$

Wave travelling in - dir.

Relation Between Particle Velocity And Wave Velocity



$$v_p = -v_w \left(\frac{\partial y}{\partial x} \right)$$



Slope of the string at point x.



Velocity of Wave on String



Tension T

μ

$$v_w = \sqrt{\frac{T}{\mu}}$$

$\mu =$ mass per unit length

Linear Mass Density

Stress

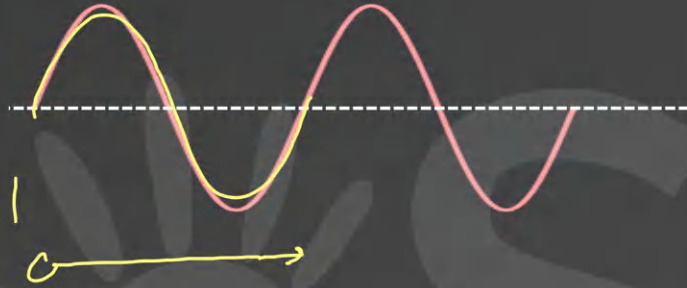
$\rho \rightarrow$ Density

$$v_w = \sqrt{\frac{T}{\mu}}$$

$$v_w = \sqrt{\frac{\text{Stress}}{\rho}}$$



Power Transmission in Travelling Wave on String



$$\langle P \rangle = \frac{1}{2} \underbrace{\sqrt{T\mu}}_{\text{Property of medium}} \underbrace{A^2 \omega^2}_{\text{Property of Source}}$$

Energy of string of one wave length

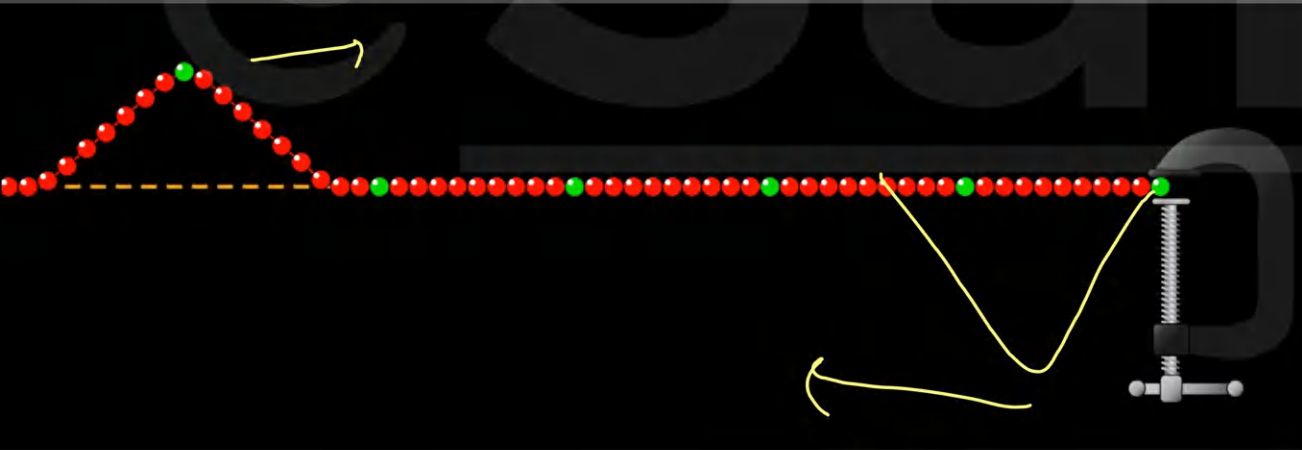
$$E = \frac{1}{2} \lambda \mu A^2 \omega^2$$

$$\langle P \rangle \text{ Time Per} = \text{Energy}$$

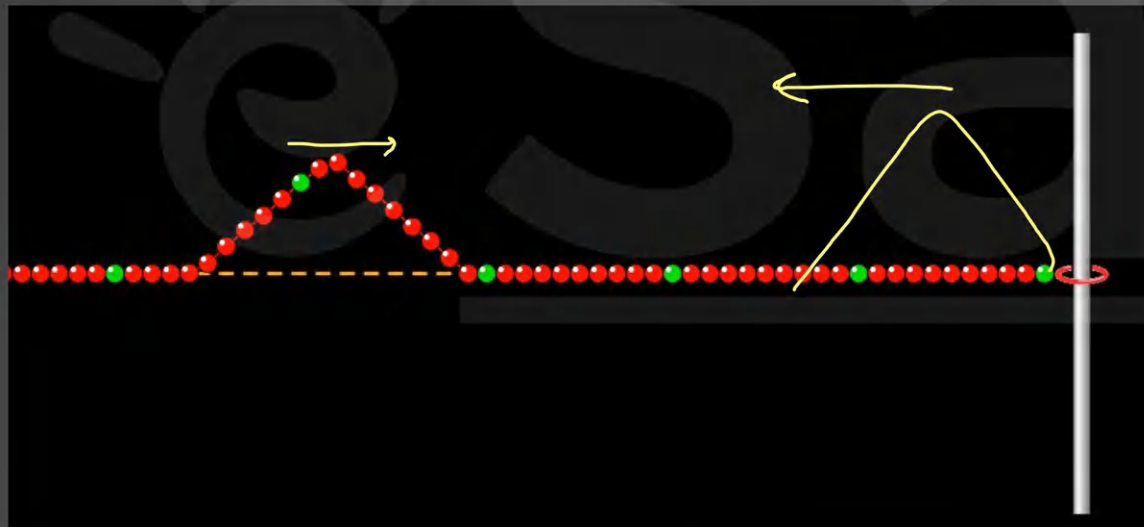


Reflection from Fixed End

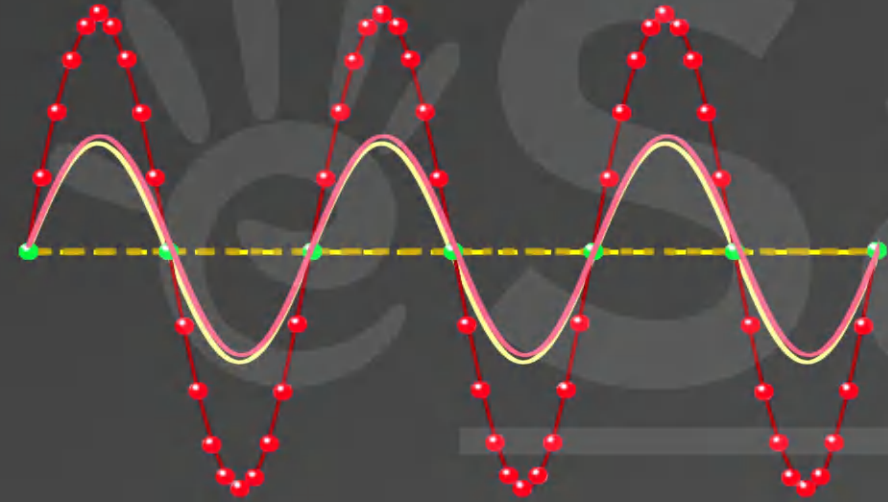
Due to reflection from fixed end
shape of the pulse gets inverted.



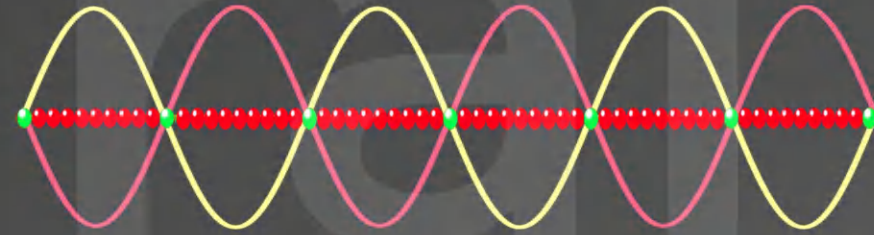
Reflection from Free End



Constructive Interference



Destructive Interference

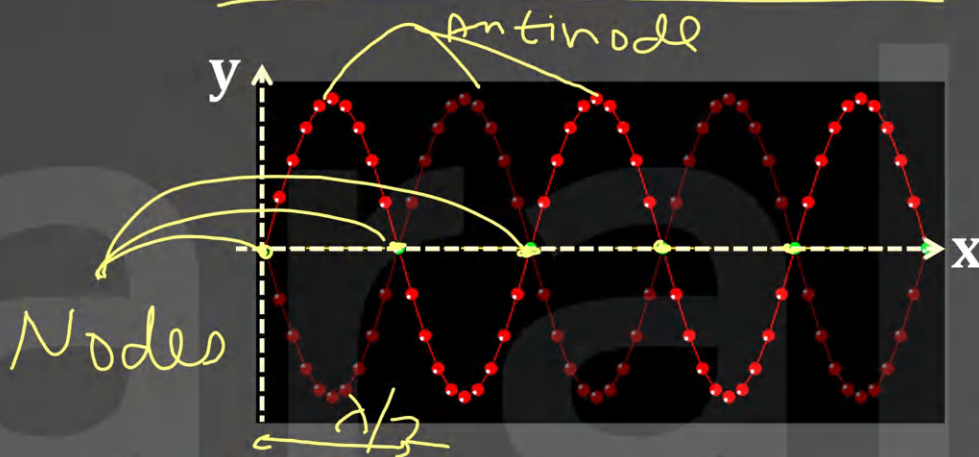


Standing Waves

When two waves of same amplitude, same frequency but moving in opposite direction interfere with each other then formation of **Standing Waves** takes place.

Distance between adjacent nodes is $\frac{\lambda}{2}$ & this portion of string is called a loop.

$$y_{\text{res}} = 2A \sin(kx) \cos(\omega t)$$



All the particles perform SHM of same frequency as of original component waves.

Nodes & Antinodes

$$y = 2A \sin(\underline{kx} + \phi_1) \sin(\underline{\omega t} + \phi_2)$$

Coefficient of $x = k$

Wavelength of component waves = $\frac{2\pi}{k}$

Coefficient of $t = \omega$

Time period of SHM of particle = $\frac{2\pi}{\omega}$

General Equation of Standing Wave



$$y = 2A \sin(kx + \phi_1) \sin(\omega t + \phi_2)$$

For ^{Anti} Nodes:

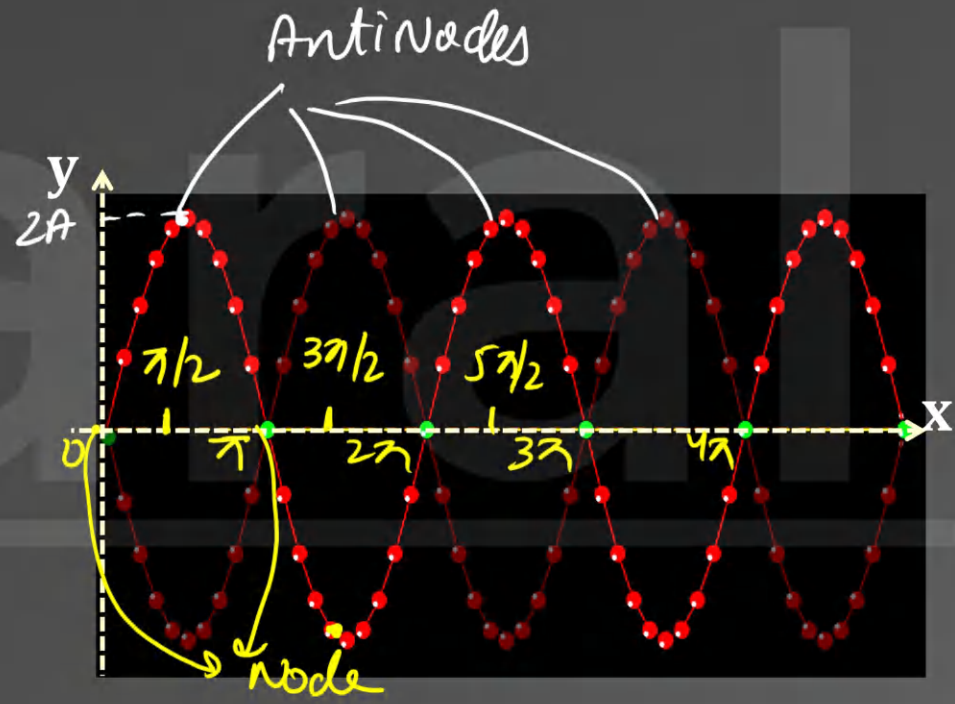
$$\sin(kx + \phi_1) = \pm 1$$

$$(kx + \phi_1) = \left(n + \frac{1}{2}\right) \pi$$

For ~~Anti~~ nodes:

$$\sin(kx + \phi_1) = 0$$

$$kx + \phi_1 = n\pi$$

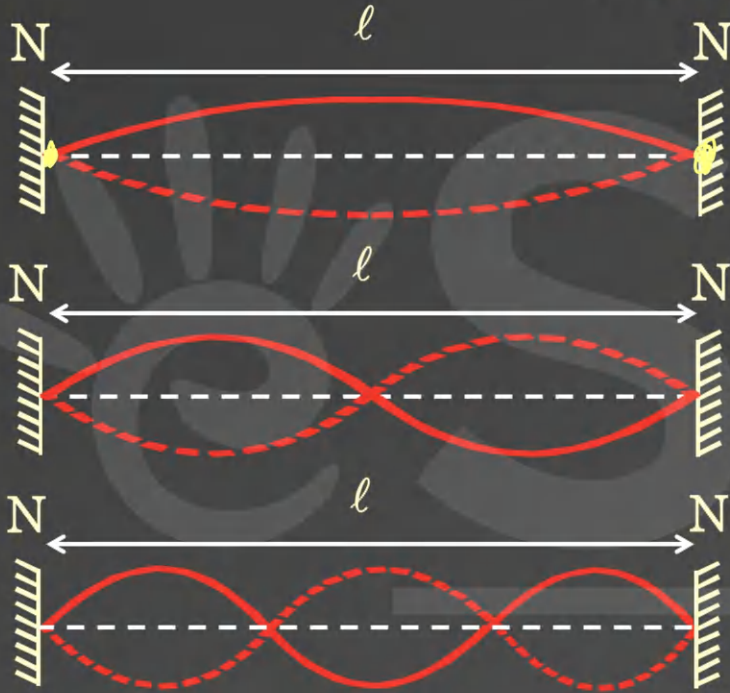


Normal Modes



String Fixed at Both Ends

$$f = \frac{v}{\lambda}$$



$$\frac{\lambda}{2} = l \quad f_0 = \frac{v}{2l}$$

Fundamental Frequency

$$\frac{2\lambda}{2} = l \quad f = \frac{2v}{2l}$$

2nd Harmonic
1st Overtone

$$\frac{3\lambda}{2} = l \quad f = \frac{3v}{2l}$$

3rd Harmonic
2nd Overtone

$$\frac{n\lambda}{2} = l \quad f = \frac{nv}{2l} \quad n^{\text{th}} \text{ Harmonic } (n-1)^{\text{th}} \text{ Overtone}$$



String Fixed at Both Ends

$$(1) \frac{n\lambda}{2} = \ell$$

$$(2) f = \frac{nv}{2\ell}$$

$$(3) f = \frac{n}{2\ell} \sqrt{\frac{T}{\mu}}$$

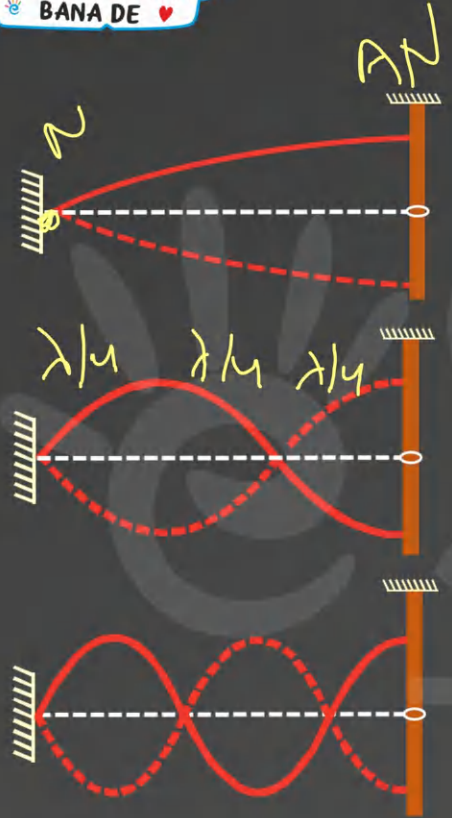
$$(4) f = n f_0$$

For fundamental frequency, $n = 1$

Normal Modes



String Fixed at One End & Free at Other



$$\frac{\lambda}{4} = \ell \quad f = \frac{v}{4\ell}$$

Fundamental Frequency

$$\frac{3\lambda}{4} = \ell \quad f = \frac{3v}{4\ell}$$

3rd Harmonic
1st Overtone

$$\frac{5\lambda}{4} = \ell \quad f = \frac{5v}{4\ell}$$

5th Harmonic
2nd Overtone

$$\frac{(2n + 1)\lambda}{4} = \ell \quad f = \frac{(2n + 1)v}{4\ell} \quad (2n + 1) \text{ Harmonic} \quad n^{\text{th}} \text{ Overtone}$$

For Node

For Antinode

$$\underline{KE = 0}$$

$$\underline{PE = 0}$$

Power transmission through node & antinode is zero. So, energy of one loop (even half loop) remains conserved.

QUIZ TIME

Interference of Waves



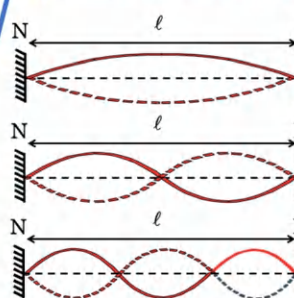
Constructive Interference

Destructive Interference

$$\lambda = 2\ell$$

$$f = \frac{v}{2\ell}$$

Normal Modes String Fixed at Both Ends



1

Fundamental Frequency (1) $\frac{n\lambda}{2} = \ell$

$\frac{2\lambda}{2} = \ell \quad f = \frac{2v}{2\ell}$

2nd Harmonic 1st Overtone (2) $f = \frac{nv}{2\ell}$

$\frac{3\lambda}{2} = \ell \quad f = \frac{3v}{2\ell}$

3rd Harmonic 2nd Overtone (3) $f = \frac{n}{2\ell} \sqrt{\frac{T}{\mu}}$

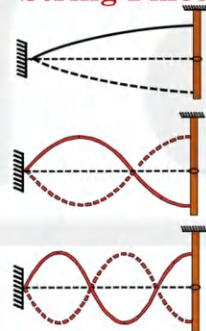
$$\frac{n\lambda}{2} = \ell \quad f = \frac{nv}{2\ell}$$

n^{th} Harmonic $(n-1)^{\text{th}}$ Overtone (4) $f = n f_0$

For fundamental frequency, $n = 1$

Wave on String

String Fixed at One End & Free at Other



2

Fundamental Frequency

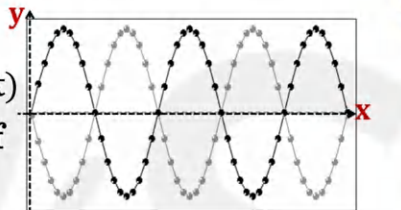
$\frac{3\lambda}{4} = \ell \quad f = \frac{3v}{4\ell}$

3rd Harmonic 1st Overtone

$\frac{5\lambda}{4} = \ell \quad f = \frac{5v}{4\ell}$

5th Harmonic 2nd Overtone

$\frac{(2n+1)\lambda}{4} = \ell \quad f = \frac{(2n+1)v}{4\ell}$ $(2n+1)$ Harmonic n^{th} Overtone



$$y_{\text{res}} = 2A \sin(kx) \cos(\omega t)$$

$$v_p = \frac{\partial y}{\partial t} = \omega \sqrt{A^2 - y^2}$$

$$a_p = \frac{\partial^2 y}{\partial t^2} = -\omega^2 y$$

Energy in Standing Wave

For Node
 KE = 0
 $\frac{\partial y}{\partial t} = 0$
 $P_{\text{Node}} = 0$

For Antinode
 PE = 0
 $\frac{\partial y}{\partial x} = 0$
 $P_{\text{Antinode}} = 0$

Power transmission through node & antinode is zero. So, energy of one loop (even half loop) remains conserved.

Standing Waves

$$y_{\text{res}} = 2A \sin(kx) \cos(\omega t)$$

For $x = x_0$ Equation of Motion

$$y = 2A \sin(kx_0) \cos(\omega t)$$

$$y = A' \cos(\omega t)$$

SHM

For Nodes - Amplitude = 0

$$\sin(kx + \phi_1) = 0$$

$$kx + \phi_1 = n\pi$$

For Antinodes - Amplitude = max

$$\sin(kx + \phi_1) = \pm 1$$

$$(kx + \phi_1) = \left(n + \frac{1}{2}\right)\pi$$

Interference of Waves



Constructive Interference

Destructive Interference

Standing Waves

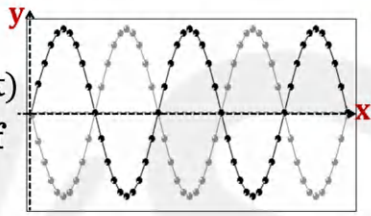
$$y_{res} = 2A \sin(kx) \cos(\omega t)$$

For $x = x_0$ Equation of Motion

$$y = 2A \sin(kx_0) \cos(\omega t)$$

$$y = A' \cos(\omega t)$$

SHM



$$y_{res} = 2A \sin(kx) \cos(\omega t)$$

$$v_p = \frac{\partial y}{\partial t} = \omega \sqrt{A^2 - y^2}$$

$$a_p = \frac{\partial^2 y}{\partial t^2} = -\omega^2 y$$

For Nodes - Amplitude = 0

$$\sin(kx + \phi_1) = 0$$

$$kx + \phi_1 = n\pi$$

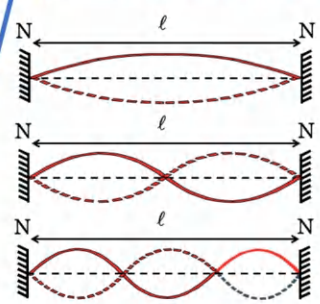
For Antinodes - Amplitude = max

$$\sin(kx + \phi_1) = \pm 1$$

$$(kx + \phi_1) = \left(n + \frac{1}{2}\right)\pi$$

Wave on String

Normal Modes String Fixed at Both Ends



$$\frac{\lambda}{2} = \ell \quad f_0 = \frac{v}{2\ell}$$

Fundamental Frequency (1) $\frac{n\lambda}{2} = \ell$

$$\frac{2\lambda}{2} = \ell \quad f = \frac{2v}{2\ell}$$

2nd Harmonic 1st Overtone (2) $f = \frac{nv}{2\ell}$

$$\frac{3\lambda}{2} = \ell \quad f = \frac{3v}{2\ell}$$

3rd Harmonic 2nd Overtone (3) $f = \frac{n}{2\ell} \sqrt{\frac{T}{\mu}}$

$$\frac{n\lambda}{2} = \ell \quad f = \frac{nv}{2\ell}$$

n^{th} Harmonic $(n-1)^{\text{th}}$ Overtone (4) $f = n f_0$

For fundamental frequency, $n = 1$

Energy in Standing Wave

For Node

$$KE = 0$$

$$\frac{\partial y}{\partial t} = 0$$

$$P_{\text{Node}} = 0$$

For Antinode

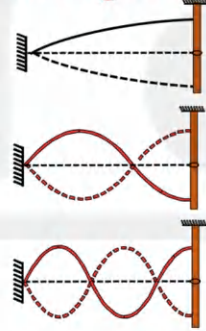
$$PE = 0$$

$$\frac{\partial y}{\partial x} = 0$$

$$P_{\text{Antinode}} = 0$$

Power transmission through node & antinode is zero. So, energy of one loop (even half loop) remains conserved.

String Fixed at One End & Free at Other



$$\frac{\lambda}{4} = \ell \quad f = \frac{v}{4\ell}$$

Fundamental Frequency

$$\frac{3\lambda}{4} = \ell \quad f = \frac{3v}{4\ell}$$

3rd Harmonic 1st Overtone

$$\frac{5\lambda}{4} = \ell \quad f = \frac{5v}{4\ell}$$

5th Harmonic 2nd Overtone

$$\frac{(2n+1)\lambda}{4} = \ell \quad f = \frac{(2n+1)v}{4\ell}$$

$(2n+1)$ Harmonic n^{th} Overtone

→ Doppler Effect

Sound Wave

Superfast Revision



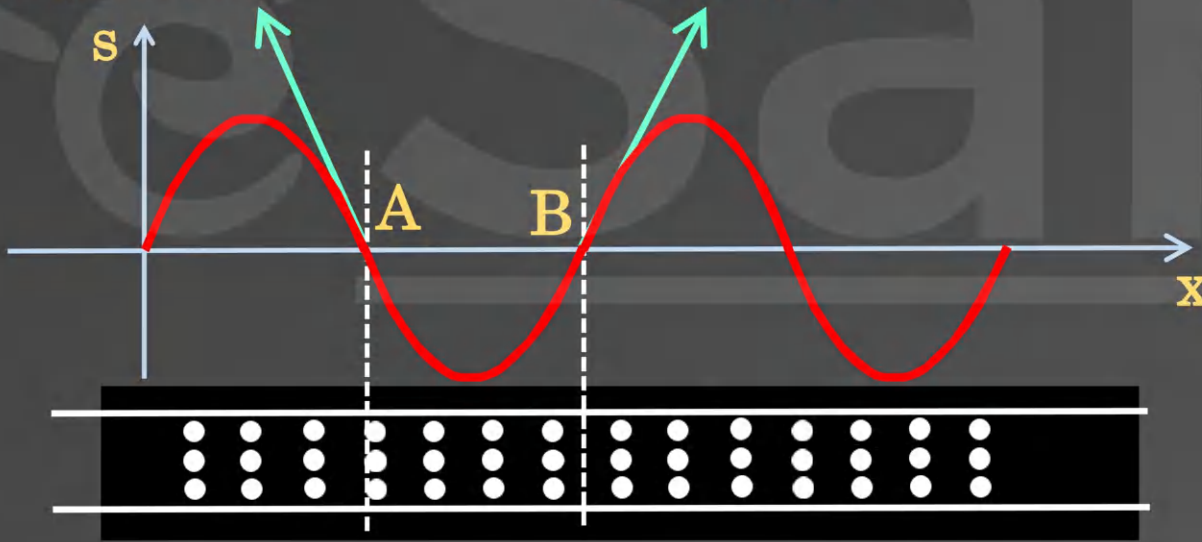
Equation of Sound Wave



$$s = s_0 \sin (\pm \omega t \pm kx + \phi)$$

Max Compressive Stress
Max. Density, Pressure
Compression

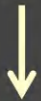
Max Tensile Stress
Min. Density, Pressure
Rarefaction



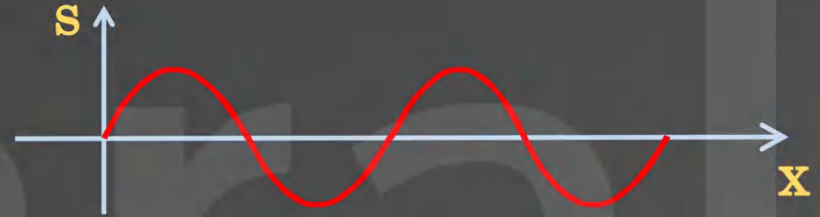
$$s = s_0 \sin (\omega t - kx + \phi)$$

$$v_w = - \frac{\text{Coefficient of } t}{\text{Coefficient of } x} = \frac{\omega}{k}$$

$$v_p = -v_w \left(\frac{\partial s}{\partial x} \right)$$



Velocity of particle



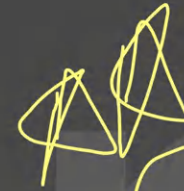
Variation of Excess Pressure in Gas Due to Propagation of Longitudinal Wave

$$p = -B \left(\frac{\partial s}{\partial x} \right)$$

Excess pressure

$$s = s_0 \sin(\omega t - kx)$$

$$p = p_0 \cos(\omega t - kx)$$



$$|p_0| = |Bks_0|$$

Amplitude of excess pressure



Velocity of Sound Wave in Gas



$$v_w = \sqrt{\frac{B}{\rho}}$$

$B \rightarrow$ Bulk modulus
 $\rho \rightarrow$ Density

$$v_w = \sqrt{\frac{\gamma P}{\rho}}$$

$$v_w = \sqrt{\frac{\gamma RT}{M_0}}$$

(T is in Kelvin)

On increasing P if T is constant
 v_w will not change

At same T if humidity increases,
 v_w increases ($\because M_0 \downarrow$)





$$v_w = \sqrt{\frac{\gamma RT}{M_0}}$$

For a small change, ΔT

$$\frac{\Delta v_w}{v_w} = \frac{1}{2} \frac{\Delta T}{T}$$

$\%$ change in $v_w = \frac{1}{2} \% \text{ in } T$



$$\sqrt{\frac{T}{\mu}}$$

Velocity of
wave on
string

$$\sqrt{\frac{B}{\rho}}$$

Velocity of
wave in gas

$$\sqrt{\frac{Y}{\rho}}$$

Velocity of
wave in thin
solid rod

Elastic Property of medium
Inertial Property of medium



Intensity in Sound Waves



$$\langle I \rangle = \frac{1}{2} \underbrace{\sqrt{B\rho}}_{\text{Property of medium}} \underbrace{s_0^2 \omega^2}_{\text{Property of source}}$$

**Property
of medium**

**Property
of source**

eSaraal





Pitch

(Dominant Frequency)

Low Frequency



Low Pitch

High Frequency



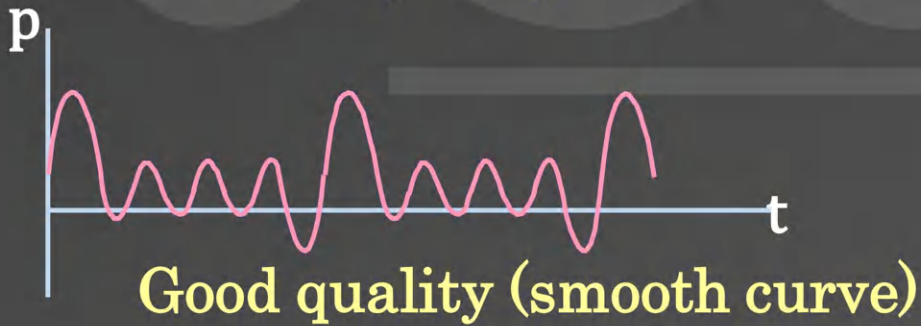
High Pitch





Quality

(Waveform of Sound wave)





Loudness
(Intensity)

$$\text{Sound level (SL)} = 10 \log_{10} \left(\frac{I}{I_0} \right)$$

measured in
decibel (dB)

$$I_0 = 10^{-12} \frac{\text{Watt}}{\text{m}^2}$$

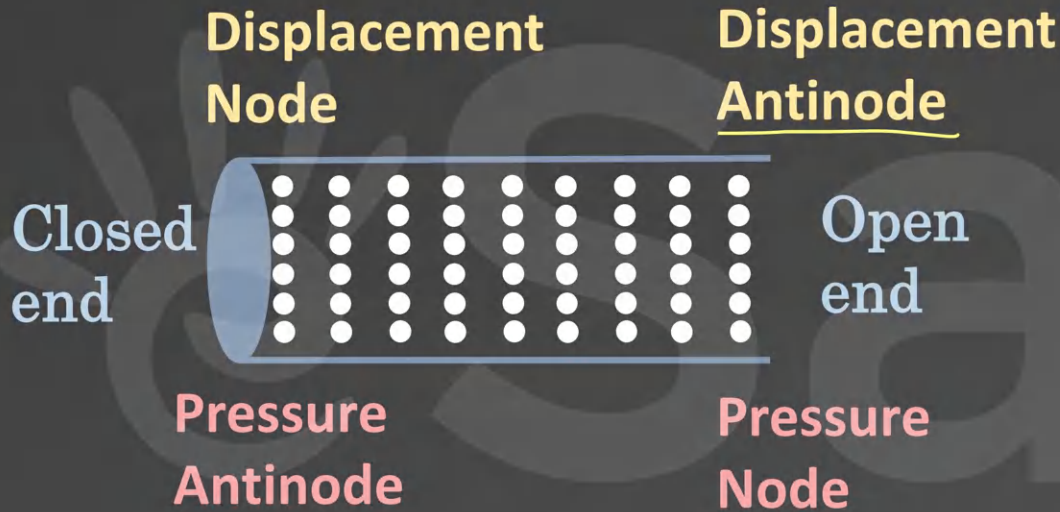
Minimum audible intensity

$$\text{Intensity} = \frac{\text{Power}}{\text{Area}}$$



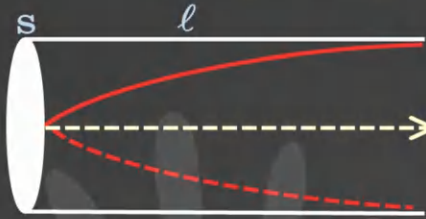


Standing Wave Inside an Organ Pipe Closed at One End



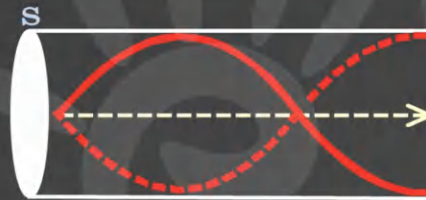


Standing Wave Inside an Organ Pipe Closed at One End



$$\frac{\lambda}{4} = \ell \quad f = \frac{1v}{4\ell}$$

Fundamental frequency



$$\frac{3\lambda}{4} = \ell \quad f = \frac{3v}{4\ell}$$

3rd Harmonic
1st overtone



$$\frac{5\lambda}{4} = \ell \quad f = \frac{5v}{4\ell}$$

5th Harmonic
2nd overtone

$$\frac{(2n + 1)\lambda}{4} = \ell$$

$$f = \frac{(2n + 1)v}{4\ell}$$

(2n + 1)th Harmonic
nth overtone





Standing Wave Inside an Organ Pipe Closed at Both End



Displacement
Antinode

Displacement
Antinode

Open
end



Open
end

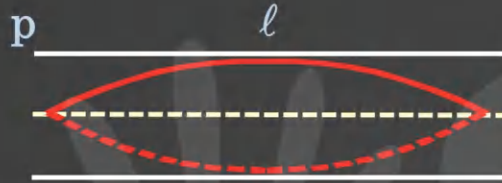
Pressure
Node

Pressure
Node



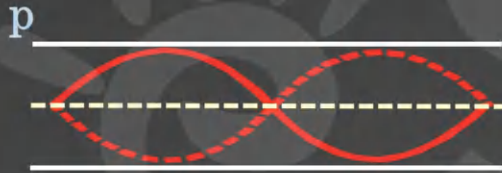


Standing Wave Inside an Organ Pipe Open at Both End



$$\frac{\lambda}{2} = l \quad f_0 = \frac{1v}{2l}$$

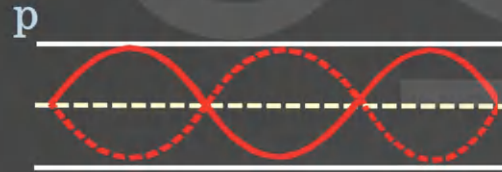
Fundamental frequency



$$\frac{2\lambda}{2} = l \quad f = \frac{2v}{2l}$$

2nd Harmonic

1st overtone



$$\frac{3\lambda}{2} = l \quad f = \frac{3v}{2l}$$

3rd Harmonic

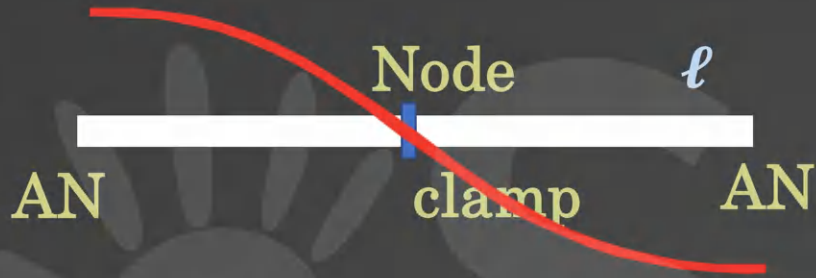
2nd overtone

$$\frac{n\lambda}{2} = l \quad f = \frac{nv}{2l} \quad n^{\text{th}} \text{ Harmonic} \quad (n-1)^{\text{th}} \text{ overtone}$$





Standing Wave in Solids



$$\sqrt{\frac{B}{\rho}}$$

$$\sqrt{\frac{Y}{\rho}}$$

$$\frac{\lambda}{2} = l \quad f = \frac{1}{2l} \sqrt{\frac{Y}{\rho}}$$

fundamental mode





Standing Wave in Solids

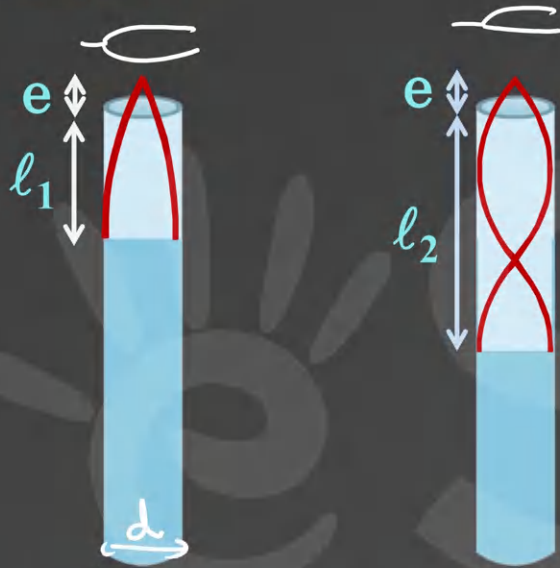


$$\frac{3\lambda}{2} = l \quad f = \frac{3}{2l} \sqrt{\frac{Y}{\rho}} \quad f_0 = \frac{1}{2l} \sqrt{\frac{Y}{\rho}}$$

1st overtone, 3rd harmonic



Resonance Tube Method to Calculate Speed of Sound in Air



Pressure node forms a bit outside open end.

1st resonance

2nd resonance

$$\frac{\lambda}{4} = l_1 + e$$

$$\frac{3\lambda}{4} = l_2 + e$$

$$v = f\lambda$$

$$v = 2f(l_2 - l_1)$$

$$e = 0.3d$$

diameter of tube



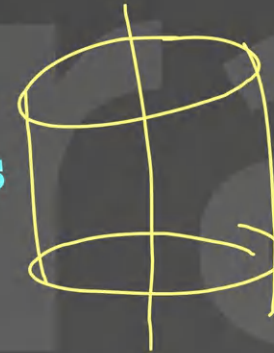
It is the locus of points which are vibrating in same phase.

Point source

Line source

Spherical wavefronts

Cylindrical wavefronts



Planar wavefronts



Change in frequency observed due to motion of both source & observer

Doppler's Effect



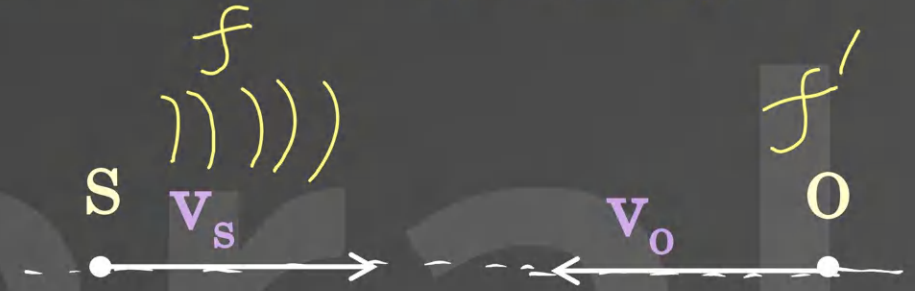
$$f' = \left(\frac{v_w + v_o}{v_w - v_s} \right) f$$

where

f = frequency produced by source

f' = frequency observed by observer

v_w = velocity of wave in medium



v_o = component of velocity of observer in medium towards source

v_s = component of velocity of source in medium towards observer



TRICK

$v_o \searrow v_s$ will be +ve

if they reduce $\frac{f'}{f}$
else -ve

$$f' = \left(\frac{v_w + v_o}{v_w - v_s} \right) f$$

$v_w = 300 \text{ m/s}$

1.



$$f' = \left[\frac{300 + (+20)}{300 - (+10)} \right] f$$

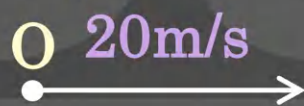
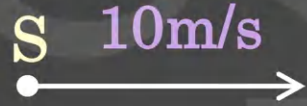
$$f' = \left(\frac{v_w + v_o}{v_w - v_s} \right) f$$

$$\left(\frac{300 + (-20)}{300 - (+10)} \right) f$$

$$v_w = 300 \text{ m/s}$$

+ve

-ve



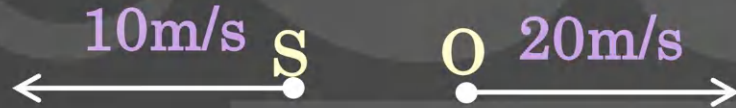
$$f' = \left[\frac{300 + (-20)}{300 - (+10)} \right] f$$

2.

$$f' = \left(\frac{v_w + v_o}{v_w - v_s} \right) f$$

$$v_w = 300 \text{ m/s}$$

3.

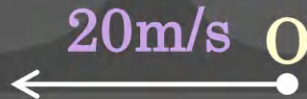
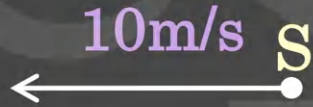


$$f' = \left[\frac{300 + (-20)}{300 - (-10)} \right] f$$

$$f' = \left(\frac{v_w + v_o}{v_w - v_s} \right) f$$

$$v_w = 300 \text{ m/s}$$

4.



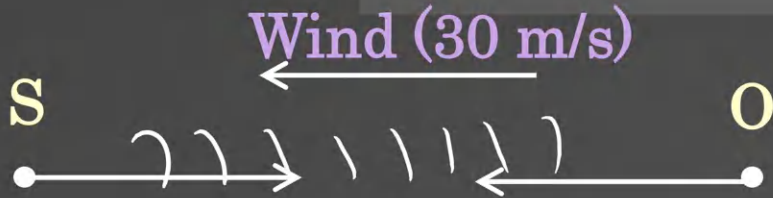
$$f' = \left[\frac{300 - (+20)}{300 - (-10)} \right] f$$

If wind is blowing

$$f' = \left(\frac{v_{\text{wave}} + v_0}{v_{\text{wave}} - v_S} \right) f \quad v_w = 300 \text{ m/s}$$



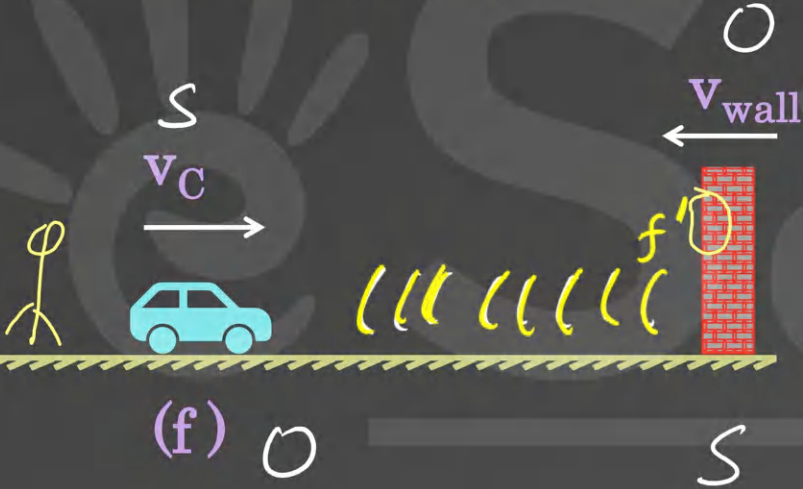
$$f' = \left(\frac{(v_{\text{wave}} + v_{\text{wind}}) + v_0}{(v_{\text{wave}} + v_{\text{wind}}) - v_S} \right) f$$



$$f' = \left(\frac{(v_{\text{wave}} - v_{\text{wind}}) + v_0}{(v_{\text{wave}} - v_{\text{wind}}) - v_S} \right) f$$

$$f_{\text{obs}} = \left(\frac{v_w + v_o}{v_w - v_s} \right) f_{\text{prod}}$$

TRICK दीवारों के गी काम होते



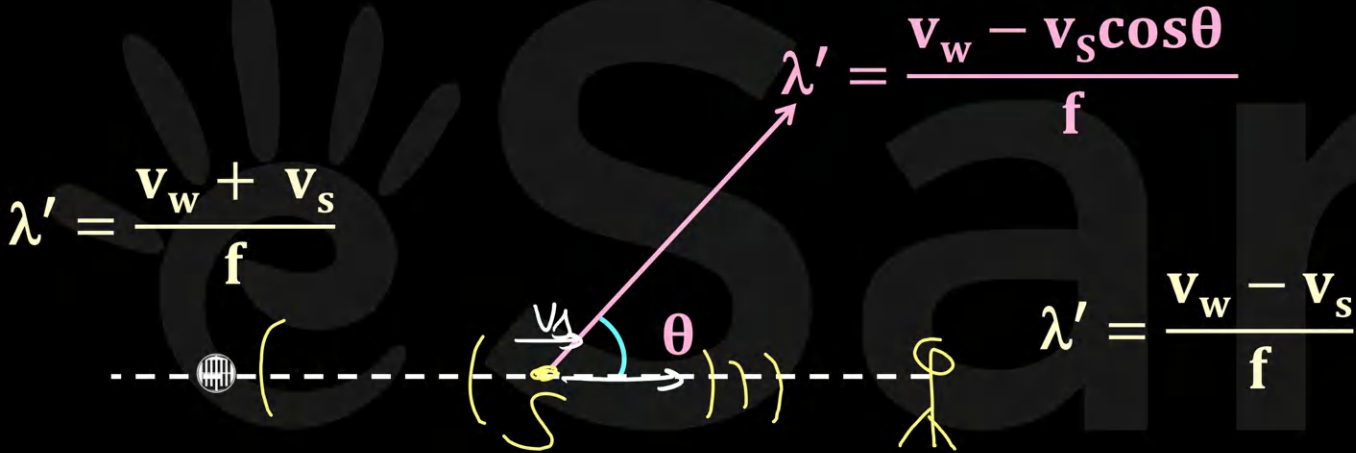
→ दीवारों के गी में ह होते

$$f' = \left[\frac{v_w + v_{\text{wall}}}{v_w - (v_c)} \right] f$$

$$f'' = \left[\frac{v_w + v_c}{v_w - (v_{\text{wall}})} \right] f'$$



Change in wavelength due to motion of a sound source



$$\lambda' = \frac{v_w + v_s}{f}$$

$$\lambda' = \frac{v_w - v_s \cos \theta}{f}$$

$$\lambda' = \frac{v_w - v_s}{f}$$

$$\lambda = \frac{v_w}{f}$$





$$p_1 = p_{10} \sin(kx - \omega t)$$

$$p_2 = p_{20} \sin(kx - \omega t + \phi)$$

Constructive Interference

$$(p_{res})_{max} = p_{10} + p_{20}$$

$$(I_{res})_{max} = (\sqrt{I_1} + \sqrt{I_2})^2$$

$$\Delta x = 0, \lambda, 2\lambda, 3\lambda \dots = n\lambda$$

Destructive Interference

$$(p_{res})_{min} = |p_{10} - p_{20}|$$

$$(I_{res})_{min} = (\sqrt{I_1} - \sqrt{I_2})^2$$

$$\Delta x = 0.5\lambda, 1.5\lambda, 2.5\lambda \dots = \left(n + \frac{1}{2}\right)\lambda$$





Interference of waves having frequency slightly different from each other produces **beats**.



504Hz 500Hz

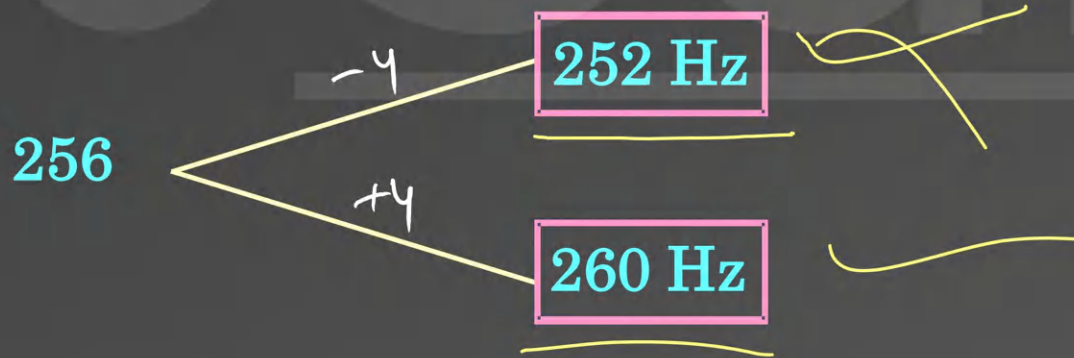
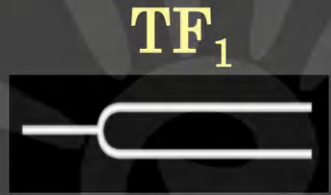
$$= 4 \text{ Hz}$$

$$\text{Beat frequency} = \Delta f = f_1 - f_2$$



Q) A TF_1 has frequency $f = 256$ Hz. It produces beats of 4 Hz with TF_2 . What could be the frequency f of TF_2 ?

Sol.

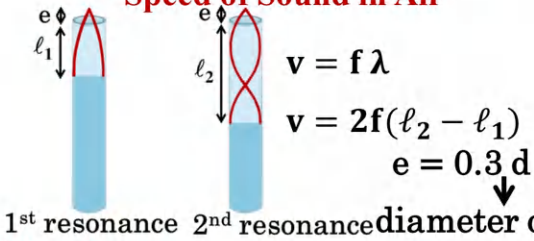


Key Points

- On applying wax on prongs of TF, its frequency decreases.
- On filling prongs of TF, its frequency increases.

QUIZ TIME

Resonance Tube Method to Calculate Speed of Sound in Air



Wavefront
 Point source
 Line source
 Cylindrical wavefronts
 Spherical wavefronts
 Planar wavefronts

Change in wavelength due to motion of a sound source

$$\lambda' = \frac{v_w \pm v_s}{f}$$

Change in frequency observed due to motion of both source & observer

$$f' = \left(\frac{v_w + v_o}{v_w - v_s} \right) f$$

If wind is blowing, take its effect also

Interference of Sound Waves

$$p_1 = p_{10} \sin(kx - \omega t)$$

$$p_2 = p_{20} \sin(kx - \omega t + \phi)$$

By Superposition Principle

$$(p_{res})^2 = p_{10}^2 + p_{20}^2 + 2 p_{10} p_{20} \cos \phi$$

$$I_{res} = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \phi \quad (I \propto p_0^2)$$

$$\frac{\lambda}{2} = \ell$$

Doppler f Formula

Beat frequency = **1**

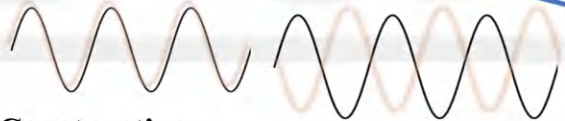
Sound Waves

Constructive Interference

$$(p_{res})_{max} = p_{10} + p_{20}$$

$$(I_{res})_{max} = (\sqrt{I_1} + \sqrt{I_2})^2$$

$$\Delta x = 0, \lambda, 2\lambda, 3\lambda \dots = n\lambda$$



Constructive Interference

Destructive Interference

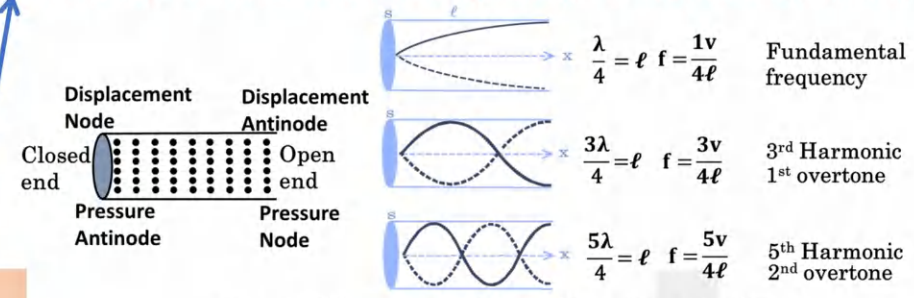
Destructive Interference

$$(p_{res})_{min} = |p_{10} - p_{20}|$$

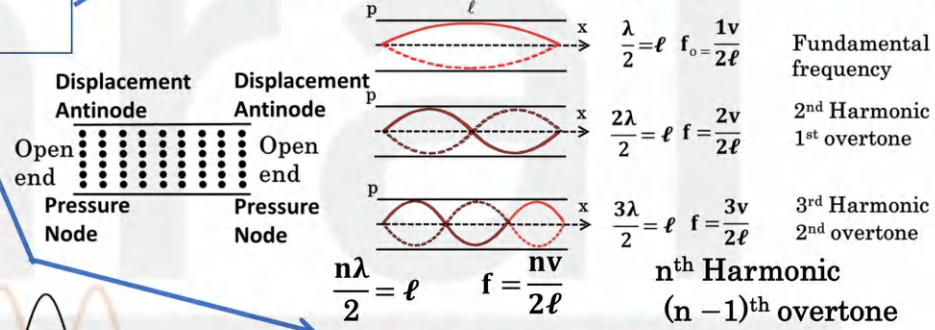
$$(I_{res})_{min} = (\sqrt{I_1} - \sqrt{I_2})^2$$

$$\Delta x = 0.5\lambda, 1.5\lambda, 2.5\lambda \dots = \left(n + \frac{1}{2}\right) \lambda$$

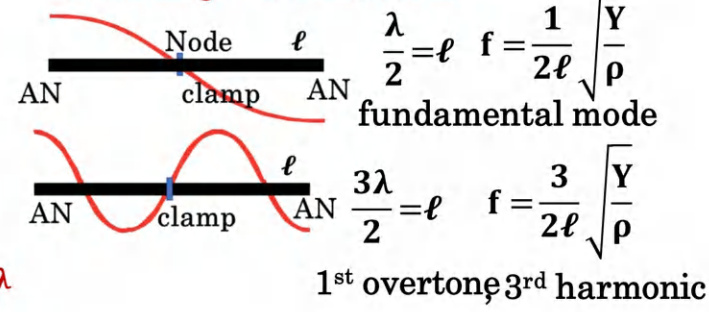
Standing Wave Inside an Organ Pipe Closed at One End



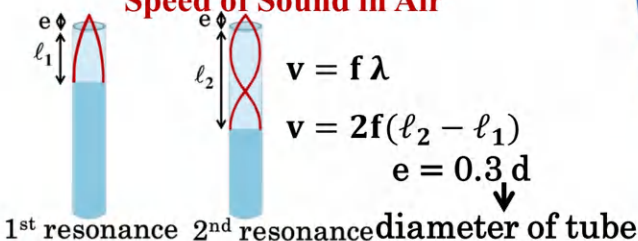
Standing Wave Inside an Organ Pipe Open at Both End



Standing Wave in Solids



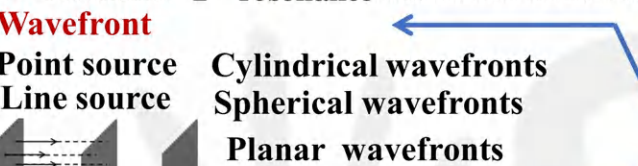
Resonance Tube Method to Calculate Speed of Sound in Air



$$v = f \lambda$$

$$v = 2f(l_2 - l_1)$$

$$e = 0.3d$$



Change in wavelength due to motion of a sound source

$$\lambda' = \frac{v_w \pm v_s}{f}$$

Change in frequency observed due to motion of both source & observer

$$f' = \left(\frac{v_w + v_o}{v_w - v_s} \right) f$$

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$$\frac{\lambda}{2} = \ell$$

$$f' = \left(\frac{v_w + v_o}{v_w - v_s} \right) f$$

Beat frequency = $\Delta f = f_1 - f_2$

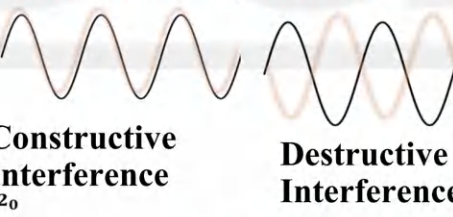
Sound Waves

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$$\Delta x = 0, \lambda, 2\lambda, 3\lambda \dots = n\lambda$$



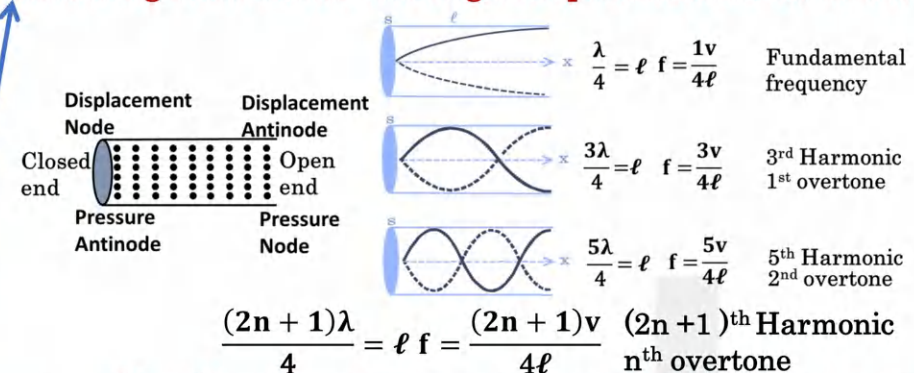
Destructive Interference

$$(p_{res0})_{min} = |p_{10} - p_{20}|$$

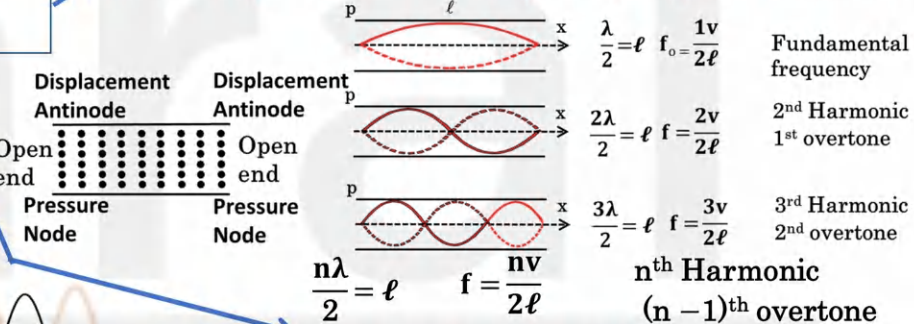
$$(I_{res})_{min} = (\sqrt{I_1} - \sqrt{I_2})^2$$

$$\Delta x = 0.5\lambda, 1.5\lambda, 2.5\lambda \dots = \left(n + \frac{1}{2}\right) \lambda$$

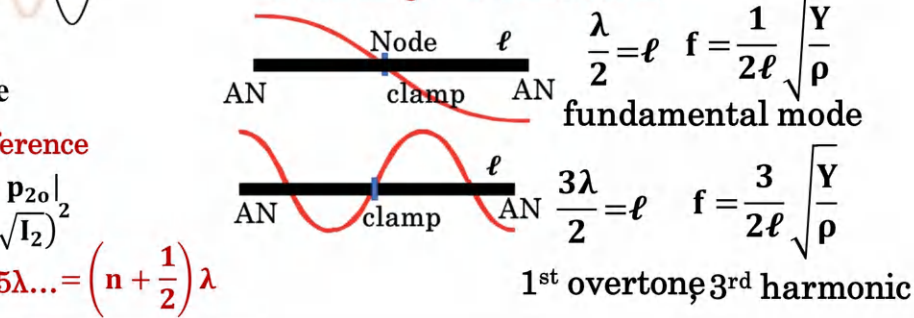
Standing Wave Inside an Organ Pipe Closed at One End



Standing Wave Inside an Organ Pipe Open at Both End



Standing Wave in Solids



Course Details

Lectures



Practice



Tests

Sheets

Prev. Yr.

Topic-Wise

Review

Study Plan

Doubt Solving

Mentorship

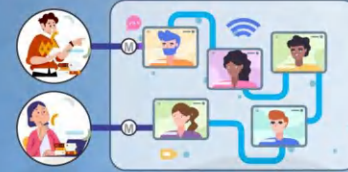


3 Layered Personalised Mentorship

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PERSONAL ACADEMIC
MENTOR



PROGRESS MENTOR
FOR TRACKING PROGRESS



LIVE MENTORSHIP SESSIONS

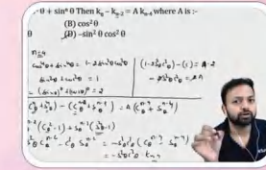


4 Layered DOUBT SOLVING

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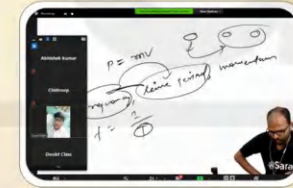
SOULTION OF PRACTICE SHEETS



DEDICATED DOUBT HOTLINE



LIVE DOUBT SOLVING CLASSES



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AIR-190
Apoorv Bansal

AIR-211
Vivek Kumar Singh

AIR-240
Shiva Ganesh Reddy

AIR-295
Shikhar Gupta

AIR-635
Chitraansh Pandey

AIR-669
Harsh Vijayvargiya

AIR-782
Param Shah

AIR-802
Loveneesh Lawaniya

AIR-263
Abhay Saini

AIR-323
Gaurav Kumawat

AIR-541
Divy Soni

AIR-821
Siddhant Sekhar

AIR-909
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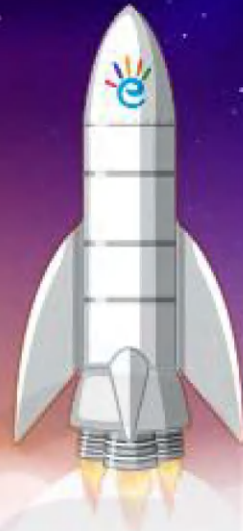
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