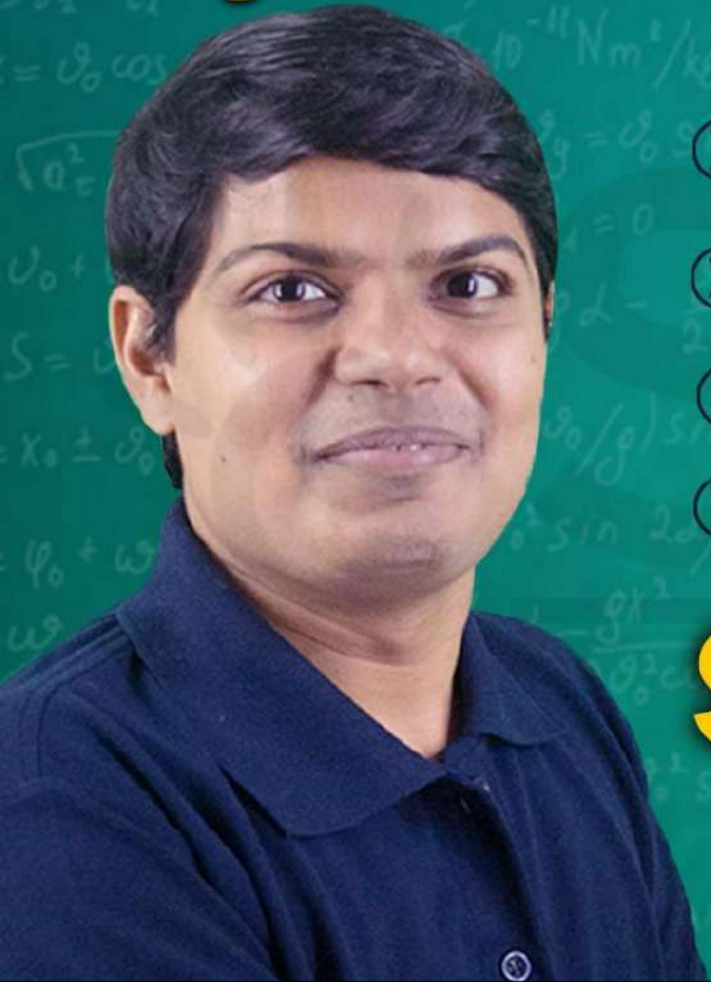


# Physics Mega Revision #5



- Ray Optics
- Wave Optics
- Optical Instruments
- Errors
- EM Waves

## Superfast Revision



### Welcome Students



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# Complete Physics Mega Revision Timetable

15 Feb

Electrostatics ✓  
Current electricity ✓  
Capacitor ✓

📁 **Surprise Gift** 📁

16 Feb

Calorimetry ✓  
Elasticity ✓  
Thermal Expansion ✓  
Heat Transfer ✓  
KTG ✓  
Thermodynamics ✓  
Fluid Mechanics ✓

17 Feb

Magnetic effect of current ✓  
Magnetism and matter ✓  
Emi ✓  
AC ✓

18 Feb

UD ✓  
Vector ✓  
Kinematics 1D ✓  
Kinematics 2D ✓  
NLM ✓  
Friction ✓  
Circular motion ✓  
Work power energy ✓  
COM ✓

19 Feb

Ray optics ✓  
Optical Instruments ✓  
Wave optics ✓  
EM Waves ✓  
Errors in measurement ✓

20 Feb

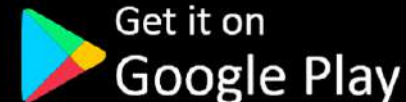
Rotation motion ✓  
Gravitation ✓  
SHM ✓  
Wave on string ✓  
Sound wave ✓

21 Feb

Atomic structure ✓  
Dual nature of radiation ✓  
X-rays ✓  
Nuclear physics ✓  
Radioactivity ✓  
Semi conductor ✓  
Communication system ✓



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## Saransh Gupta Sir

### eSaral Physics HoD

- IIT Bombay, CS
- AIR-41 IIT-JEE
- Air-71 AIEEE (JEE Main)
- AIR-4 NSO
- 1% In Top INPHO
- 8+ Years of Teaching Experience
- Mentored Lakhs of Students





## Prateek Gupta Sir eSara Chemistry Faculty

- **IIT Bombay, Metallurgy**
- **Online Creativity & Visualization Expert**
- **Mentored Lakhs of Students**



## N.K. Gupta Sir eSaral Math Faculty & Master Planner

- IIT Kanpur, Mechanical
- Ex Vice President & Academic Head, Allen, Kota
- Mentored many of **Rank 1 & Top 100** Students
- **30+** years of Teaching Experience
- **Mentored** over 3,00,000 Students



## Dr. Anshuman Agarwal eSaral Biology Faculty

- **MBBS, MD, FIPM**
- **AIR-196, AIPMT(NEET)**
- **ARR-46, RPMT**
- **NTSE Scholar**
- **Ex HoD Biology, Resonance, Kota**
- **10+ years of Teaching Experience**
- **Mentored over thousands of doctors**



## Dr. Kushika Taneja eSaral Biology Faculty

- **Ex-HoD Biology**, Pace IIT and Medical, Indore
- Biology faculty at Rao Academy, Kota
- **7+ years** of Teaching Experience
- **Mentored** over thousands of doctors

# ★ Today's Session Highlights ★

- **Admit Card Information**
- **Frequently Asked Topics of Each Chapter**
- **Quiz after each Topic** ★★







**Will a Donkey look like Zebra if  
Strips are put in front of Camera ?**



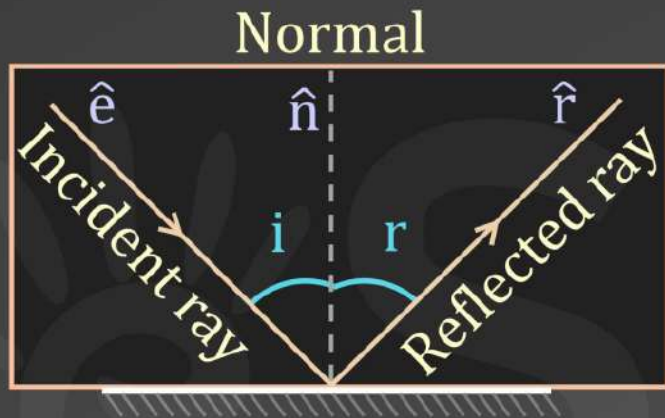


**NO. Donkey will be a Donkey  
but with less intensity.**



# Ray Optics

## Superfast Revision



Incident ray, reflected ray and normal lies in the same plane.

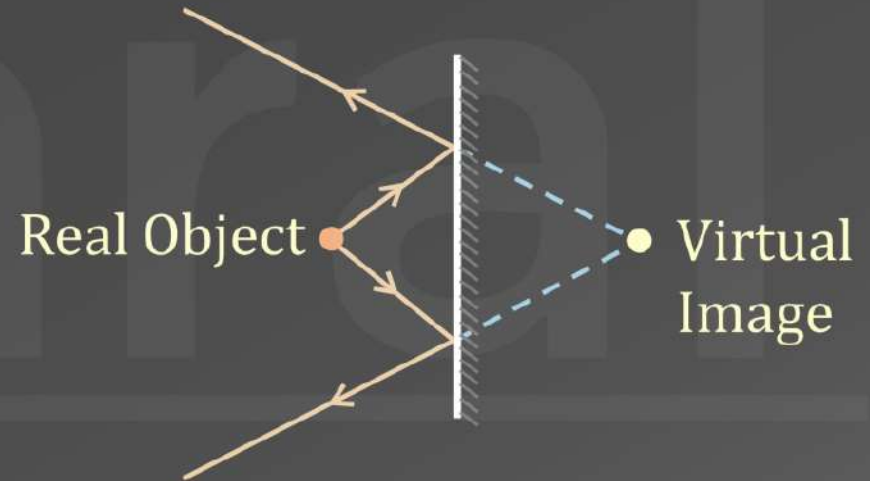
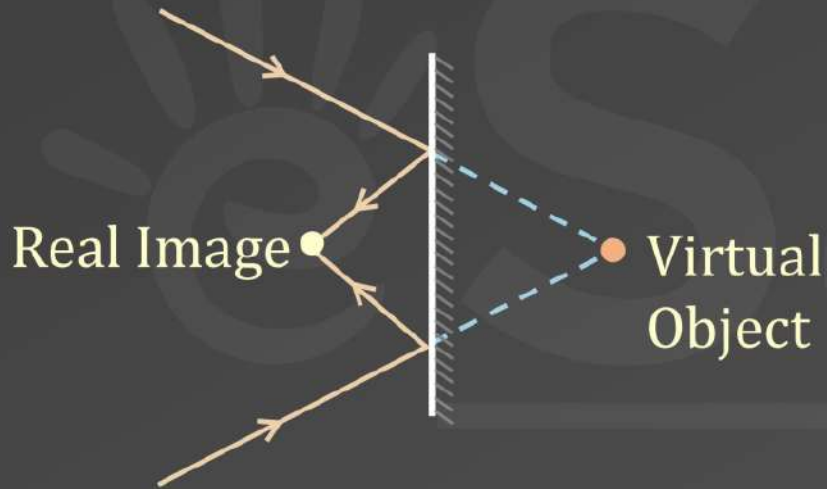
$$[\hat{e} \hat{r} \hat{n}] = 0$$

$$[\hat{e} \times \hat{r}] \cdot \hat{n} = 0$$

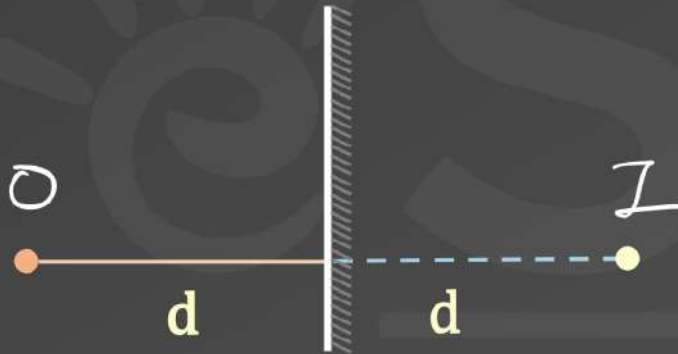
The angle of reflection is equal to the angle of incidence

$$\underline{\angle i = \angle r}$$

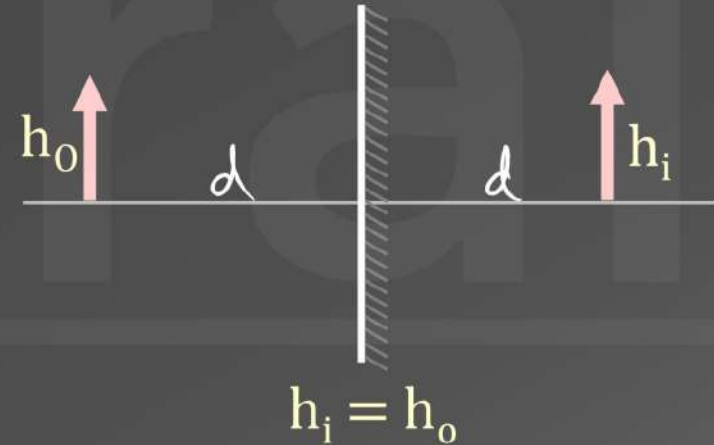
1. It forms Real Image of Virtual Object and Virtual Image of Real Object.



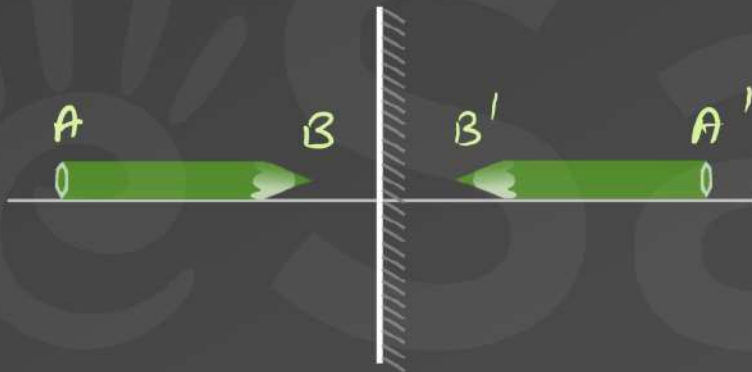
2. The distance of object from mirror is equal to the distance of image from the mirror.

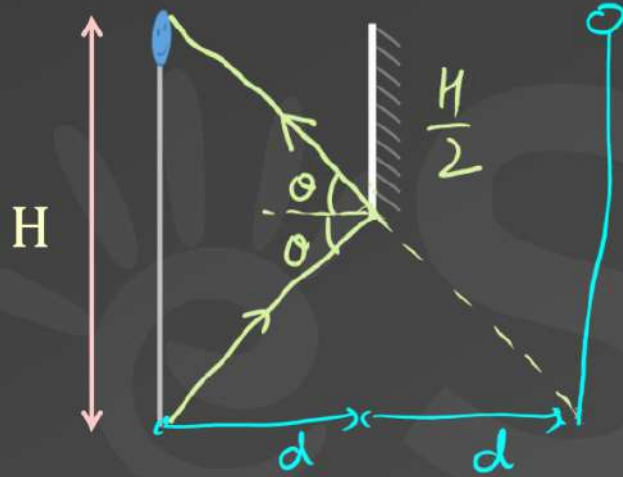


3. The size of the image is same as that of the object.



4. Image formed by Plane mirror is side-ways inverted.





Minimum size of a plane mirror  
required to see the full image of  
an observer is half the size of that  
observer.





$$(\vec{V}_O)_{\parallel} = (\vec{V}_I)_{\parallel}$$

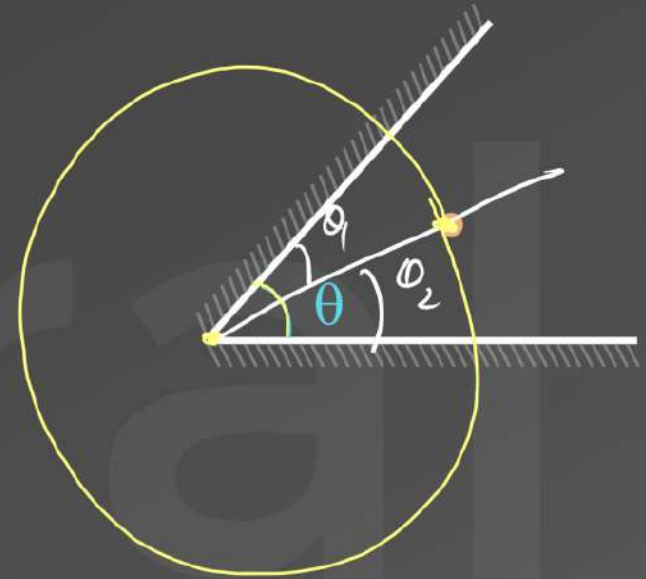
$$(\vec{V}_{O/M})_{\perp} = -(\vec{V}_{I/M})_{\perp}$$

# Mirrors at an Angle

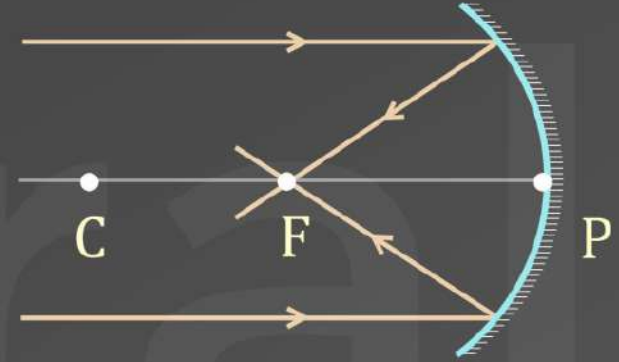


$$\frac{360}{\theta} = N = 8 \quad \theta = 45^\circ$$

Condition	No. of Images
If <u>N = Even Integer</u>	<u>N - 1</u>
If N = Odd Integer	
1. If object is on angle Bisector	<u>N - 1</u>
2. If Not	<u>N</u>
If <u>N ≠ Integer</u> ✕✕	Count Manually



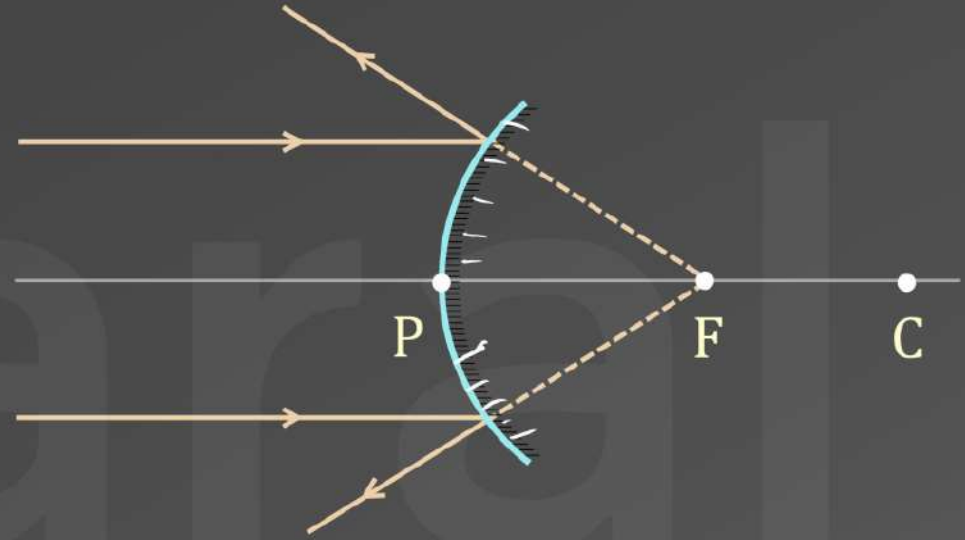
When a paraxial light beam parallel to the principle axis is incident on a mirror the reflected rays are converged at a point F on the principle axis of a concave mirror.



# Focus and Focal Length of a Mirror

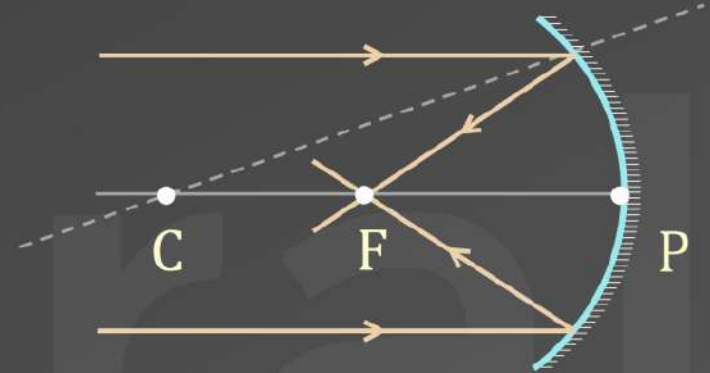


For convex mirror reflected rays appear to diverge from a point F on principle axis. The point F is called principal focus of the mirror.

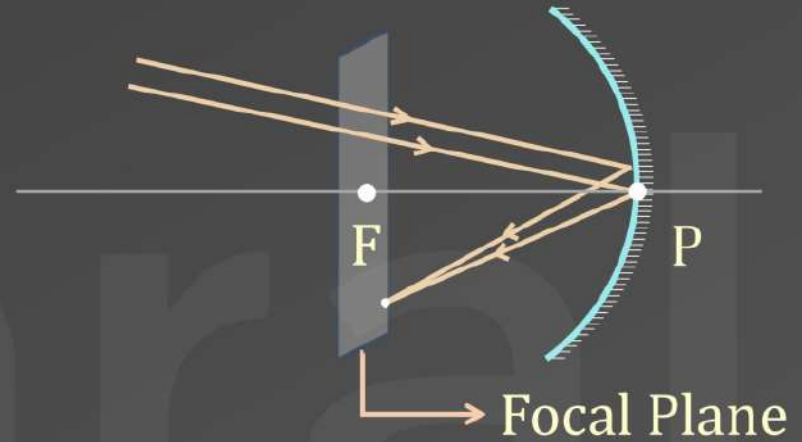


Focal length is the distance of focus from the pole.

$$f = \frac{R}{2}$$



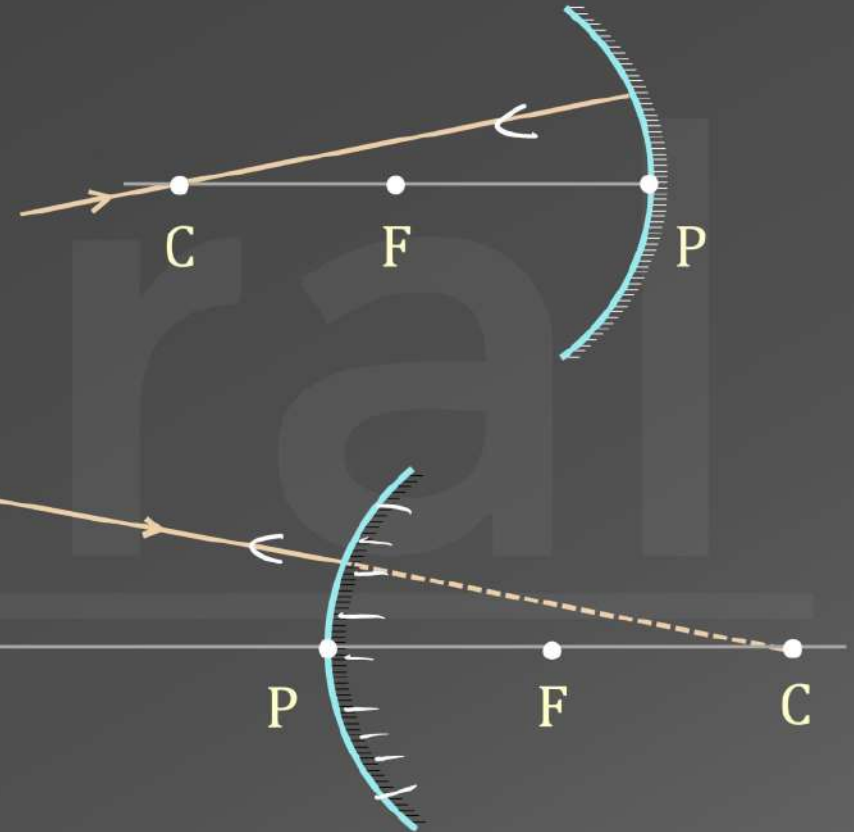
Focal Plane is the plane passing through focus and perpendicular to principal axis.



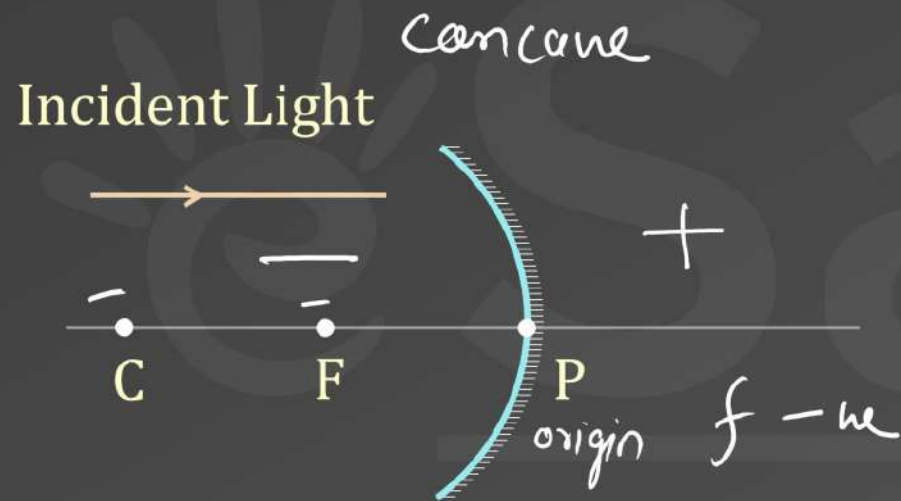
# Ray Tracing Diagram



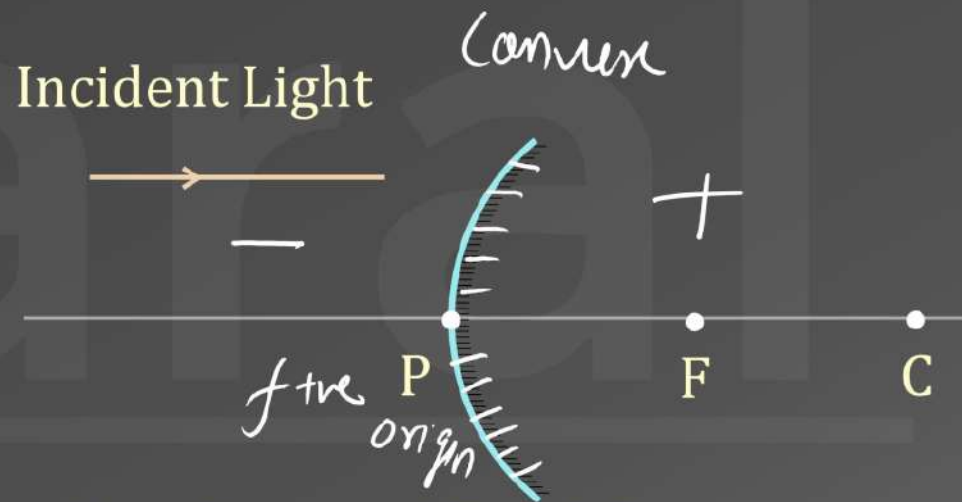
A ray passing through or directed towards centre of curvature, after reflection from the mirror, retraces its path.



Along principal axis, distances are measured from the pole.  
Direction of incident light is taken as positive. ✪



Coordinates of C and F are -ve



Coordinates of F and C are +ve





TRICK

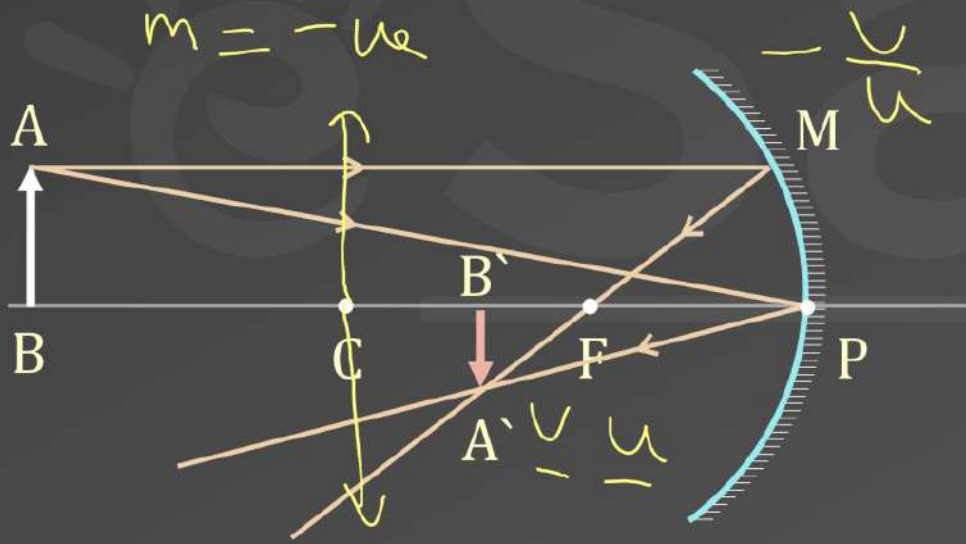
# Mirror Equation



$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$$

'u' : coordinate of object  
'v' : coordinate of image  
'f' : coordinate of focus

$$m = \frac{-v}{u} = \frac{f}{f - u}$$



Linear magnification  
(Transverse magnification)

$$m = \frac{\text{height of image}}{\text{height of object}} = \frac{h_i}{h_o}$$

( $h_i$  and  $h_o$  are put with sign)

# Magnification



$$m = \frac{h_i}{h_o}$$



Magnification	Image
$ m  > 1$	Enlarged
$m < 0$ (-ve)	Inverted
$ m  < 1$	Diminished
$m > 0$	Erect

-2

Inv, Enlarged

$+\frac{1}{2}$

Erect, Dim

$$m_{\text{net}} = \frac{h_{\text{I-final}}}{h_{\text{object}}}$$

$$m_{\text{net}} = \underline{m_1} \times \underline{m_2} \times \underline{m_3} \times \dots$$

$$m_{\text{net}} = \frac{h_{I_1}}{h_0} \times \frac{h_{I_2}}{h_{I_1}} \times \frac{h_{I_3}}{h_{I_2}} \times \dots = \frac{h_{\text{I-final}}}{h_0}$$

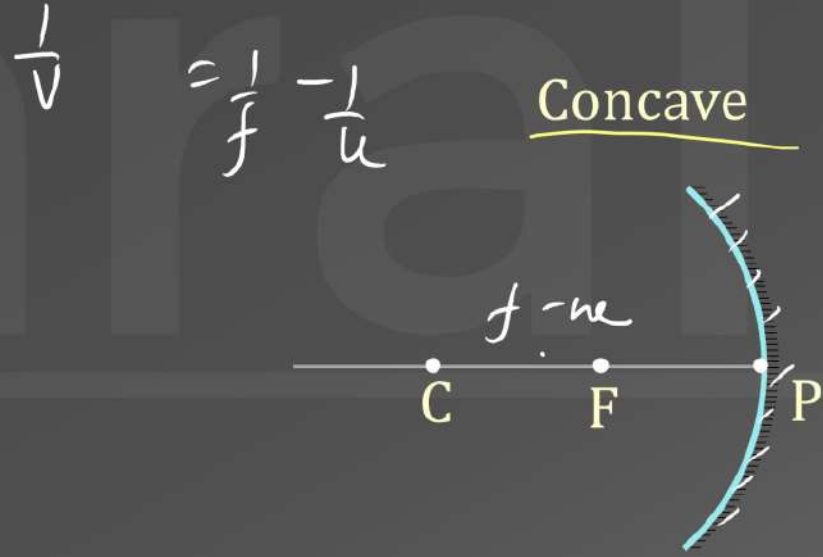
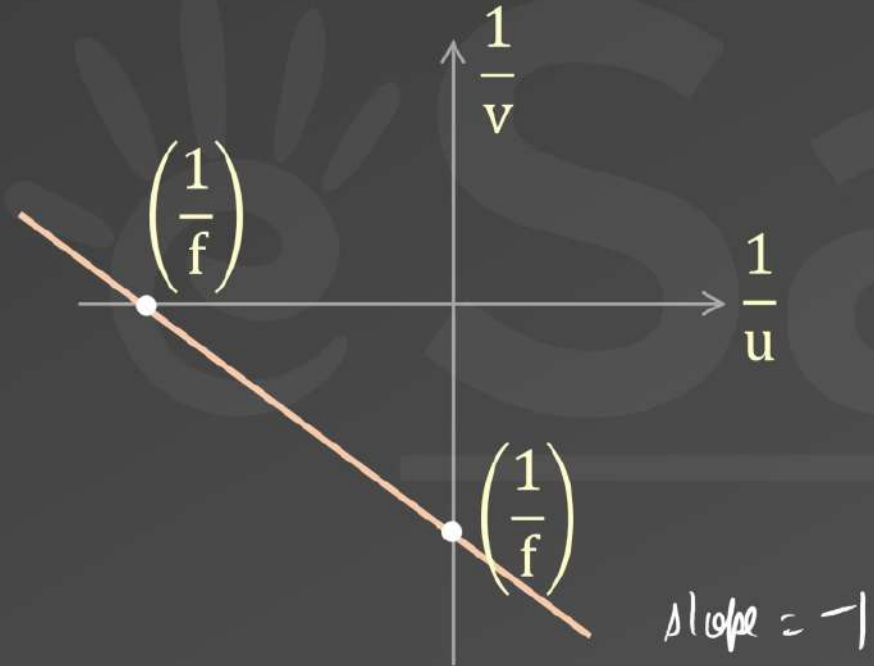


TRICK

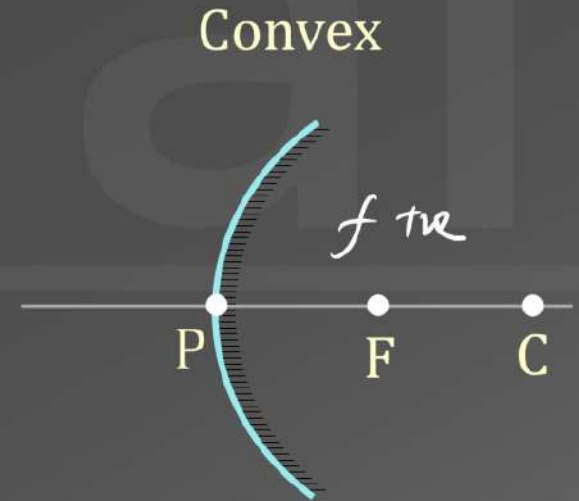
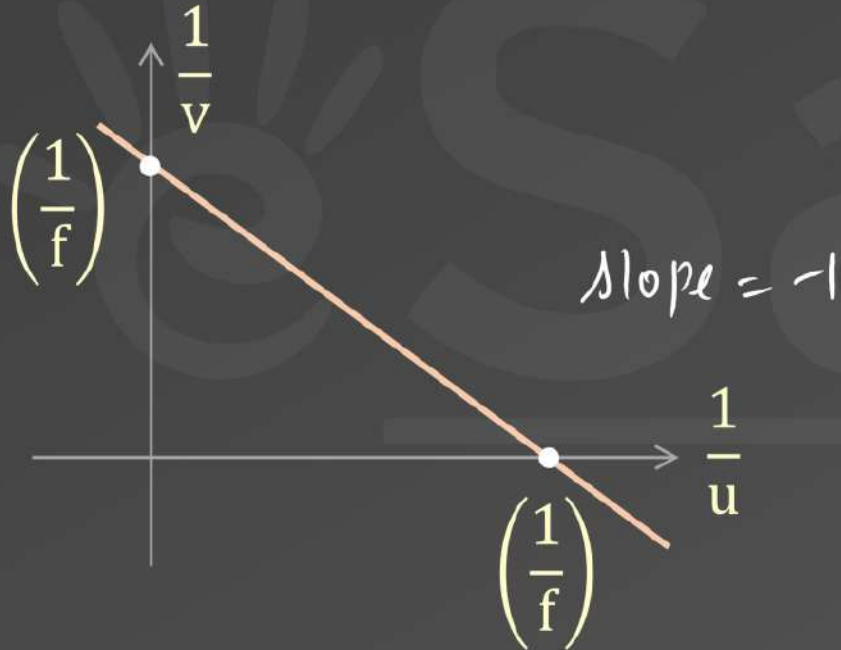
Graphs ✨



$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f} \Rightarrow \frac{1}{v} = \frac{1}{f} + \frac{1}{u}$$



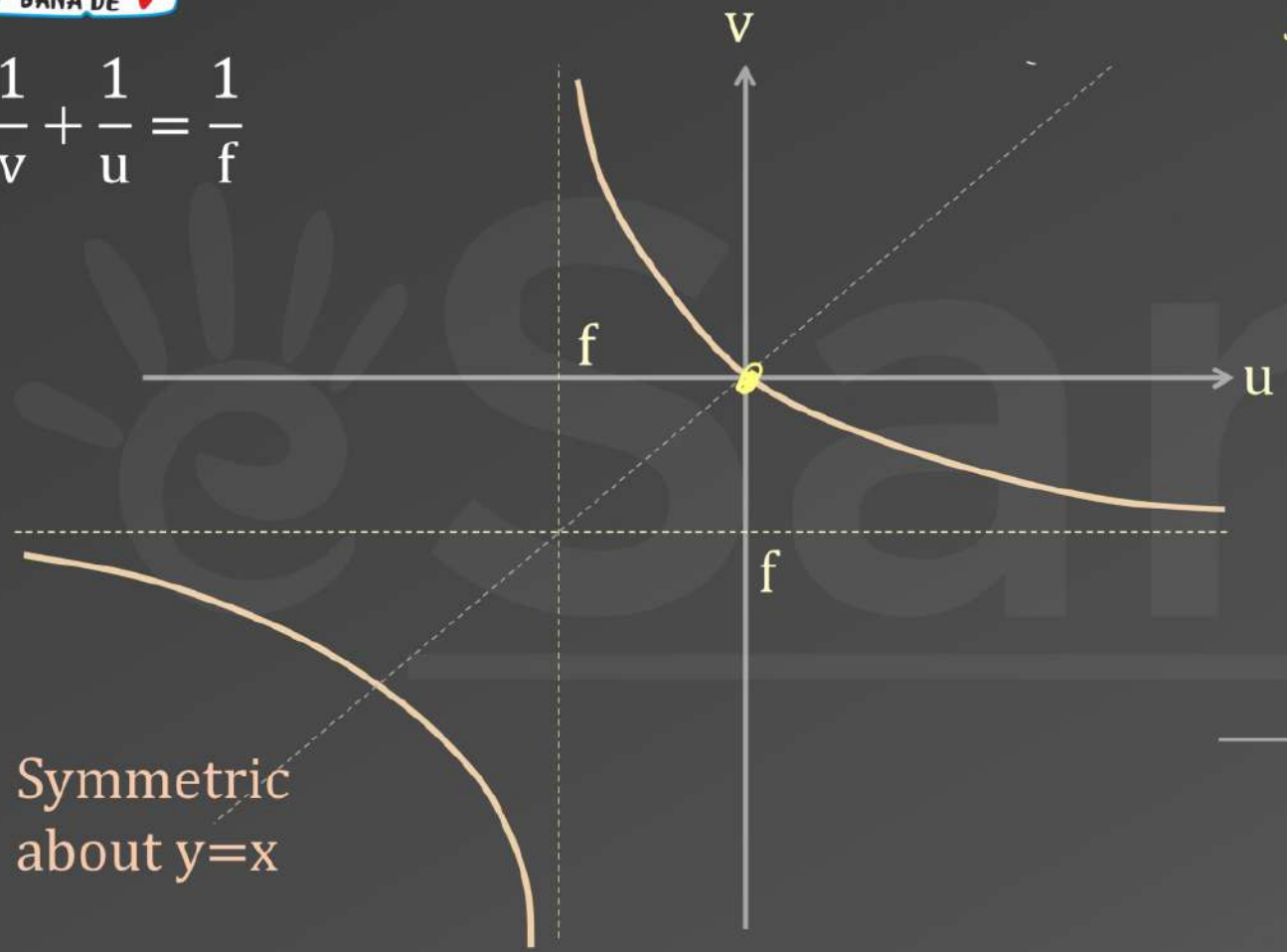
$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f} \Rightarrow \frac{1}{v} = \left(-\frac{1}{u}\right) + \frac{1}{f}$$



# Graphs



$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$$



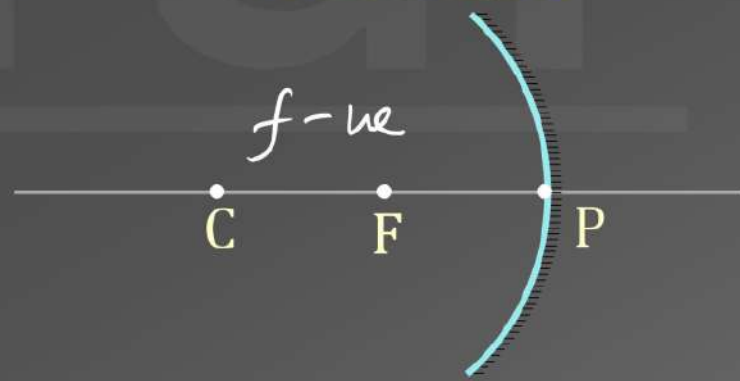
Symmetric about  $y=x$

TRICK

ORIGIN passes

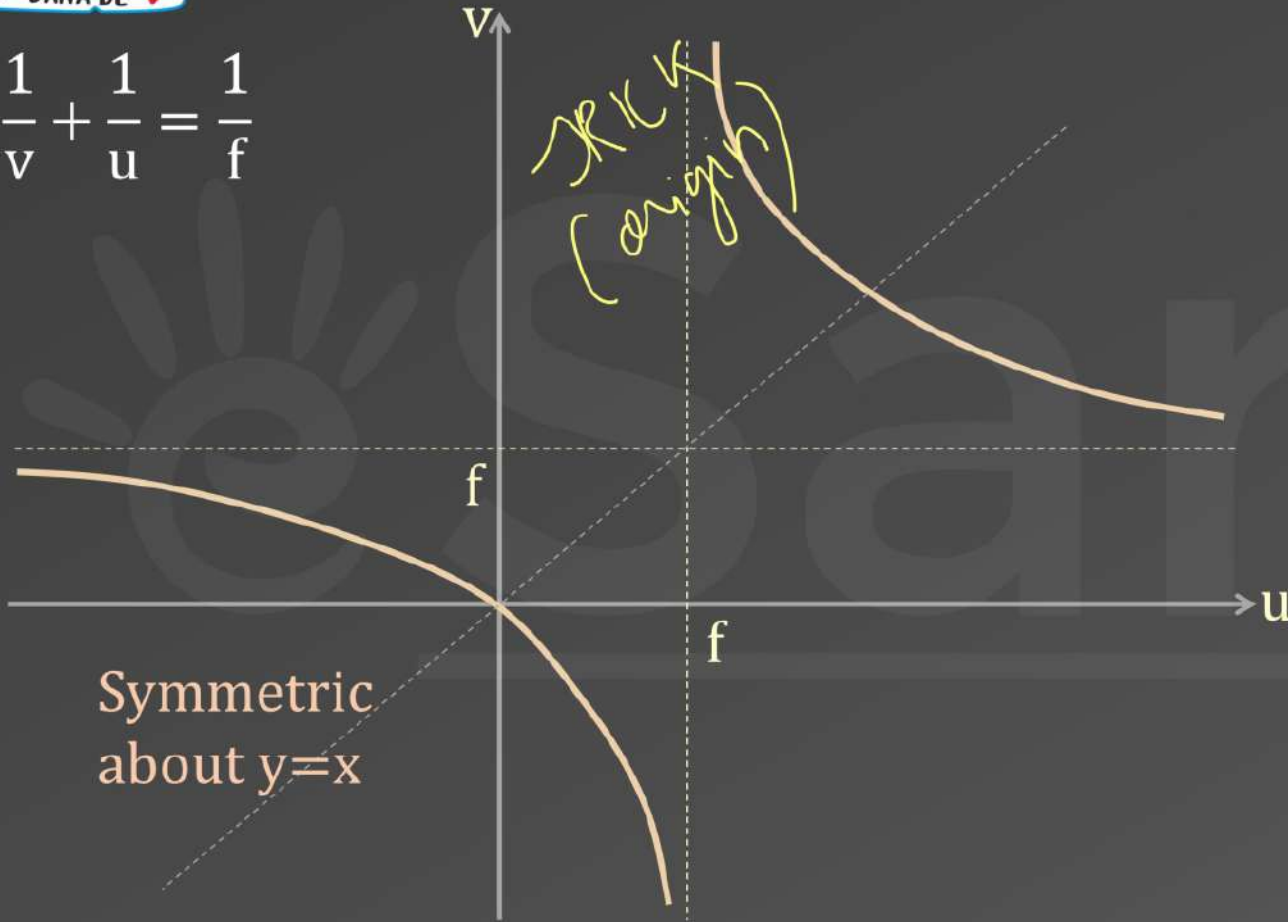
$f - ve$

Concave

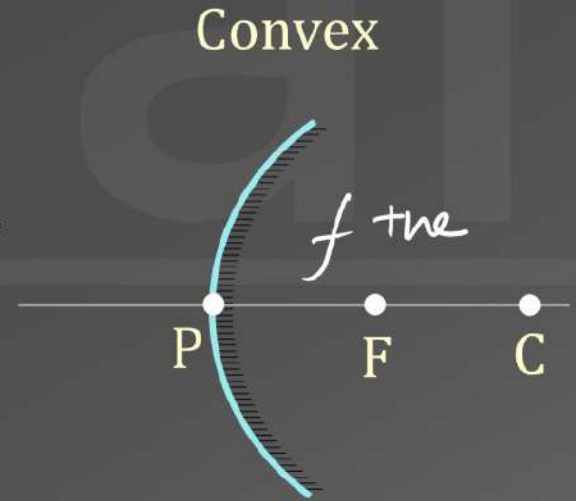




$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$$



Symmetric  
about  $y=x$



# Newton's Formula



from F +ve

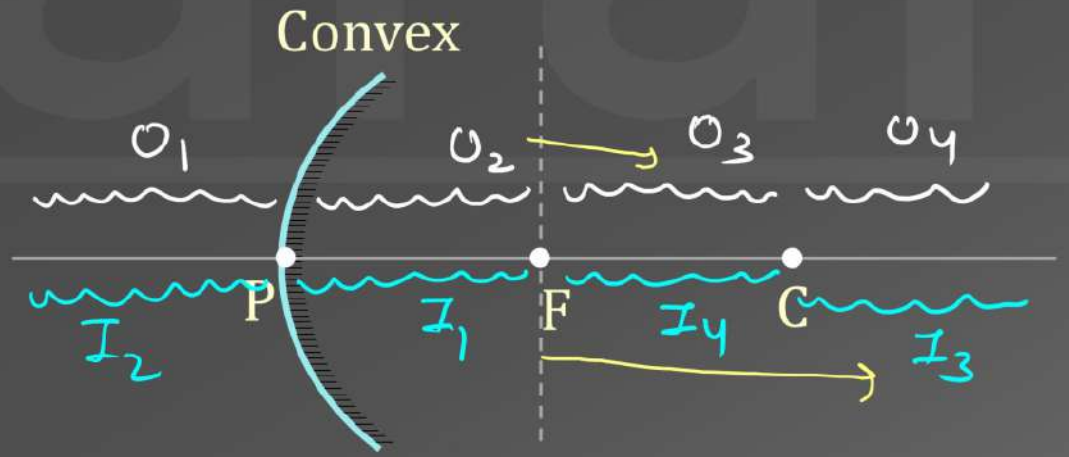
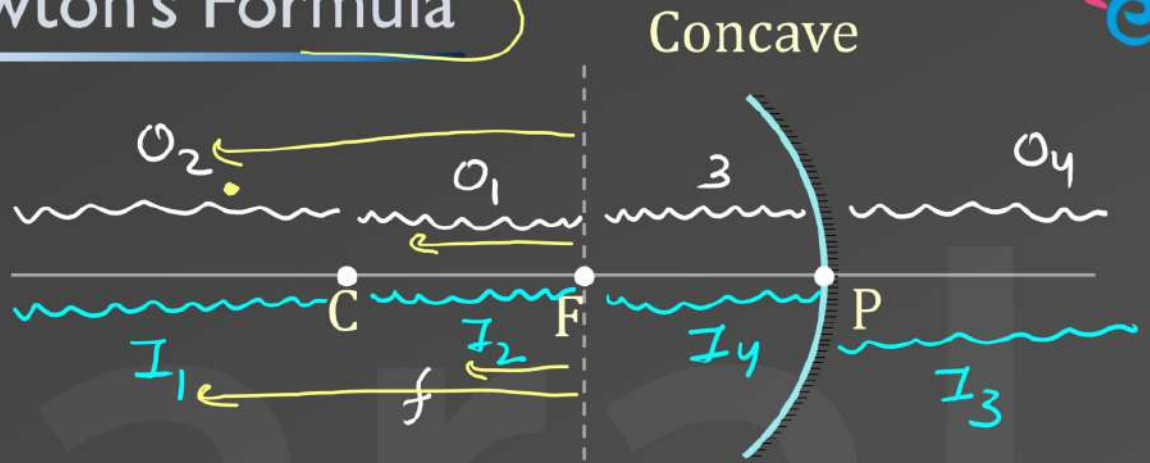
$$x_i x_o = f^2$$

same sign

$$x_o x_i = f^2 \quad +ve$$

$$|x_o| < f$$

$$|x_i| > f$$

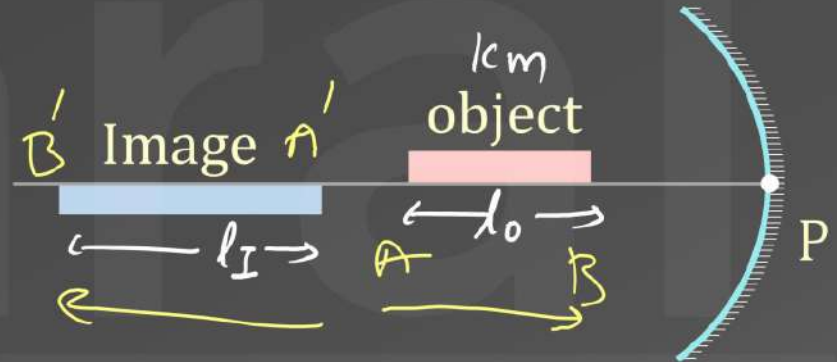




$$LM = \frac{\text{Length of image along PA}}{\text{Length of object along PA}}$$

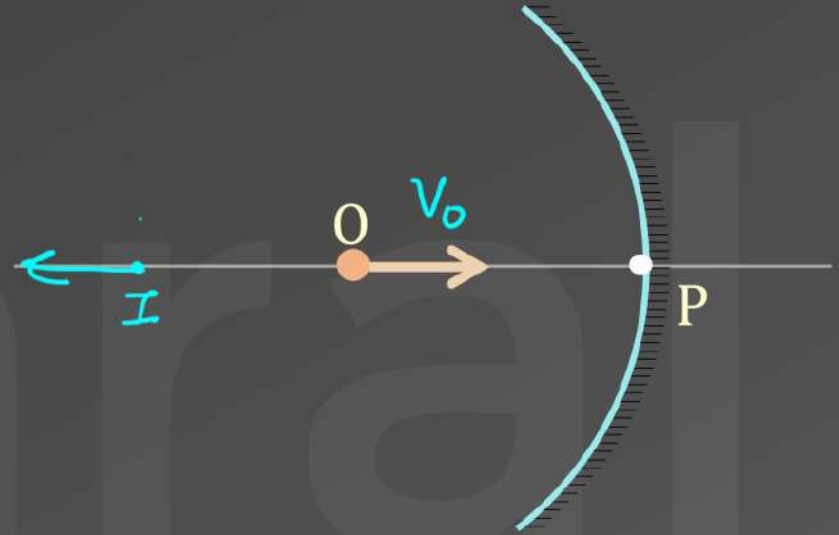
$$LM = -m^2 \text{ where } m \text{ is (TM)}$$

$$= \frac{l_I}{l_o}$$



Along PA

$$\vec{V}_I = -m^2 \vec{V}_O$$



# QUIZ TIME

MIRRORS AT AN ANGLE  
 $N = 360/\theta$

CONDITION	NO. OF IMAGES
If $N = \text{EVEN Integer}$	$N - 1$
If $N = \text{ODD Integer}$ 1. Object on $L$ Bisector 2. If Not	<b>1</b>
If $N \neq \text{Integer}$	Count Manually

RAY TRACING DIAGRAM

<p>A ray <math>\parallel</math> to principal axis after reflection passes/appear to pass through focus.</p>	<p>A ray passing through centre of curvature after reflection retraces its path.</p>
<p>A ray <math>\parallel</math> to principal axis after reflection passes through focus.</p>	<p>A ray passing through centre of curvature after reflection retraces its path.</p>

MAGNIFICATION

**3**

LINEAR magnification

$$m = \frac{\text{ht. of Image}}{\text{ht. of Object}} = \frac{h_i}{h_o}$$

( $h_i$  &  $h_o$  with sign.)

$|m| > 1 \rightarrow$  Enlarged  
 $|m| < 1 \rightarrow$  Diminished  
 $m < 0 \rightarrow$  Inverted;  $m > 0 \rightarrow$  Erect

NET MAGNIFICATION

$$m_{\text{net}} = \frac{h_{\text{I-final}}}{h_{\text{object}}}$$

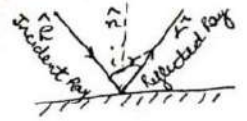
$$m_{\text{net}} = m_1 \times m_2 \times m_3 \dots$$

$$m_{\text{net}} = \frac{h_{I_1} \times h_{I_2} \times h_{I_3} \dots}{h_o \times h_{I_1} \times h_{I_2}}$$

$$= \frac{h_{\text{I-final}}}{h_o}$$

LAWS OF REFLECTION

- $[\hat{e} \hat{r} \hat{n}] = 0$   
 $[\hat{e}' \hat{x} \hat{r}] \cdot \hat{n} = 0$
- $L_i = L_r$



FOCAL LENGTH  
**5**  
 Distance of focus from Pole

OBJECT

Real  
 (Intersection of Diverging Rays)  
 Virtual  
 (Intersection of Converging Incident Ray)

IMAGE

Real Image  
 Virtual Object  
 Virtual Image  
 Real Object

REFLECTION

MIRROR Equation  
**2**

$U \rightarrow$  Coordinate of Object  
 $V \rightarrow$  Coordinate of Image  
 $f \Rightarrow$  focus coord.

PROPERTIES OF IMAGE FORMED BY PLANE MIRROR

- It forms (i) Real Image of Virtual Object  
 (ii) Virtual Image of Real Object
- Distance of Object = Distance of image from the mirror  
 (from the mirror) ( $h_i = h_o$ )
- Size of Image = Size of Object
- Image formed is SIDEWAYS INVERTED.

VELOCITY OF Image

$$(\vec{V}_o)_{\parallel} = (\vec{V}_i)_{\parallel}$$

$$(\vec{V}_o/m)_{\perp} = -(\vec{V}_i/m)_{\perp}$$

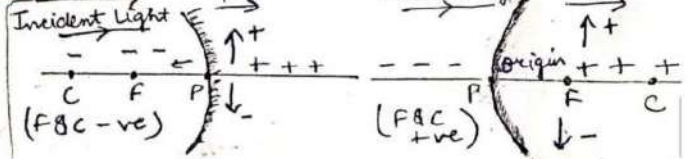
VELOCITY OF Image of Moving Object (Sph. Mirror)

$$\vec{V}_I = -m^2 \vec{V}_O$$

LONGITUDINAL magnification

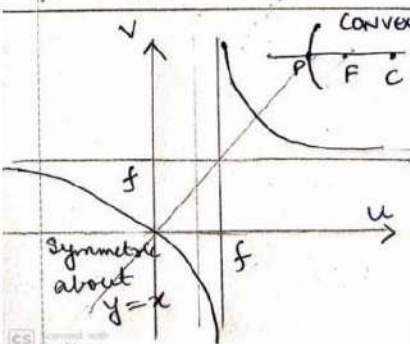
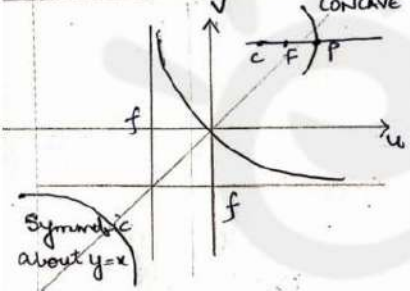
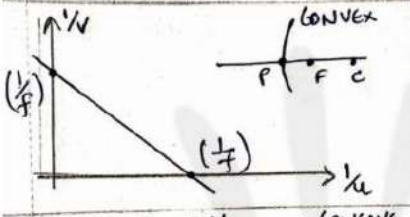
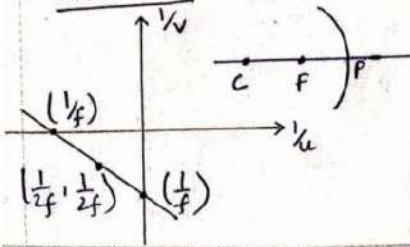
**4**

SIGN-CONVENTION



# GRAPHS

CONCAVE



# MIRRORS AT AN ANGLE

$N = 360/\theta$

CONDITION	NO. OF IMAGES
If $N = \text{EVEN Integer}$	$N - 1$
If $N = \text{ODD Integer}$	$N - 1$
1. Object on L Bisector	$N$
2. If Not	
If $N \neq \text{Integer}$	Count Manually

## RAY TRACING DIAGRAM

<p>A ray    to principal axis after reflection passes/appear to pass through focus.</p>	<p>A ray passing through centre of curvature after reflection retraces its path.</p>
<p>A ray    to principal axis after reflection passes through focus.</p>	<p>A ray passing through centre of curvature after reflection retraces its path.</p>

## MAGNIFICATION

$$m = \frac{-v}{u} = \frac{f}{f-u}$$

## LINEAR Magnification

$$m = \frac{\text{ht. of Image}}{\text{ht. of Object}} = \frac{h_i}{h_o}$$

( $h_i$  &  $h_o$  with sign.)

$|m| > 1 \rightarrow$  Enlarged

$|m| < 1 \rightarrow$  Diminished

$m < 0 \rightarrow$  Inverted;  $m > 0 \rightarrow$  Erect

## NET MAGNIFICATION

$$m_{\text{net}} = \frac{h_{\text{I-final}}}{h_{\text{object}}}$$

$$m_{\text{net}} = m_1 \times m_2 \times m_3 \dots$$

$$m_{\text{net}} = \frac{h_{\text{I1}}}{h_o} \times \frac{h_{\text{I2}}}{h_{\text{I1}}} \times \frac{h_{\text{I3}}}{h_{\text{I2}}} \dots$$

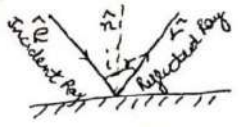
$$= \frac{h_{\text{I-final}}}{h_o}$$

Min. size of a plane mirror required to see the full image of an observer is half the size of that observer



# LAWS OF REFLECTION

- $[\hat{e} \hat{v} \hat{n}] = 0$   
 $[\hat{e} \times \hat{r}] \cdot \hat{n} = 0$
- $L_i = L_v$



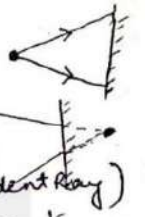
## FOCAL LENGTH

$$f = R/2$$

Distance of focus from Pole

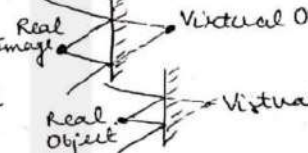
## OBJECT

Real (Intersection of Diverging Rays)  
Virtual (Intersection of Converging Incident Ray)



## IMAGINE

Real  
Virtual



# REFLECTION

## MIRROR Equation

$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$$

$U \rightarrow$  Coordinate of Object

$V \rightarrow$  Coordinate of Image

$f \rightarrow$  focus coord.

## LONGITUDINAL Magnification

$$LM = -m^2 = \frac{L_i}{L_o}$$

where  $m$  is  $(\text{Im})/L_o$



## PROPERTIES OF IMAGE FORMED BY PLANE MIRROR

- It forms (i) Real Image of Virtual Object  
(ii) Virtual Image of Real Object
- Distance of Object = Distance of image from the mirror
- Size of Image = Size of Object ( $h_i = h_o$ )
- Image formed is SIDE-WAYS INVERTED.

## VELOCITY OF Image

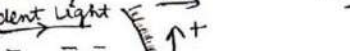
$$(\vec{V}_o)_{\parallel} = (\vec{V}_i)_{\parallel}$$

$$(\vec{V}_o/m)_{\perp} = -(\vec{V}_i/m)_{\perp}$$

## VELOCITY OF Image of Moving Object (Sp. Motion)

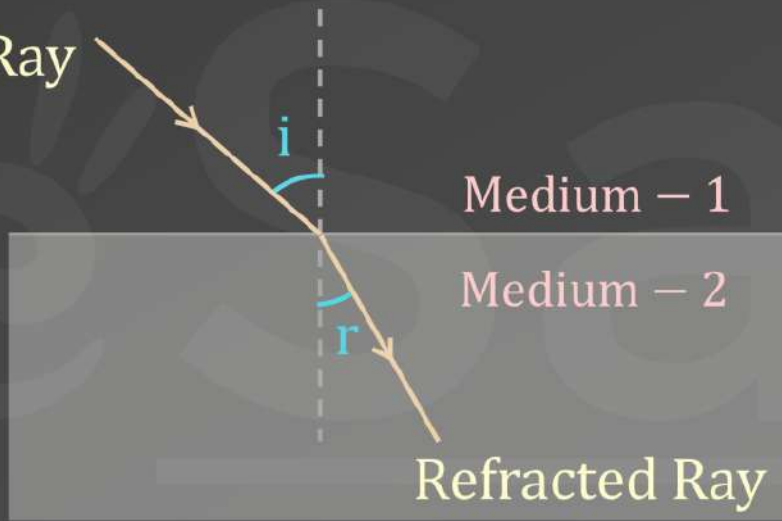
$$\vec{V}_I = -m^2 \vec{V}_O$$

## SIGN-CONVENTION



Normal to the surface

Incident Ray



Refracted Ray



Refractive index of medium ( $\mu$ )

$$\mu = \frac{c}{v_m}$$

$c$  → vacuum  
 $v_m$  → medium

$$\mu_{\text{vacuum}} = 1$$

$$\mu_{\text{air}} = 1.0003 \approx 1$$

$$\mu_{\text{water}} = 4/3 = 1.33$$

$$\mu_{\text{glass}} = 3/2 = 1.5$$





$$\mu_{\text{air}} = 1$$

Optically Rarer  
(Lesser  $\mu$ )

$$\mu_{\text{vacuum}} = 1$$

$$\mu_{\text{air}} = 1.0003 \approx 1$$

$$\mu_{\text{water}} = 4/3 = 1.33$$

$$\mu_{\text{glass}} = 3/2 = 1.5$$

$\mu_{\text{glass}} = 3/2$  Optically Denser  
(Higher  $\mu$ )







Relative Refractive index of medium(1) w.r.t medium (2) is defined as

$$\underline{\underline{\mu_{1/2} = \frac{\mu_1}{\mu_2}}}$$

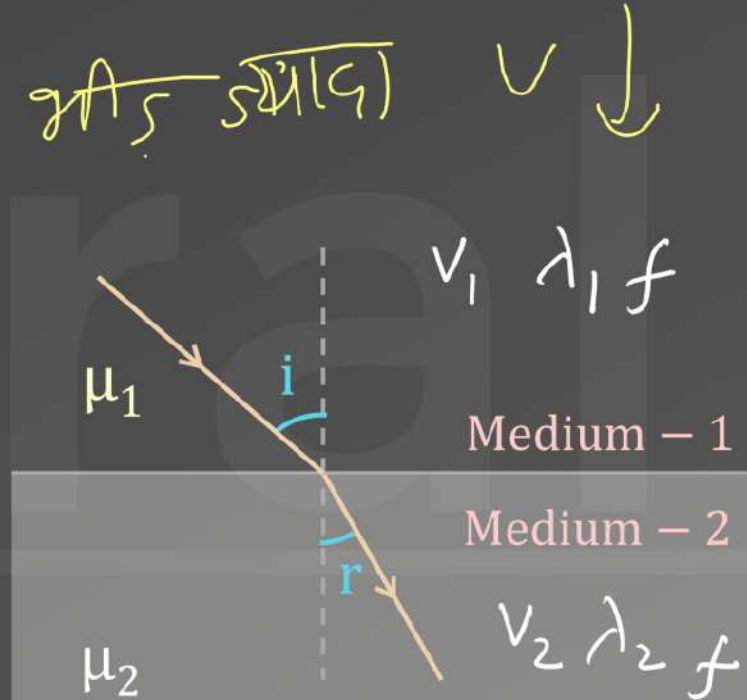
eSaral



$$v = f \lambda$$

$$\frac{v_1}{v_2} = \frac{\lambda_1}{\lambda_2} = \frac{\mu_2}{\mu_1}$$

TRICK  
 $\mu \uparrow \quad v \downarrow \quad \lambda \downarrow$



When light from same source enters different medium then its speed and wavelength changes but frequency remains same.

- (i) Incident ray, refracted ray and normal to surface always lie in the same plane.

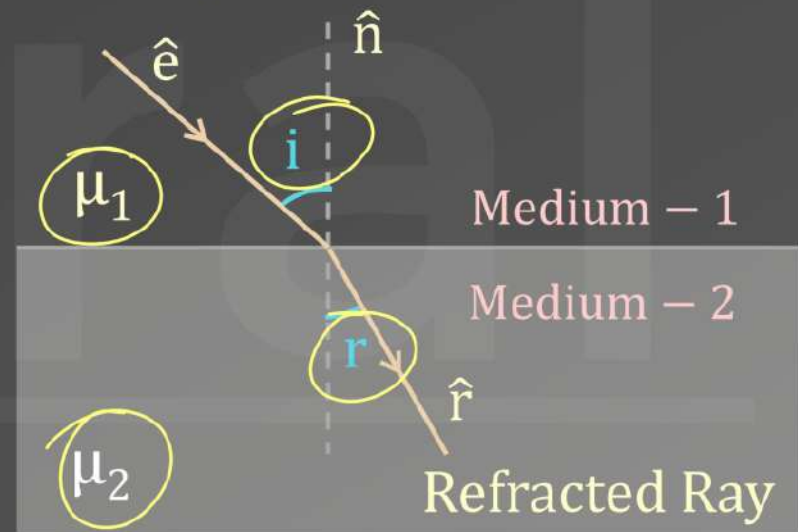
In vector form

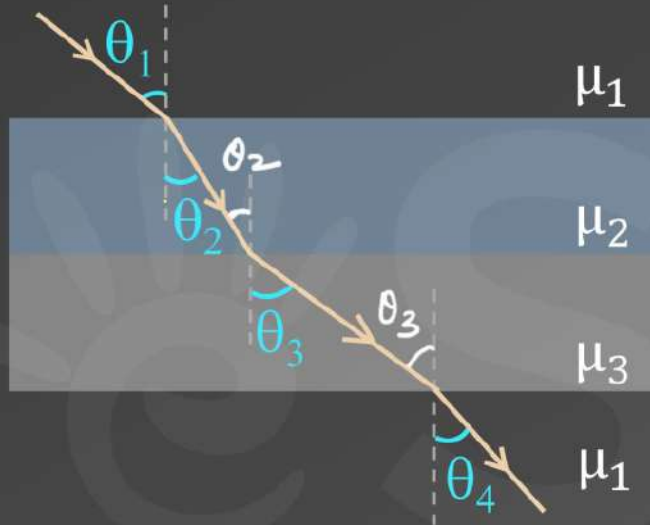
$$[\hat{e} \quad \hat{n} \quad \hat{r}] = 0 \Rightarrow (\hat{e} \times \hat{r}) \cdot \hat{n} = 0$$

- (ii) Snell's Law

$$\mu_1 \sin i = \mu_2 \sin r$$

Incident Ray





$$\mu_1 \sin \theta_1 = \mu_2 \sin \theta_2 = \mu_3 \sin \theta_3 = \mu_1 \sin \theta_4$$



## Atmospheric Refraction

- Early Sunrise and Delayed Sunset
- Apparent flattenning of Sun at sunset and sunrise
- Twinkling of Stars

# Apparent Depth

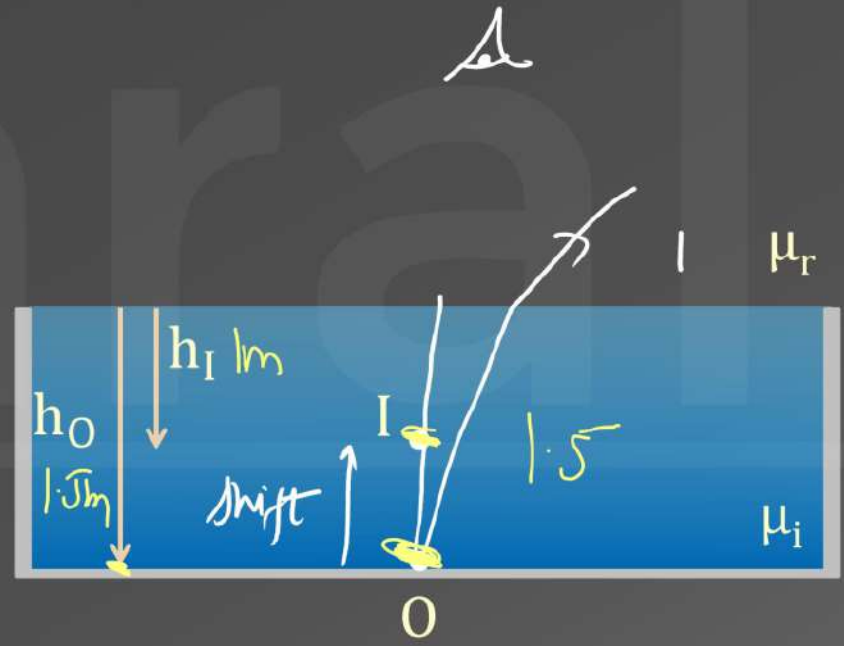


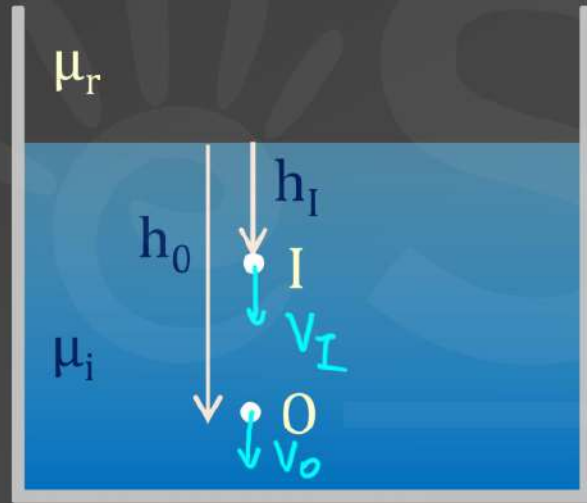
✳ ✳

$$h_I = \frac{h_o}{\mu_i/\mu_r}$$

$$h_I = \frac{h_o}{\mu}$$

$$\begin{aligned} \text{Shift} &= h_o - h_I \\ &= h_o \left( 1 - \frac{1}{\mu_i/\mu_r} \right) \\ &= h_o \left( 1 - \frac{1}{\mu} \right) \end{aligned}$$





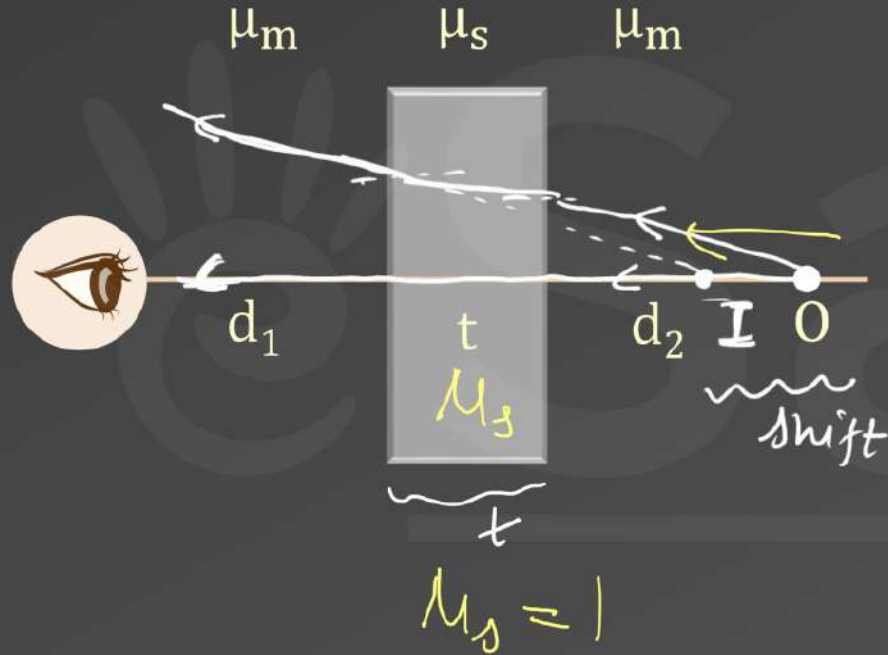
diff<sup>n</sup>  
wrt  
t

$$h_I = \frac{h_0}{\mu_i/\mu_r}$$

$$\vec{V}_I = \frac{\vec{V}_0}{\mu_i/\mu_r}$$



# Refraction through Parallel Slab



TRICK

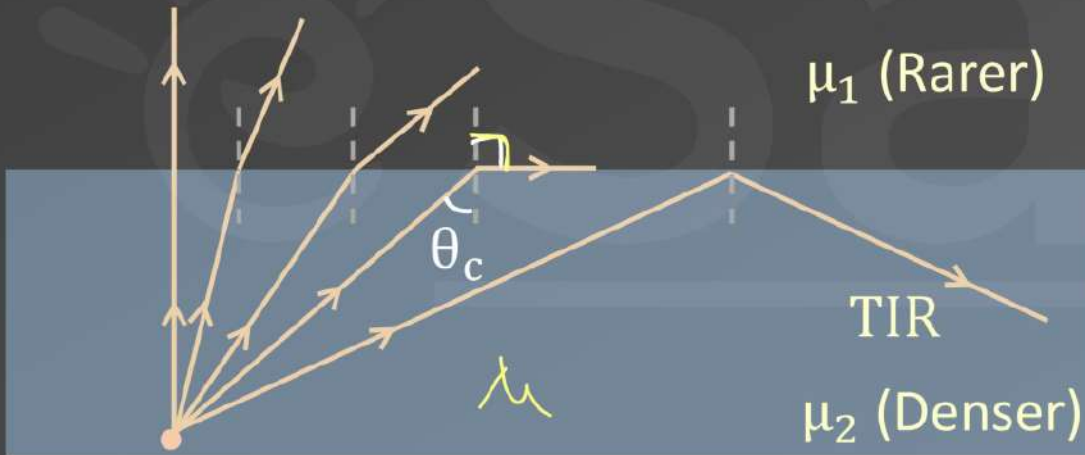
$$\text{shift} = t \left( 1 - \frac{1}{\mu_s / \mu_m} \right)$$

in direction of incident Ray





$$\sin \theta_c = \frac{1}{\mu} = \frac{1}{\mu_2 / \mu_1}$$



Critical Angle ( $\theta_c$ ) : Angle of incident at which angle of refraction becomes  $90^\circ$ .

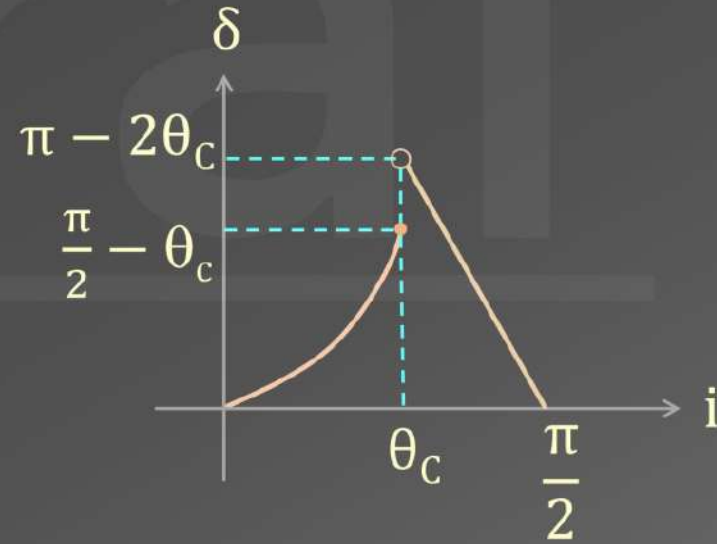
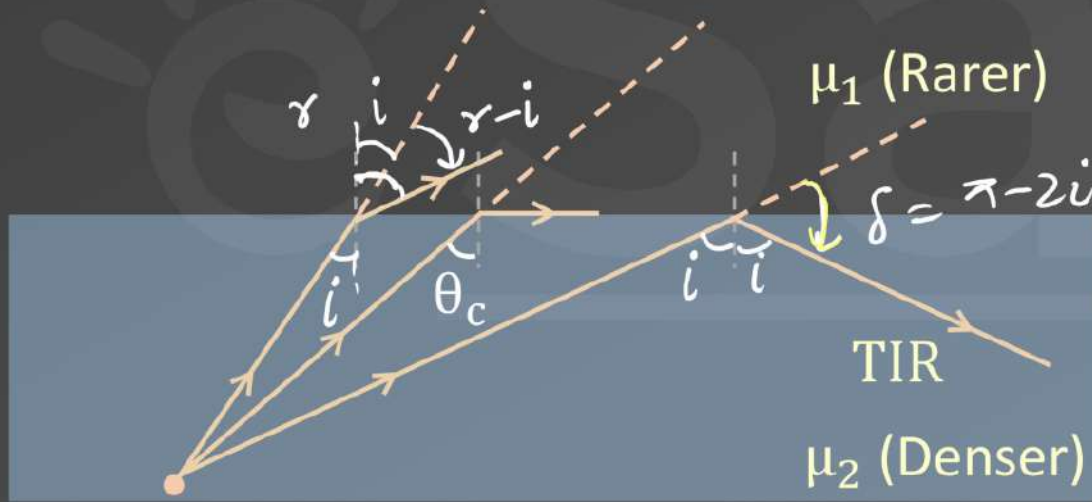
## Applications of TIR

- Optical Fibre
- Mirage / Looming
- Sparkling of Diamond
- Prism to bend light by  $90^\circ$ ,  $180^\circ$

## Total Internal Reflection

Refraction :  $\delta = r - i$

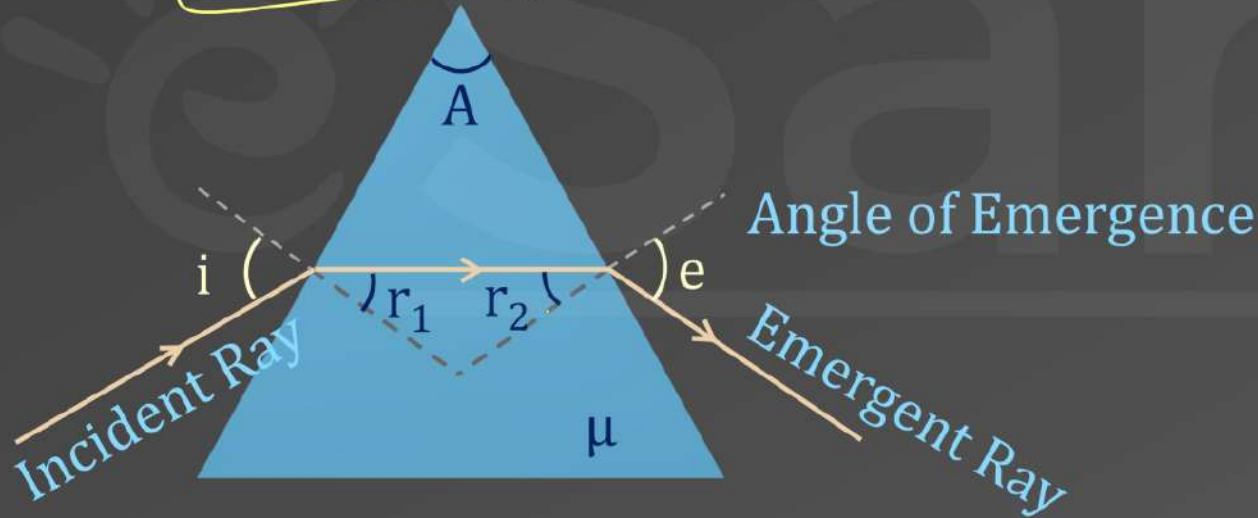
Reflection :  $\delta = \pi - 2i$

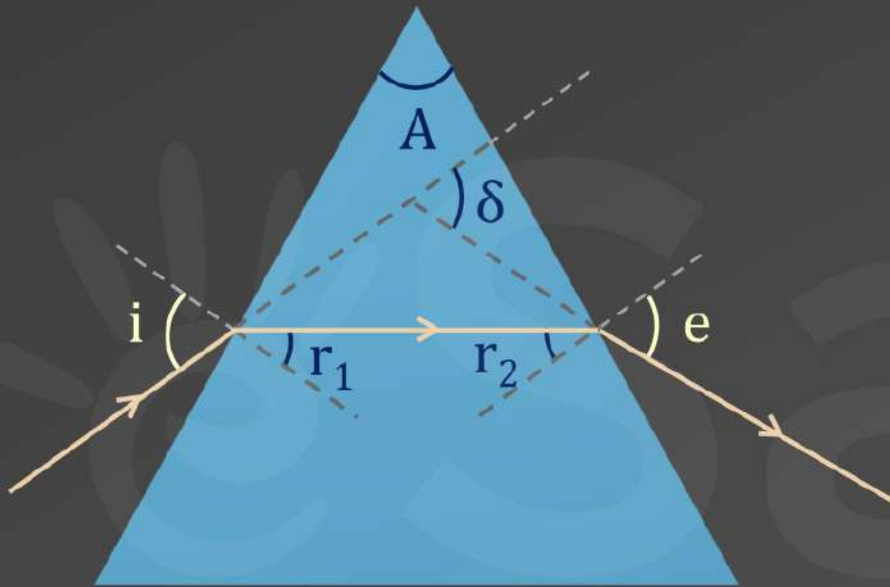


$$1 \sin i = \mu \sin r_1$$

$$\mu \sin r_2 = 1 \sin e$$

$$A = r_1 + r_2$$





$$\delta = i + e - A$$

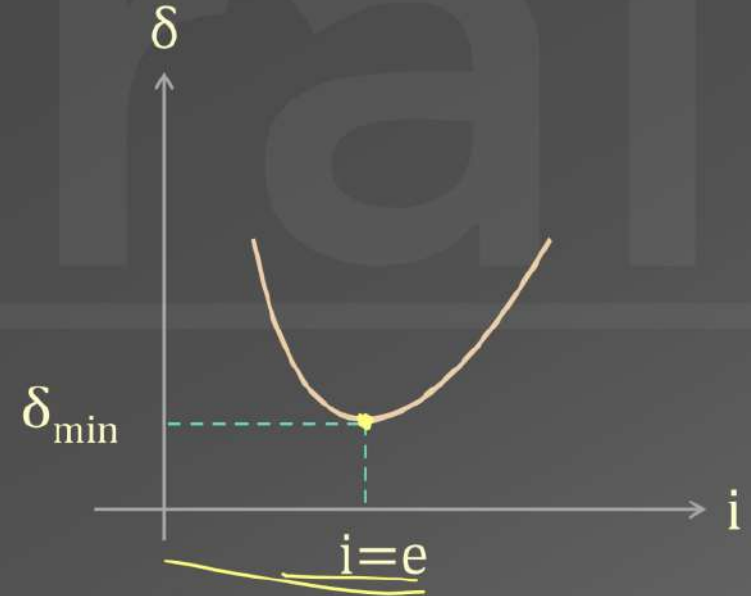
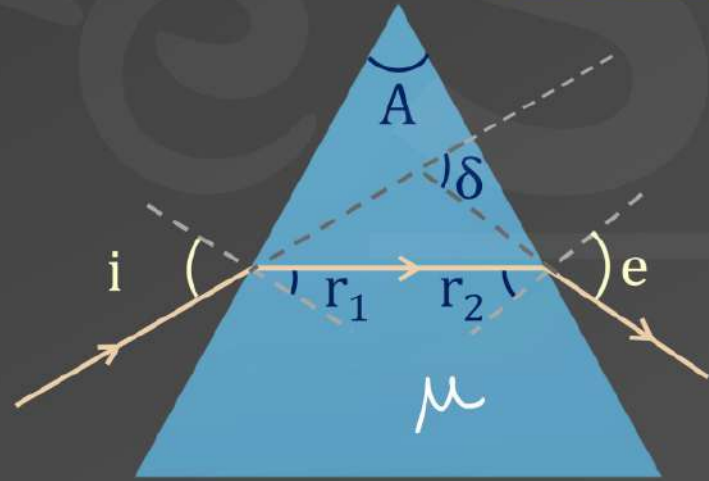


$\delta_{min}$   
 $i=e$

$r_1 = r_2$

$$\mu = \frac{\sin\left(\frac{\delta_{min} + A}{2}\right)}{\sin\left(\frac{A}{2}\right)}$$

$\delta = i + e - A$



# Maximum Angle of Deviation



$\delta_{\max}$

$i = 90^\circ$

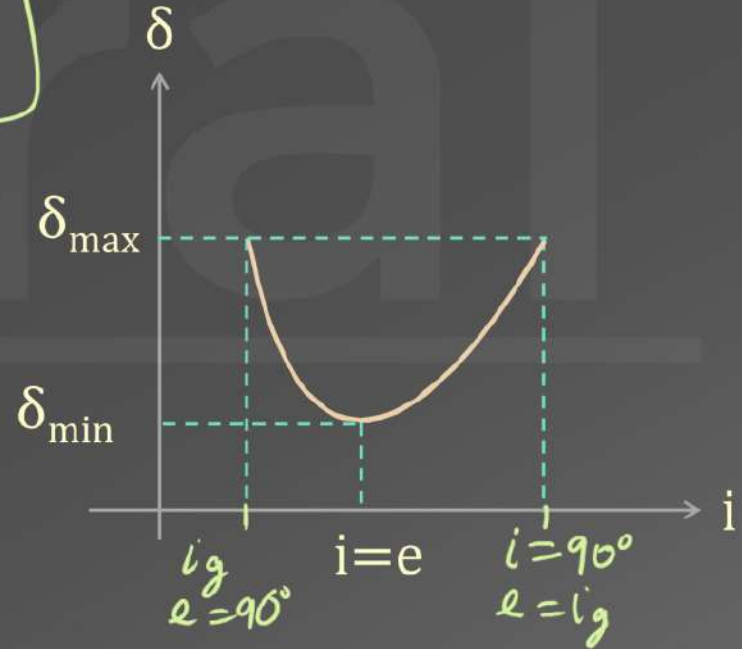
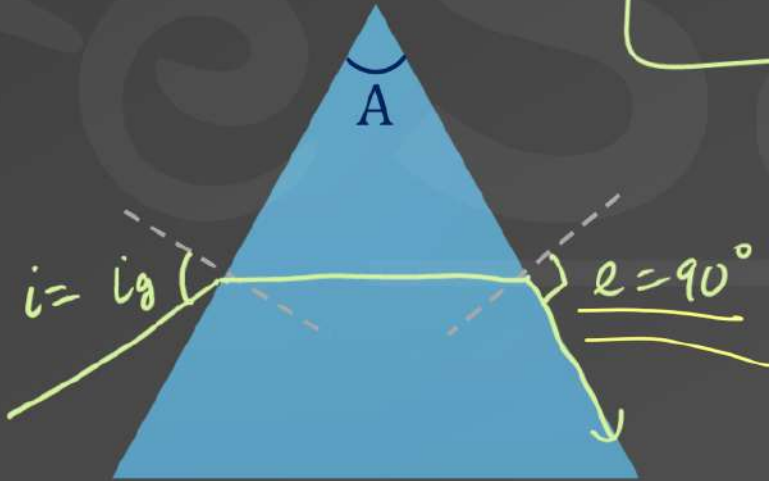
$e = i_g$

$i = i_g$

$e = 90^\circ$

$\delta = i + e - A$

$\Rightarrow \delta_{\max} = i_g + 90^\circ - A$



Thin Prism have very small angle of prism.



$$\delta = (\mu - 1)A$$



$$\delta_{\min}$$

$$i = e$$

$$\mu = \frac{\sin\left(\frac{\delta_{\min} + A}{2}\right)}{\sin\left(\frac{A}{2}\right)}$$

$$\delta_{\max}$$

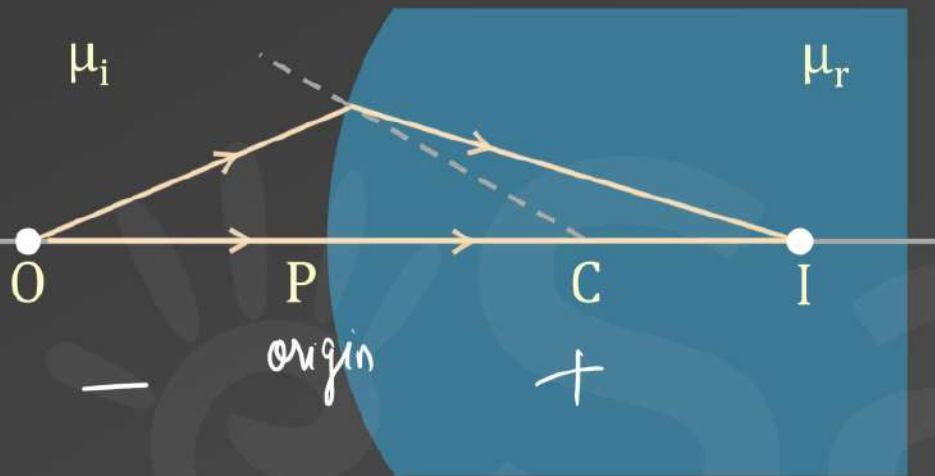
$$i = 90^\circ$$

$$e = e_g$$

$$i = i_g$$

$$e = 90^\circ$$





P is taken as origin.

Direction along incident ray is taken as positive.

$u$  = Coordinate of object.

$v$  = Coordinate of image.

$R$  = Coordinate of centre of curvature.

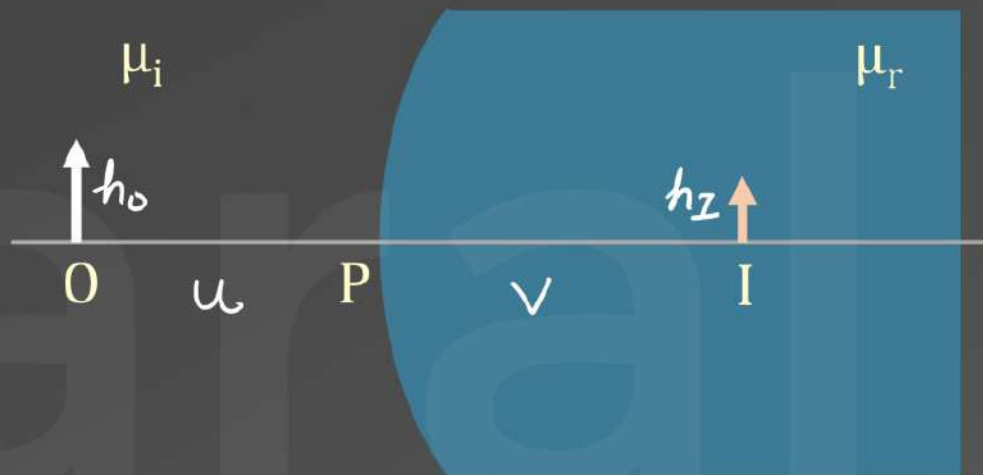
$\mu_i$  = Refractive index of medium having incident rays.

$\mu_r$  = Refractive index of medium having refracted rays.

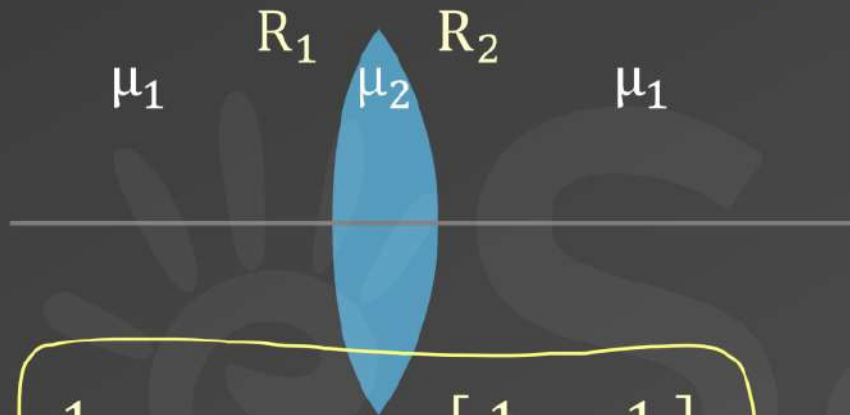
$$\frac{\mu_r}{v} - \frac{\mu_i}{u} = \frac{\mu_r - \mu_i}{R}$$

$$m = \frac{\text{Height of image}}{\text{Height of object}} \quad (\text{with sign})$$

$$m = \frac{h_I}{h_O} = \frac{v/\mu_r}{u/\mu_i}$$



# Lens



$$m = \frac{h_I}{h_o} = \frac{v}{u}$$

$$\frac{1}{f} = (\mu_{2/1} - 1) \left[ \frac{1}{R_1} - \frac{1}{R_2} \right]$$

(Lens Maker's formula)

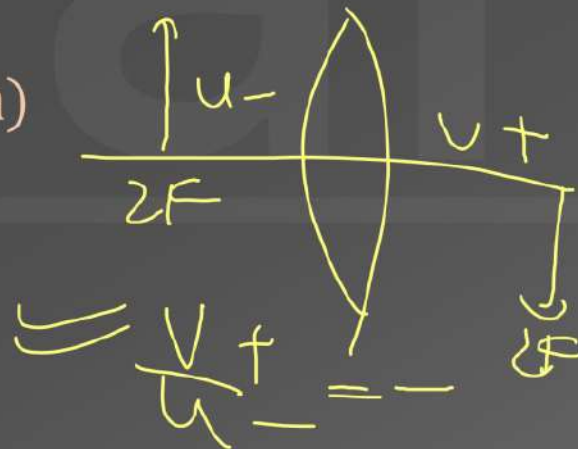
$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$

**TRICK**

Lens formula

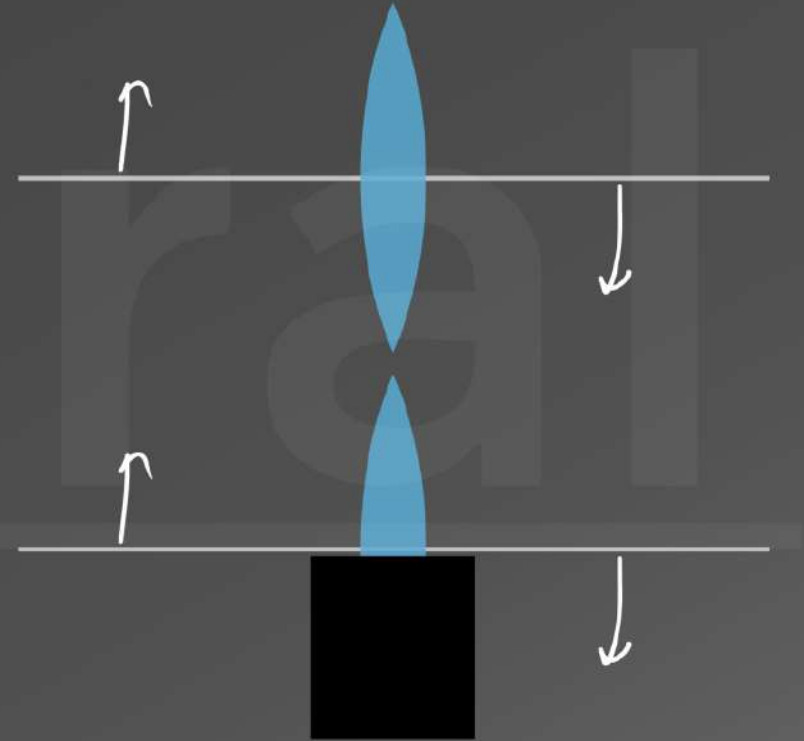
$u, v, f, R_1, R_2$  are coordinates

(Less)



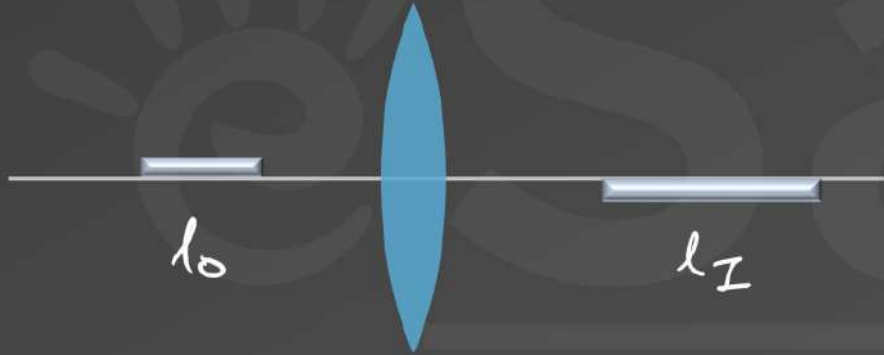
Location of image remains unchanged, only intensity decreases

Remember Donkey 😊 !!

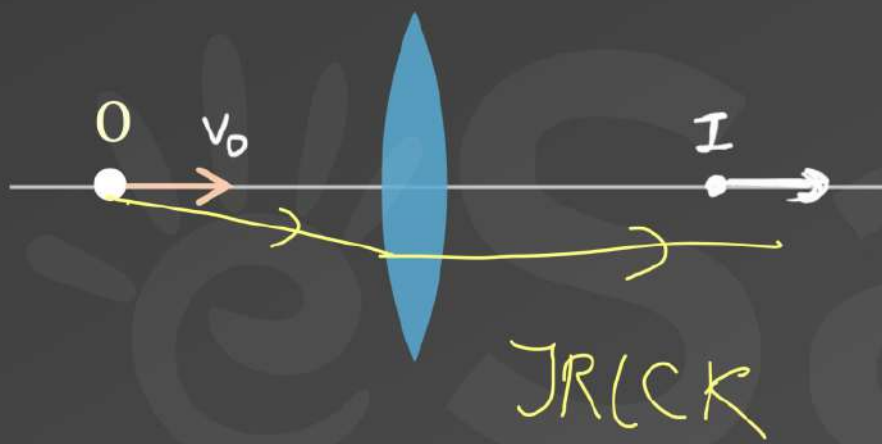


$$\text{LM} = m^2 = \frac{l_I}{l_o}$$

$$m = \frac{h_I}{h_o} = \frac{v}{u}$$



# Velocity of Image



$$\vec{v}_I = m^2 \vec{v}_0$$



$$P = \frac{1}{f}$$

SI unit : diopetre (D) ( $m^{-1}$ )

$f$  +ve  
 $P$  +ve



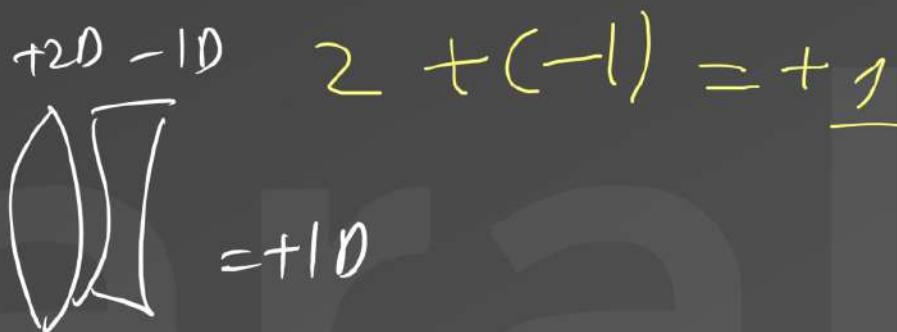
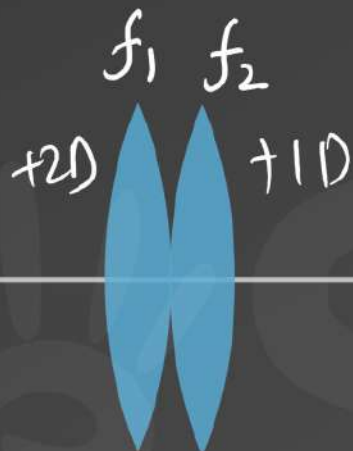
Convex

$f$  -ve  
 $P$  -ve



Concave

# Lenses Kept Very Close to Each Other



$$\frac{1}{f_{eq}} = \frac{1}{f_1} + \frac{1}{f_2} + \frac{1}{f_3} + \dots$$

~~$$f_{eq} = f_1 + f_2 + f_2$$~~

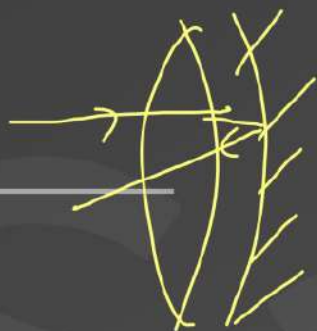
$$P_{eq} = P_1 + P_2 + P_3 + \dots$$

with sign





Mirror



$$P_m = -\frac{1}{f_m}$$

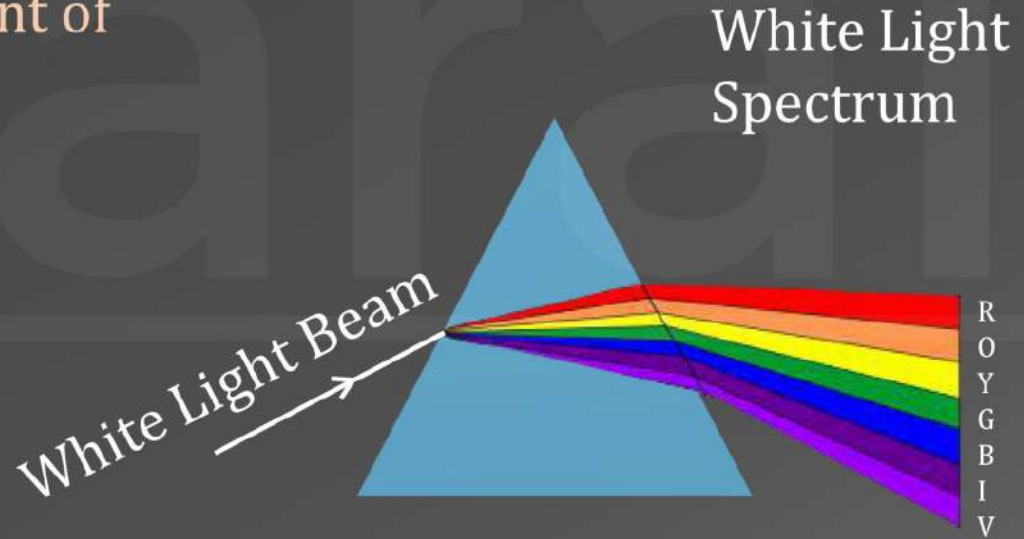
$$P_{eq} = P_1 + P_2 + P_3 + \dots$$

$$P_{eq} = \underbrace{P_L}_L + \underbrace{P_m}_M + \underbrace{P_L}_L$$

$$P_{eq} = \frac{1}{f_L} - \frac{1}{f_m} + \frac{1}{f_L} = -\frac{1}{f_{eqm}}$$

The phenomenon of splitting of light into its component colours is known as Dispersion.

The pattern of colour component of light is called spectrum of light.



Cauchy's eq.

$$\mu = A + \frac{B}{\lambda^2}$$

$\lambda \uparrow \quad \mu \downarrow$

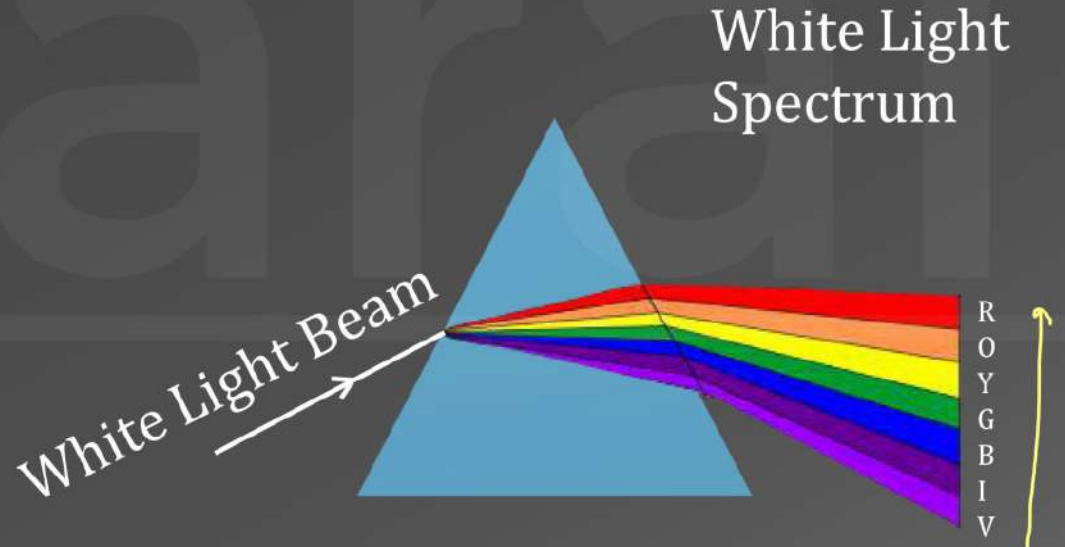
$\lambda_{min}$   
 $\mu_{max}$

$\lambda_{max}$   
 $\mu_{min}$

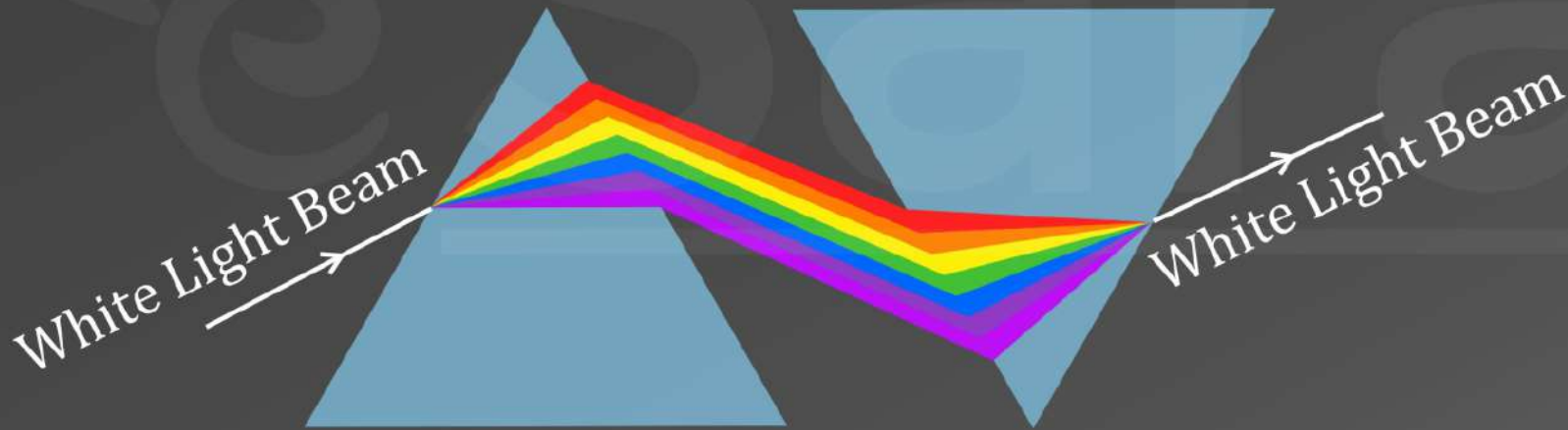
V I B G Y O R

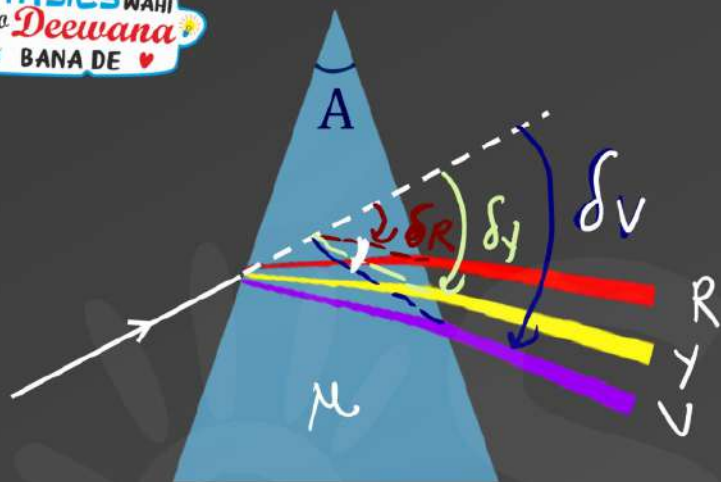
Most  
deviation

Least  
deviation



Achromatic Combination





$$\delta_V = (\mu_V - 1)A$$

$$\delta = (\mu - 1)A$$

$$\delta_Y = (\mu_Y - 1)A$$

$$\delta_R = (\mu_R - 1)A$$

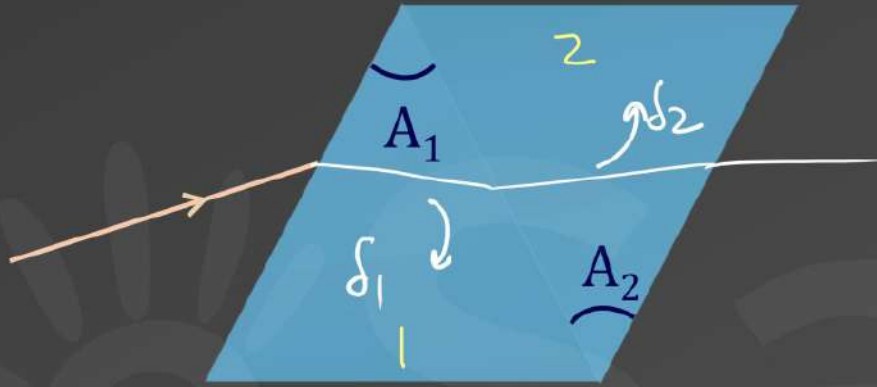
$$\mu_Y \approx \frac{\mu_V + \mu_R}{2}$$

$$\begin{aligned} \text{Angular dispersion } (\theta) &= \delta_V - \delta_R \\ &= (\mu_V - \mu_R) A \end{aligned}$$

$\theta$  is property of prism but  
 $\omega$  is property of material.

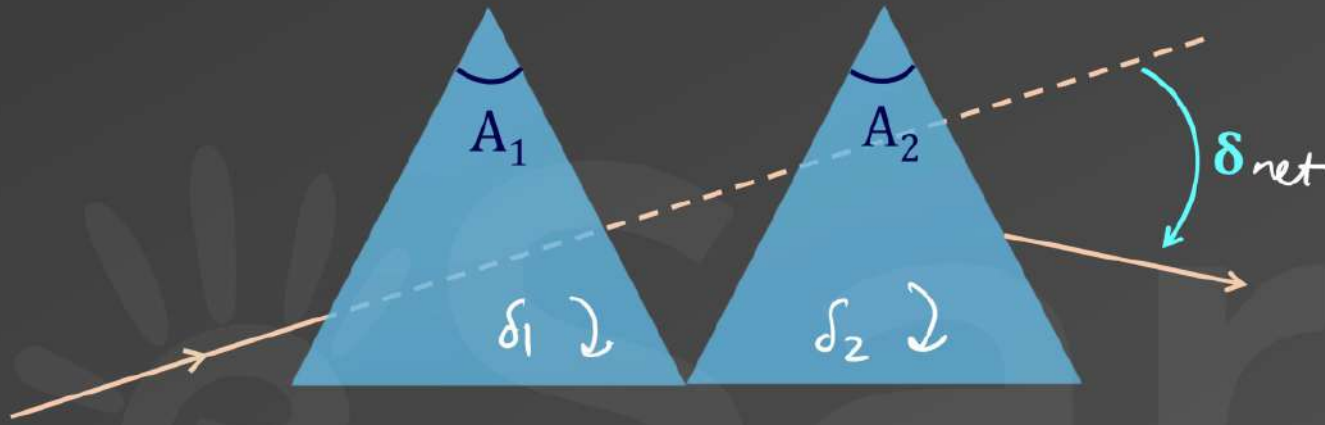
$$\text{Average deviation} = \delta_Y = (\mu_Y - 1)A$$

$$\text{Dispersive power } \omega = \frac{\theta}{\delta_Y} = \frac{(\mu_V - \mu_R)A}{(\mu_Y - 1)A}$$



$$\delta_{\text{net}} = \delta_1 - \delta_2$$

$$\theta_{\text{net}} = \theta_1 - \theta_2$$



$$\delta_{net} = \delta_1 + \delta_2$$

$$\theta_{net} = \theta_1 + \theta_2$$

Dispersion But Not Average Deviation       $\delta_{\text{net}} = 0$

Average Deviation But No Dispersion       $\theta_{\text{net}} = 0$

Achromatic Combination

$$\frac{w_1}{f_{x_1}} + \frac{w_2}{f_{x_2}} = 0$$



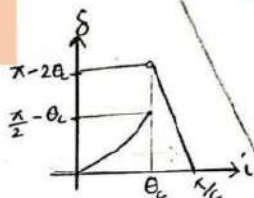


# QUIZ TIME

Total Internal Reflection

1

Angle of Deviation



PRISM

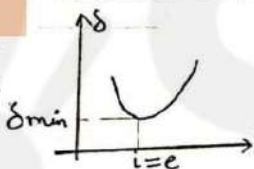
$$A = \delta_1 + \delta_2$$

Angle of Deviation

2

GRAPH b/w L of Deviation & L of Incidence

$$\mu = \frac{\sin\left(\frac{\delta_{\min} + A}{2}\right)}{\sin\left(\frac{A}{2}\right)}$$



Maximum L of Deviation

$$\delta_{\max} = i_g + 90 - A$$

Thin Prism

$$\delta = (\mu - 1)A$$

Refraction from Curved Surface

$$\frac{\mu_r}{v} - \frac{\mu_i}{u} = \frac{\mu_r - \mu_i}{R}$$

Transverse Magnification

$$m = \frac{h_i}{h_o} = \frac{v/\mu_r}{u/\mu_i}$$

Longitudinal Magnification in Lens

5

Velocity of Image

Power of Lens =  $P = 1/f$

Achromatic Combination

$$\frac{\omega_1}{f_1} + \frac{\omega_2}{f_2} = 0$$

REFRACTION

LENS

3

Lens Maker's formula

$$\text{Lens Formula} = \frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$

REFRACTIVE INDEX OF MEDIUM

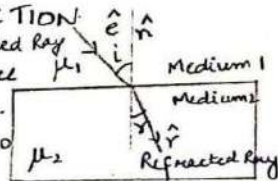
$$\mu = \frac{c}{v_m} \rightarrow \text{Speed of Light in Vacuum}$$

$$v_m \rightarrow \text{Speed of Light in Medium}$$

$$v_m = f \lambda_m \Rightarrow \frac{v_1}{v_2} = \frac{\lambda_1}{\lambda_2} = \frac{\mu_2}{\mu_1} \left[ \text{frequency same} \right]$$

LAWS OF REFRACTION

1) Incident Ray, Refracted Ray and normal to Surface always lie in same plane.  $[\hat{e} \hat{n} \hat{r}] = 0 \Rightarrow [\hat{e} \times \hat{n}] \cdot \hat{r} = 0$



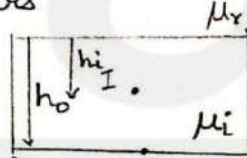
2. SNELL'S LAW

$$\mu_1 \sin i = \mu_2 \sin r$$

Atmospheric Refraction

1. Early Sunrise & Delayed Sunset
2. Apparent flattening of Sun at Sunrise and Sunset
3. Twinkling of Stars

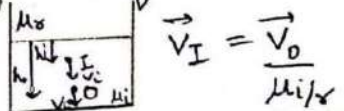
APPARENT DEPTH



4

$$\text{Shift} = h_o \left(1 - \frac{1}{\mu_i/\mu_r}\right)$$

Velocity of Image formed due to Refraction from Plane Surface



$$\vec{v}_I = \frac{\vec{v}_O}{\mu_i/\mu_r}$$

Refraction through Parallel Slab

$$\text{SHIFT} = t \left(1 - \frac{1}{\mu_s/\mu_m}\right)$$

LENS kept Very close to Each other

$$\frac{1}{f_{eq}} = \frac{1}{f_1} + \frac{1}{f_2} + \frac{1}{f_3} + \dots$$

$$P_{eq} = P_1 + P_2 + P_3 + \dots \text{ (with sign)}$$

Silvering of Lens

$$P_{eq} = P_L + P_m + P_R$$

$$P_{eq} = \frac{1}{f_L} - \frac{1}{f_m} + \frac{1}{f_R} = -\frac{1}{f_{eq}}$$

Dispersion

Cauchy's eq<sup>n</sup>

$$\mu = A + \frac{B}{\lambda^2} \quad \uparrow \mu \downarrow \lambda$$

Most Deviation Least Deviation

THIN PRISM

$$\mu_y \approx \frac{\mu_v + \mu_r}{2}$$

Angular Dispersion (theta)

$$= \delta_v - \delta_r = (\mu_v - \mu_r) A$$

$$\text{Avg. Deviation} = \delta_y = (\mu_y - 1) A$$

$$\text{Dispersive Power} = \frac{\theta}{\delta_y} = \frac{(\mu_v - \mu_r) A}{(\mu_y - 1) A}$$

theta is property of Prism  
omega is property of material

Dispersion but not Avg Deviation

$$\delta_{net} = 0$$

Avg Deviation but Not Dispersion

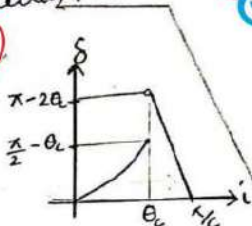
$$\theta_{net} = 0$$

Q  
U  
I  
Z

Total Internal Reflection

$\sin \theta_c = \frac{1}{\mu}$

Angle of Deviation



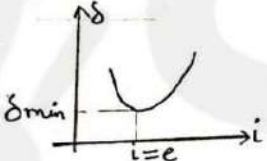
PRISM

$A = r_1 + r_2$

Angle of Deviation

$\delta = i + e - A$

GRAPH b/w L of Deviation & L of Incidence



$\mu = \frac{\sin(\frac{\delta_{min} + A}{2})}{\sin(\frac{A}{2})}$

Maximum L of Deviation

$\delta_{max} = i_g + 90 - A$

Thin Prism

$\delta = (\mu - 1)A$

Refraction from Curved Surface

$\frac{\mu_r}{v} - \frac{\mu_i}{u} = \frac{\mu_r - \mu_i}{R}$

Transverse Magnification

$m = \frac{h_I}{h_o} = \frac{v/\mu_r}{u/\mu_i}$

Longitudinal Magnification in Lens  $\Rightarrow LM = m^2$

Velocity of Image  $< \vec{V}_I = m^2 \vec{V}_o$

Power of Lens =  $P = 1/f$

Achromatic Combination

$\frac{\omega_1}{f_{v1}} + \frac{\omega_2}{f_{v2}} = 0$

REFRACTION

REFRACTIVE INDEX OF MEDIUM

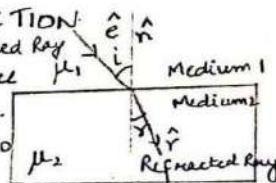
$\mu = \frac{c}{v_m} \rightarrow$  Speed of Light in Vacuum  
 $v_m \rightarrow$  Speed of Light in Medium

$v_m = f \lambda_m \Rightarrow \frac{v_1}{v_2} = \frac{\lambda_1}{\lambda_2} = \frac{\mu_2}{\mu_1}$  [frequency same]

LAWS OF REFRACTION

1) Incident Ray, Refracted Ray and normal to Surface always lie in same plane.

$[\hat{e} \hat{n} \hat{r}] = 0 \Rightarrow [\hat{e} \times \hat{n}] \cdot \hat{r} = 0$



2. SNELL'S LAW

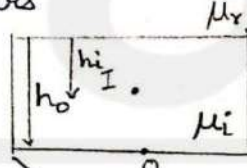
$\mu_1 \sin i = \mu_2 \sin r$

Atmospheric Refraction

- 1. Early Sunrise & Delayed Sunset
- 2. Apparent flattening of Sun at Sunrise and Sunset
- 3. Twinkling of Stars

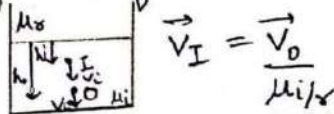
APPARENT DEPTH

$h_I = \frac{h_o}{\mu_{i/s}}$



Shift =  $h_o (1 - \frac{1}{\mu_{i/s}})$

Velocity of Image formed due to Refraction from Plane Surface



$\vec{V}_I = \frac{\vec{V}_o}{\mu_{i/s}}$

Refraction through Parallel Slab SHIFT =  $t (1 - \frac{1}{\mu_{s/m}})$

LENS kept Very close to Each other

$\frac{1}{f_{eq}} = \frac{1}{f_1} + \frac{1}{f_2} + \dots$

$P_{eq} = P_1 + P_2 + P_3 + \dots$  (with sign)

Silvering of Lens

$P_{eq} = P_L + P_m + P_L$

$P_{eq} = \frac{1}{f_1} - \frac{1}{f_m} + \frac{1}{f_2} = -\frac{1}{f_{eq}}$

Dispersion

Cauchy's eqn

$\mu = A + \frac{B}{\lambda^2}$   $\uparrow \mu \downarrow \lambda$

Most Deviation  $\downarrow$  Least Deviation  $\uparrow$

THIN PRISM

$\mu_y \approx \frac{\mu_v + \mu_r}{2}$

Angular Dispersion ( $\theta$ )

$= \delta_v - \delta_r = (\mu_v - \mu_r) A$

Avg. Deviation =  $\delta_y = (\mu_y - 1) A$

Dispersive Power =  $\frac{\theta}{\delta_y} = \frac{(\mu_v - \mu_r) A}{(\mu_y - 1) A}$

$\theta$  is property of Prism  
 $\omega$  is property of material

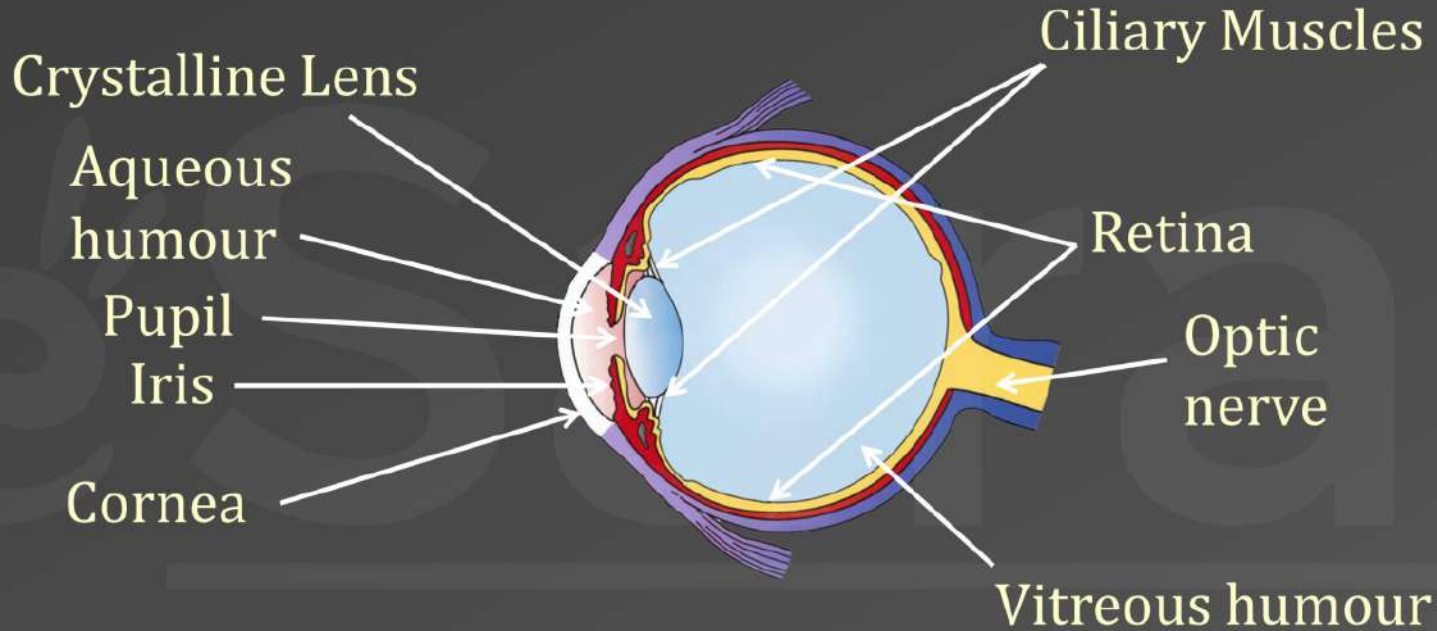
Dispersion but not Avg Deviation

$\delta_{net} = 0$

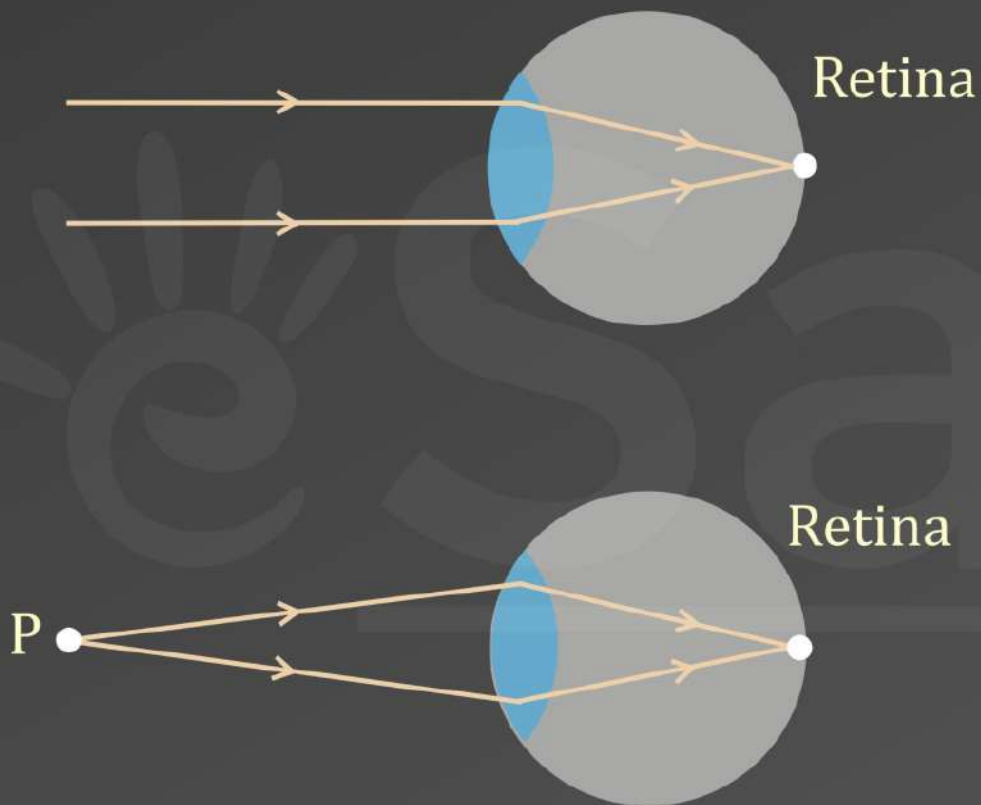
Avg Deviation but Not Dispersion

$\theta_{net} = 0$

# Human Eye



# Human Eye



Accommodation

Far Point at  $\infty$

Near Point at 25cm

Least Distance for  
Distinct Vision

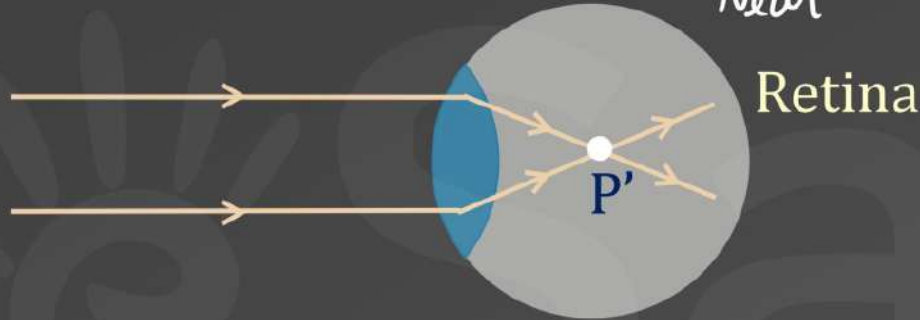


## 1. Nearsightedness : (Myopia)

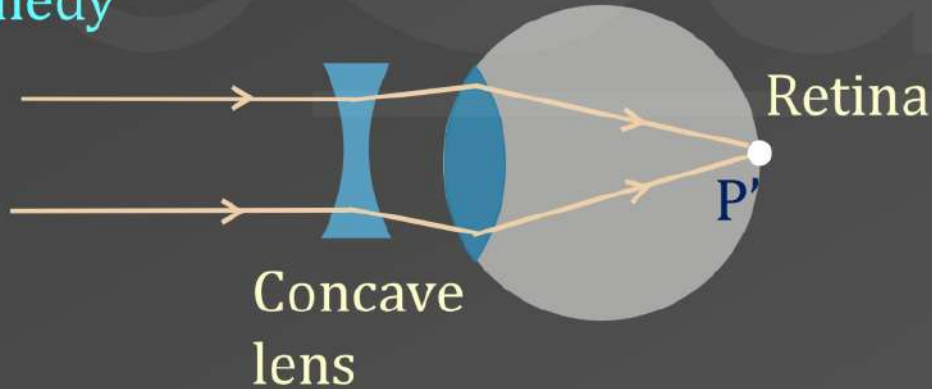
✓ पास  
Near

✗ दूर  
Far

TRICK



Remedy



# Defects of Eyes

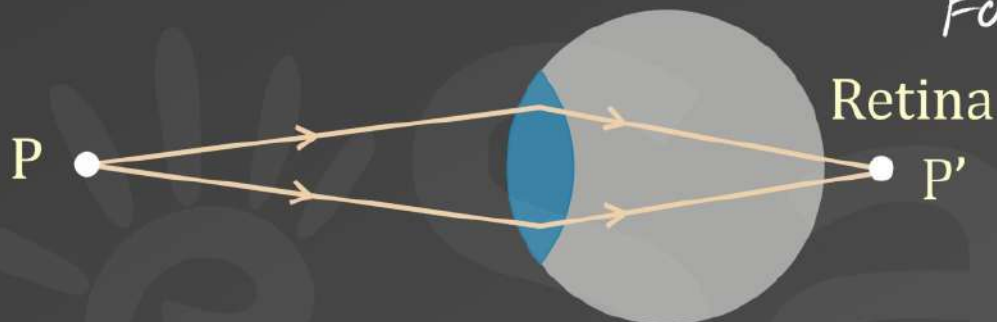


## 2. Farsightedness : (Hypermetropia)

✓  
दूर  
Far

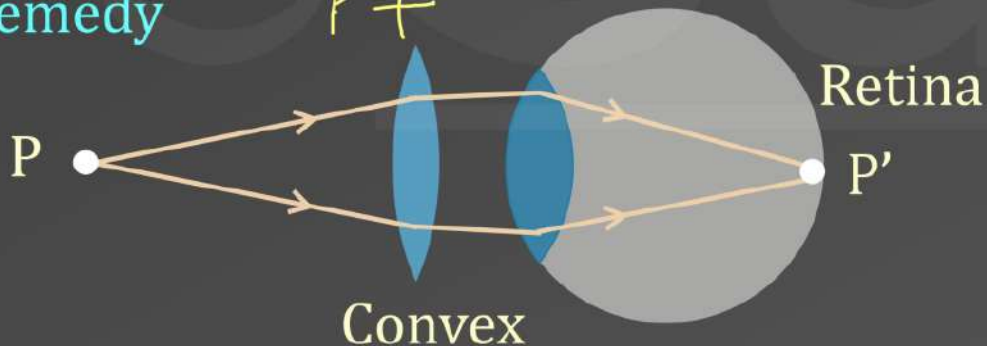
✗  
पास  
Near

TRICK

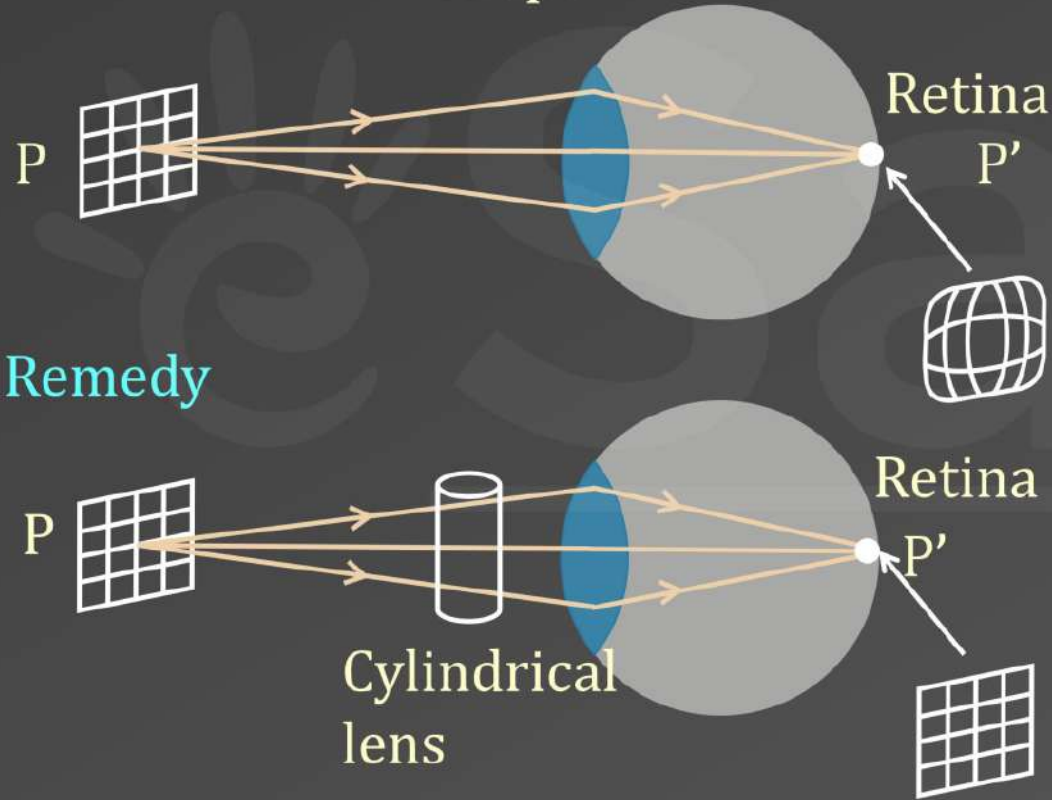


Remedy

P +



3. Astigmatism: When Cornea not spherical in shape



Remedy

Cylindrical lens





In old age Near Point of eyes may increase to as much as 200cm. This defect of eye is called Presbyopia.



Image at  $\infty$  (Normal Adjustment)

Angular Magnification =  $\frac{D}{f}$

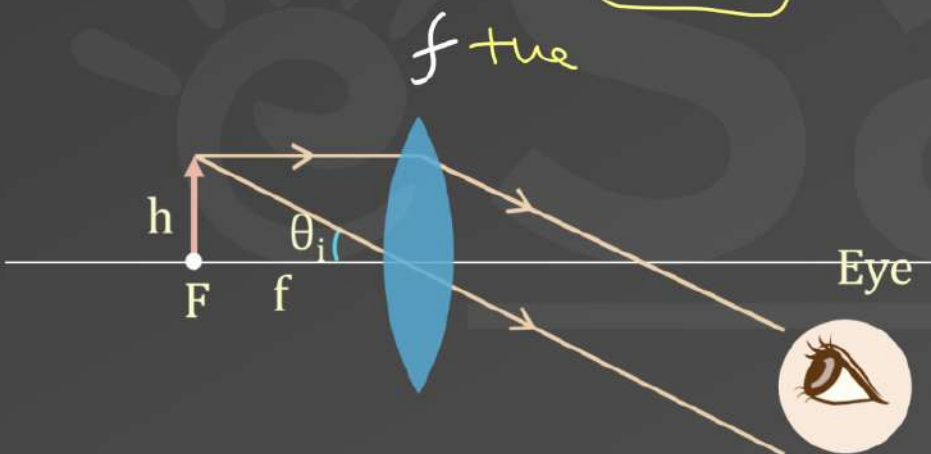
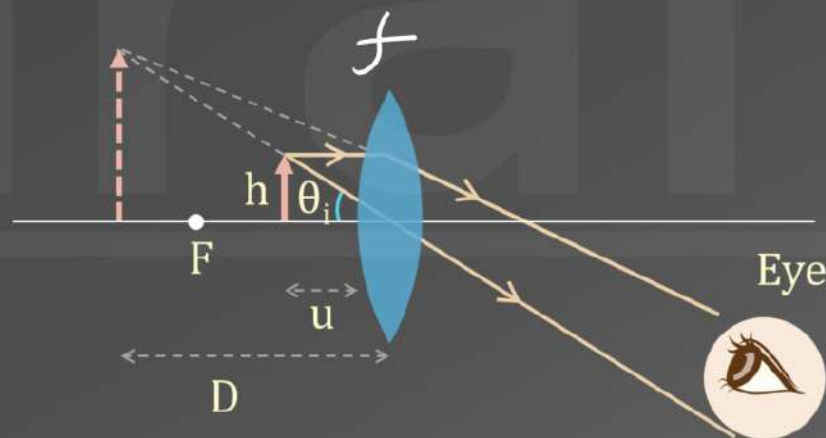


Image at Least Distance of Distinct Vision

Angular Magnification =  $\frac{D}{f} + 1$



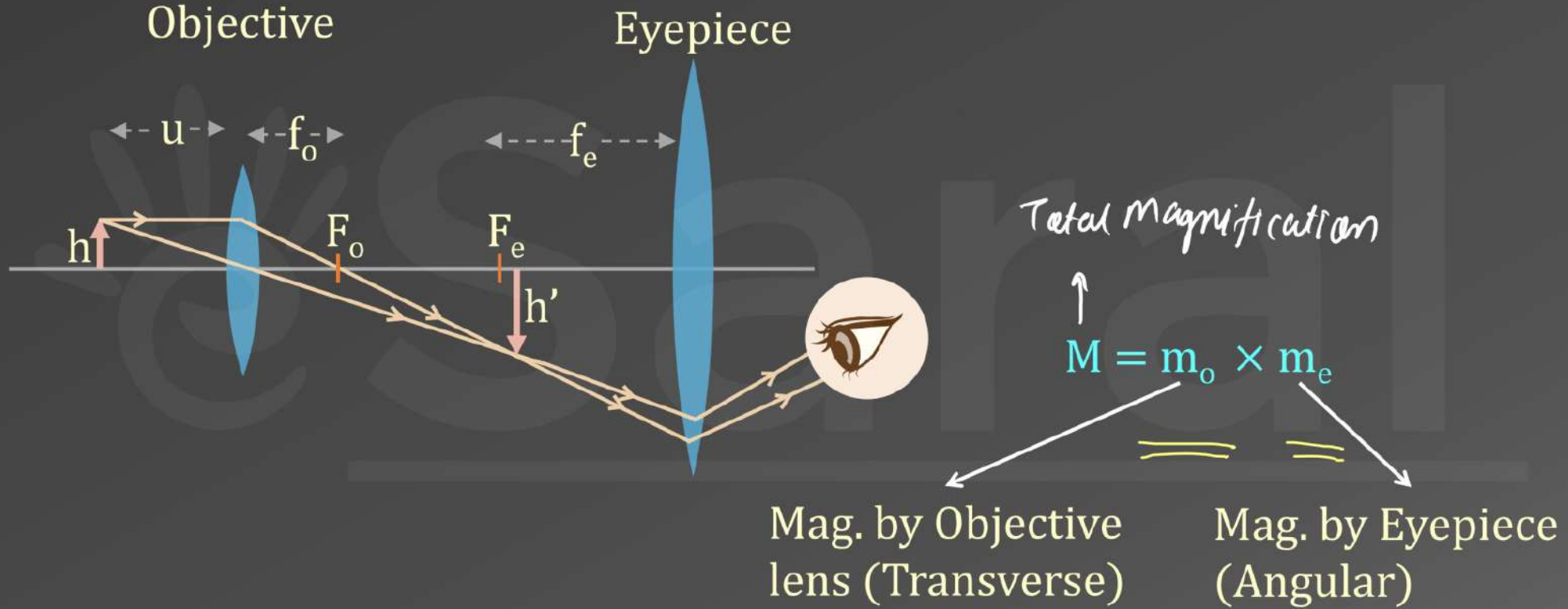


Image at  $\infty$  (Normal Adjustment)

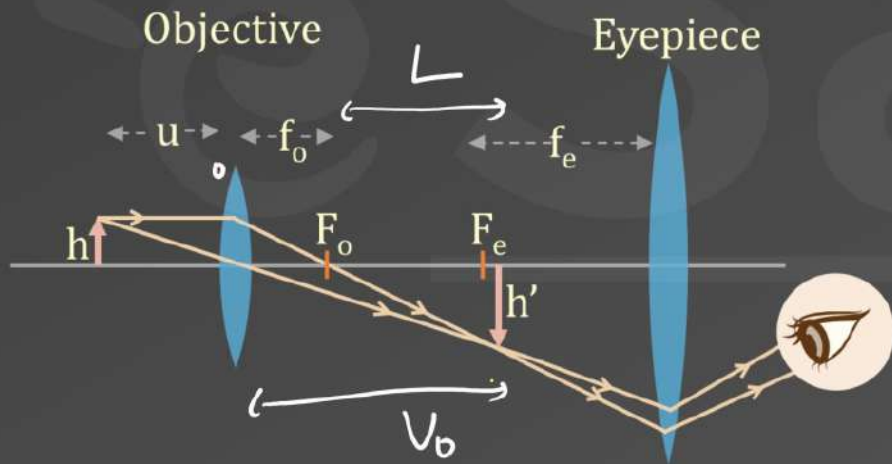
Tube length of Comp Micro.

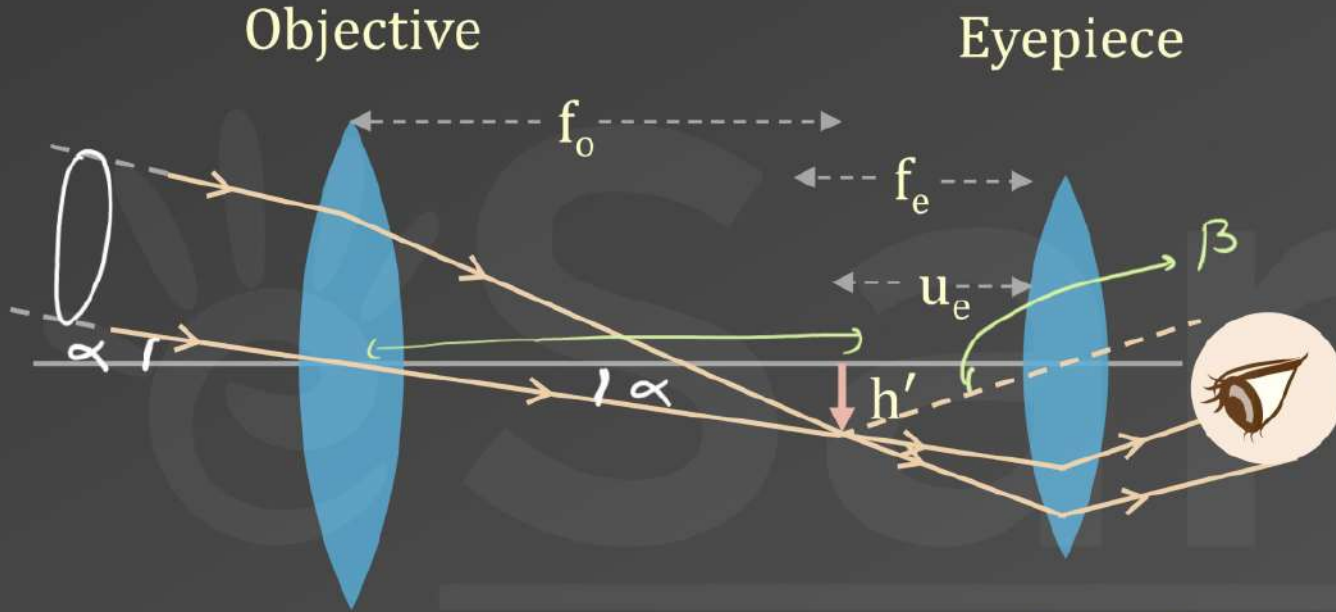
Total Magnification =

$$\frac{L}{f_o} \frac{D}{f_e}$$

Image at Least Distance of Distinct Vision

$$\text{Total Magnification} = \left| \frac{v_o}{u_o} \right| \left( \frac{D}{f_e} + 1 \right)$$





$$\text{Magnifying Power} = \frac{\beta}{\alpha} = \boxed{\frac{f_o}{|u_e|}}$$

Image at  $\infty$  (Normal Adjustment)

Magnifying Power =  $\frac{f_o}{f_e}$

In this case length of telescope tube is  $f_o + f_e$

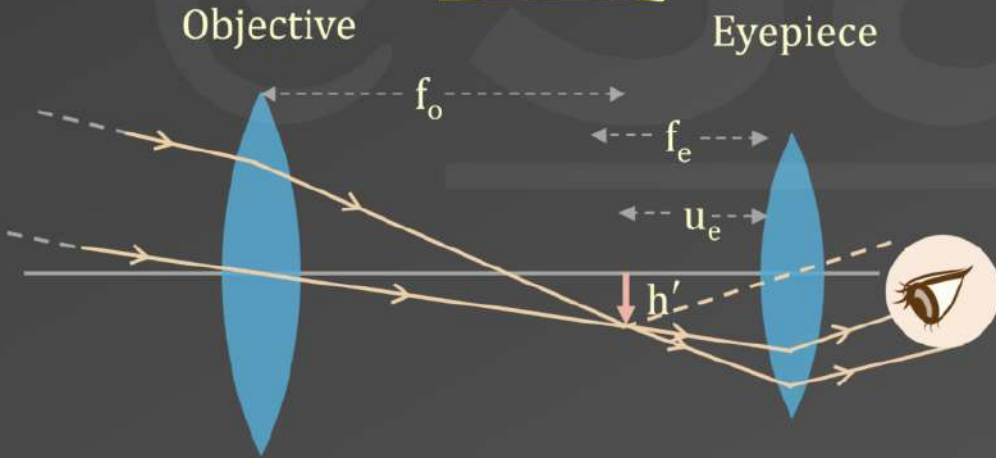
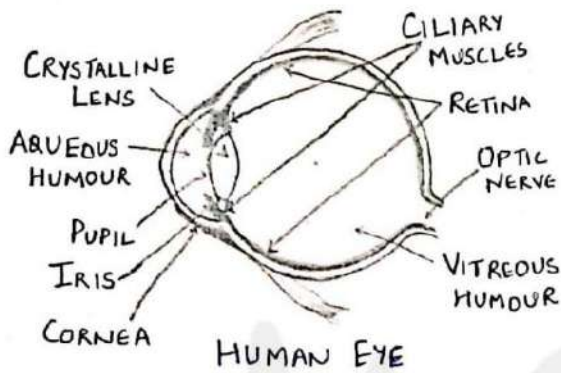


Image at Least Distance of Distinct Vision

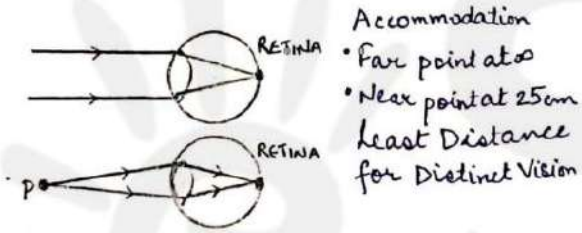
Magnifying Power =  $f_o \left( \frac{1}{f_e} + \frac{1}{D} \right)$

$\frac{f_o}{f_e} + \frac{f_o}{D}$

# QUIZ TIME



HUMAN EYE

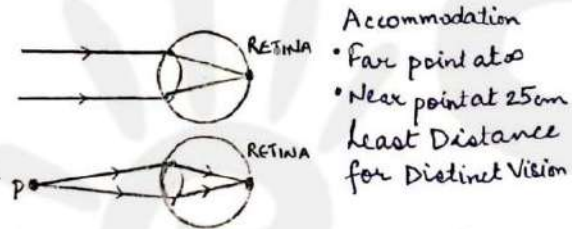
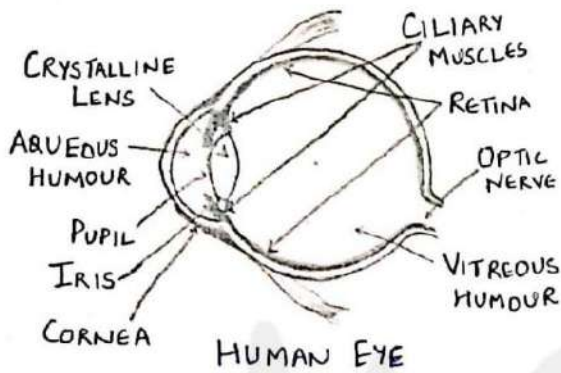


## OPTICAL INSTRUMENTS

DEFECTS OF EYES	REMEDY
1. NEARSIGHTEDNESS: (MYOPIA) 	
2. FARSIGHTEDNESS: (HYPERMETROPIA) 	
3. ASTIGMATISM: 	
4. PRESBYOPIA: In old age, Near point increases to as much 200cm.	

INSTRUMENT	IMAGE AT $\infty$ (Normal Adjustment)	IMAGE at Least Distance of Distinct Vision
1. SIMPLE MICROSCOPE 	Angular Magnification <div style="text-align: center; background-color: #f4a460; padding: 5px;"><b>1</b></div>	Angular Magnification <div style="text-align: center; background-color: #f4a460; padding: 5px;"><b>2</b></div>
2. COMPOUND MICROSCOPE 	Total Magnification, $M = m_o \times m_e$ <div style="text-align: center; background-color: #f4a460; padding: 5px;"><b>3</b></div>	Total Magnification $= \left  \frac{v_o}{u_o} \right  \left( \frac{D}{f_e} + 1 \right)$
3. TELESCOPE 	Magnifying Power = $\beta_x = \left  \frac{f_o}{f_e} \right $ In this case, <div style="text-align: center; background-color: #f4a460; padding: 5px;"><b>4</b></div> Length of Telescope is $f_o + f_e$	Magnifying Power $= f_o \left( \frac{1}{f_e} + \frac{1}{D} \right)$





## OPTICAL INSTRUMENTS

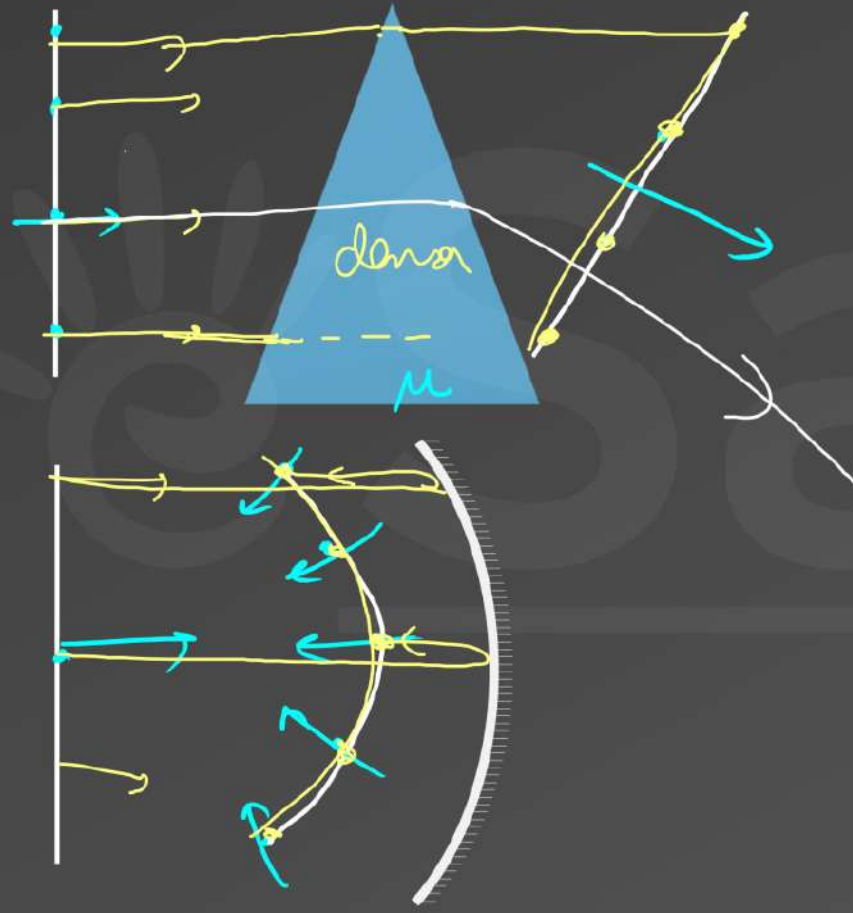
DEFECTS OF EYES	REMEDY
<b>1. NEARSIGHTEDNESS: (MYOPIA)</b> 	
<b>2. FARSIGHTEDNESS: (HYPERMETROPIA)</b> 	
<b>3. ASTIGMATISM:</b> 	
<b>4. PRESBYOPIA:</b> In old age, Near point increases to as much 200cm.	

INSTRUMENT	IMAGE AT ∞ (Normal Adjustment)	IMAGE at Least Distance of Distinct Vision
<b>1. SIMPLE MICROSCOPE</b> 	Angular Magnification $= \frac{D}{f}$	Angular Magnification $= \frac{D}{f} + 1$
<b>2. COMPOUND MICROSCOPE</b> 	Total Magnification, $M = m_o \times m_e$ $= \frac{L}{f_o} \frac{D}{f_e}$	Total Magnification $= \left  \frac{v_o}{u_o} \right  \left( \frac{D}{f_e} + 1 \right)$
<b>3. TELESCOPE</b> 	Magnifying Power = $\beta_x = \left  \frac{f_o}{f_e} \right $ $= \frac{f_o}{f_e}$ In this case, Length of Telescope is $f_o + f_e$	Magnifying Power $= f_o \left( \frac{1}{f_e} + \frac{1}{D} \right)$

# Wave Optics

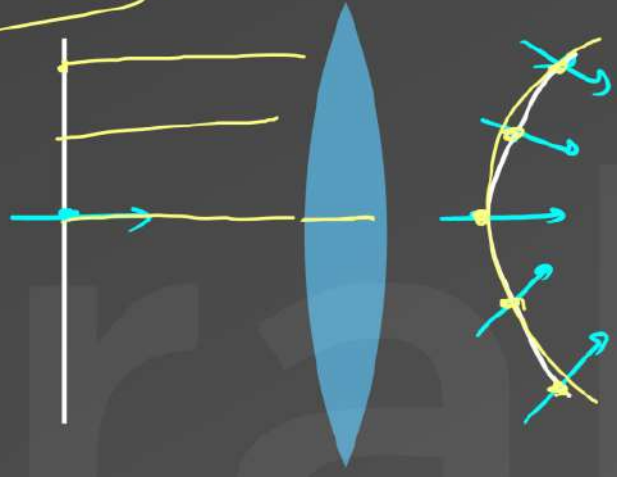
## Superfast Revision

# Huygens Principle



TRICK

5  
people



Two sources are said to be Coherent if they produce waves having constant (with respect to time) phase difference.

For Incoherent sources, phase difference varies with time.

Two independent ordinary sources (like lamps) are incoherent sources.

# Interference of Waves



$$y_1 = A_1 \sin(kx - \omega t)$$

$$y_2 = A_2 \sin(kx - \omega t + \phi)$$

$$(A_{\text{res}})^2 = A_1^2 + A_2^2 + 2 A_1 A_2 \cos \phi$$

$$I \propto A^2$$

$$I_{\text{res}} = I_1 + I_2 + 2\sqrt{I_1}\sqrt{I_2} \cos \phi$$

If  $I_1 = I_2 = I_0$ , then

$$I_{\text{res}} = 4I_0 \cos^2\left(\frac{\phi}{2}\right)$$

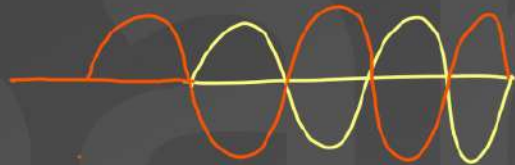
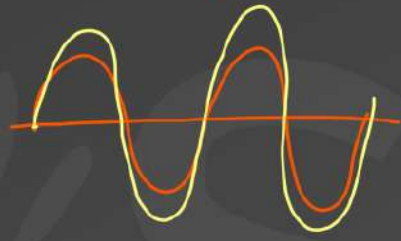


## Constructive Interference

$$\cos\phi = 1$$

$$\phi = 2n\pi$$

$$A_{\max} = (A_1 + A_2)$$



$$I_{\max} = (\sqrt{I_1} + \sqrt{I_2})^2$$

$$I_{\max} = \underline{\underline{4I_0}} \text{ (If same source of } I_0)$$

$$\underline{\underline{\Delta x = 0, \lambda, 2\lambda, 3\lambda\dots}} = \underline{\underline{n\lambda}}$$

## Destructive Interference

$$\cos\phi = -1$$

$$\phi = (2n + 1)\pi$$

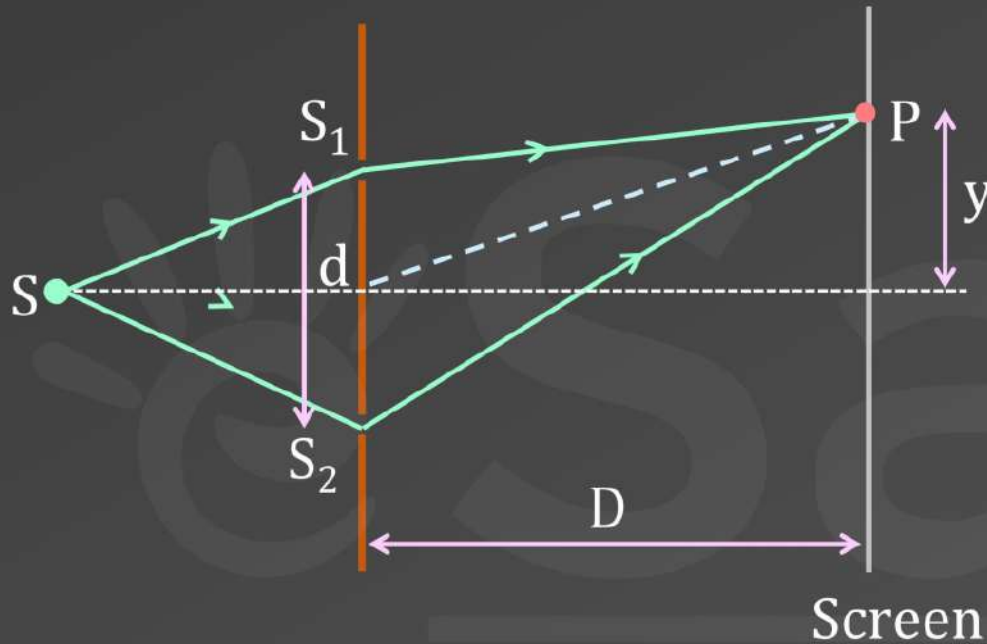
$$A_{\min} = (A_1 - A_2)$$

$$I_{\min} = (\sqrt{I_1} - \sqrt{I_2})^2$$

$$I_{\min} = \underline{\underline{0}} \text{ (If same source of } I_0)$$

$$\Delta x = 0.5\lambda, 1.5\lambda, 2.5\lambda\dots = \left(n + \frac{1}{2}\right)\lambda$$

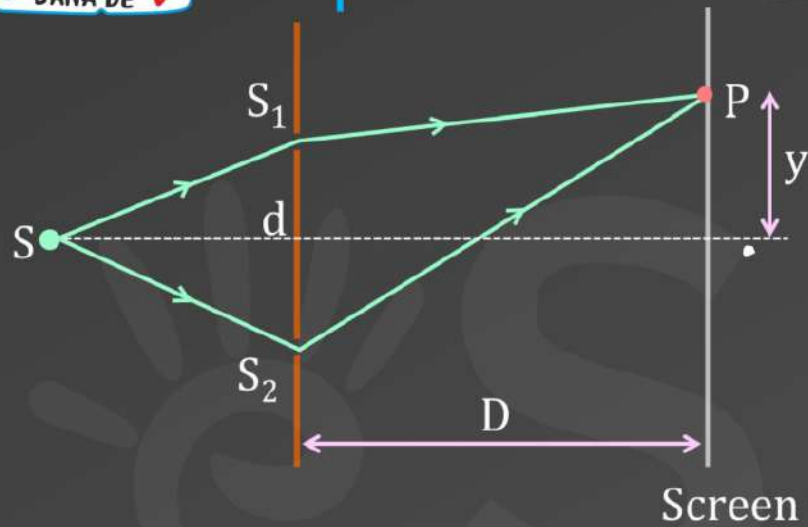
# Young's Double Slit Experiment (YDSE)



$$\Delta x = \frac{yd}{D}$$

$d$  is distance between slits  $S_1$  and  $S_2$   
 $D$  is distance between slit and screen

# Young's Double Slit Experiment (YDSE)



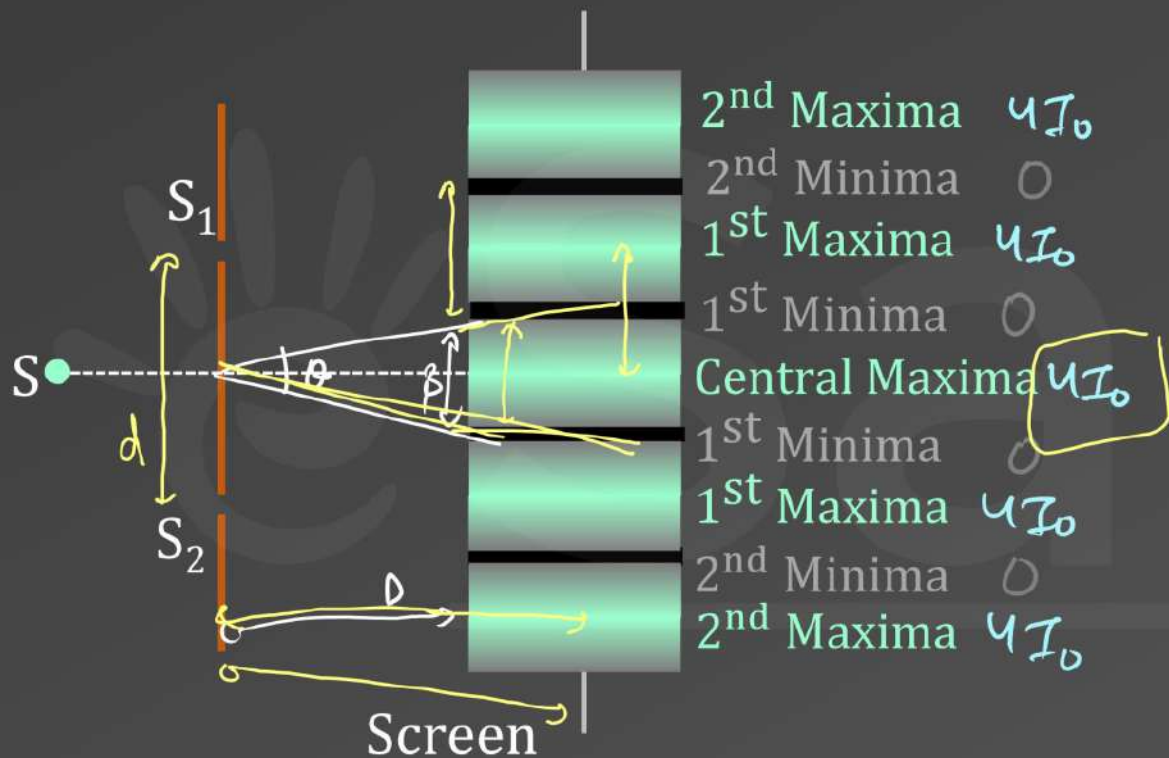
$$\sin \alpha \approx \frac{y}{D}$$

$$y = \frac{\Delta n D}{d}$$

$y = 0$	$\frac{\lambda D}{2d}$	$\frac{\lambda D}{d}$	$\frac{3\lambda D}{2d}$	$\frac{2\lambda D}{d}$
↓	↓	↓	↓	↓
Central Maxima	1 <sup>st</sup> Minima	1 <sup>st</sup> Maxima	2 <sup>nd</sup> Minima	2 <sup>nd</sup> Maxima



# Fringe Width

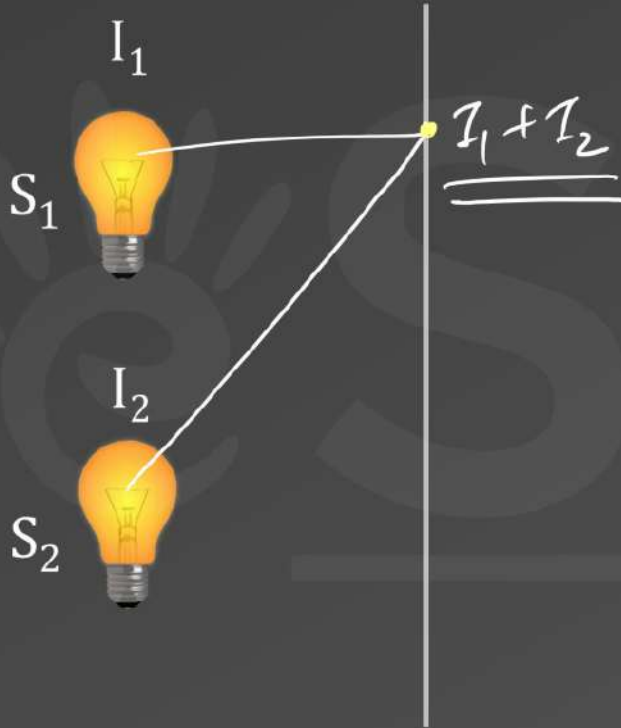


The distance between two successive dark fringes (or bright fringes) is known as Fringe Width ( $\beta$ ).

Fringe Width  $\beta = \frac{\lambda D}{d}$

$$\theta = \frac{\beta}{D} = \frac{\lambda}{d}$$

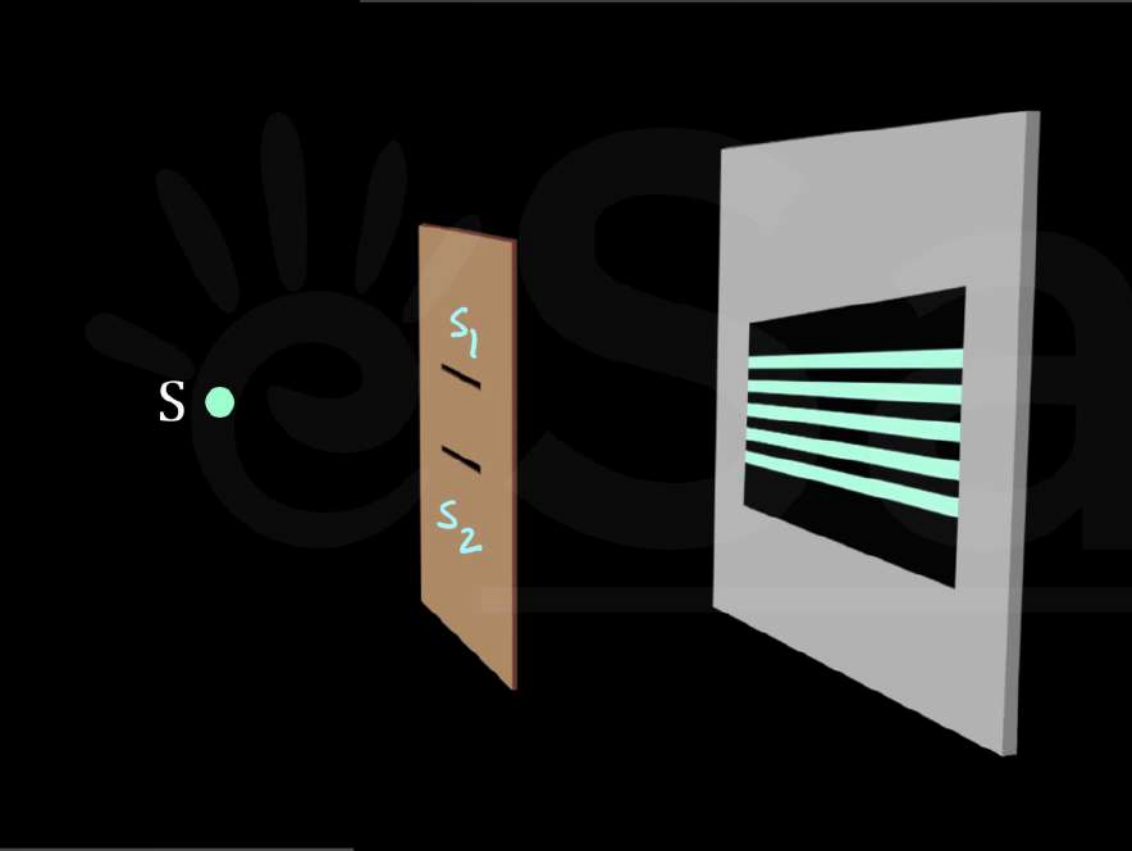
Angular Fringe Width



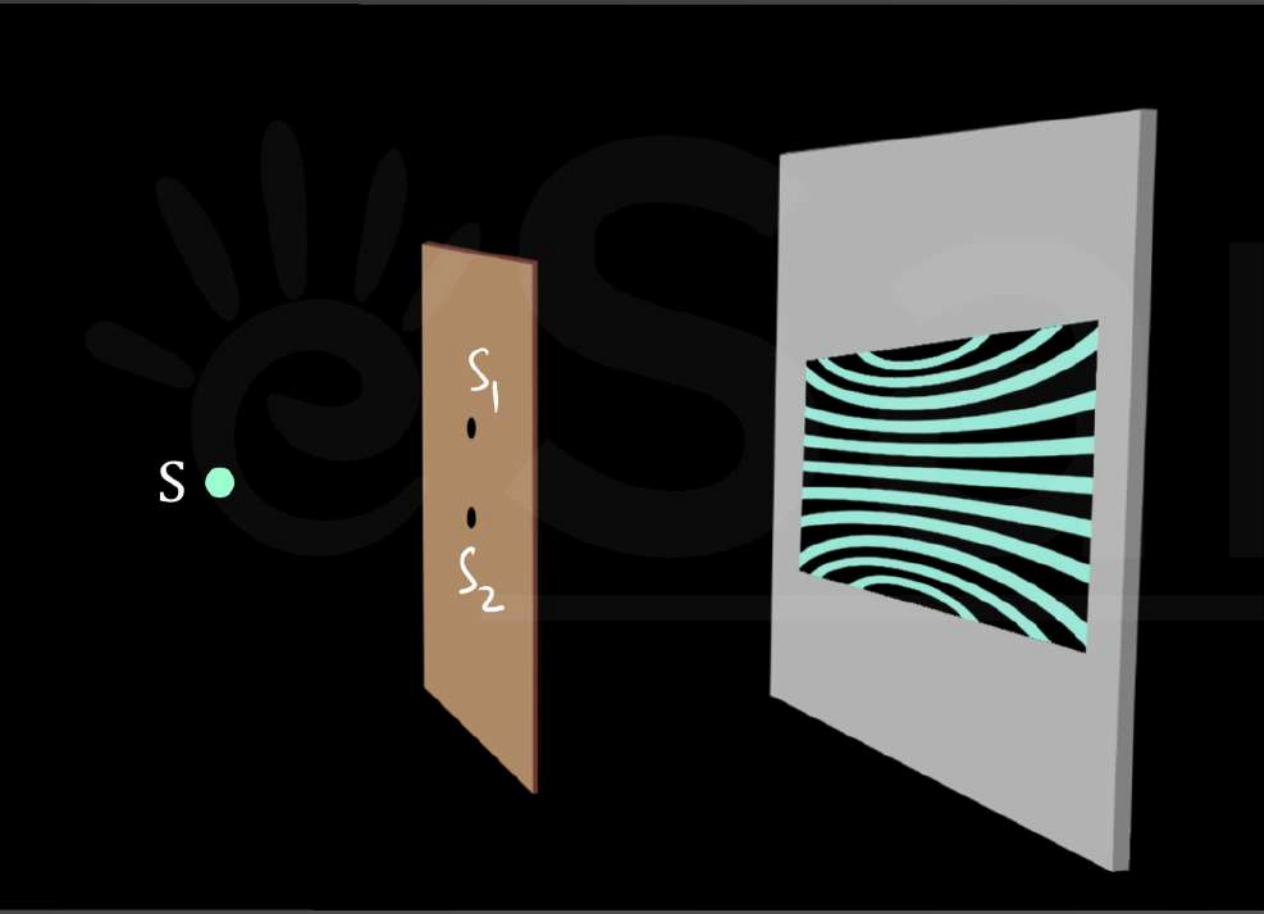
Incoherent Sources

$$I_{\text{res}} = I_1 + I_2$$

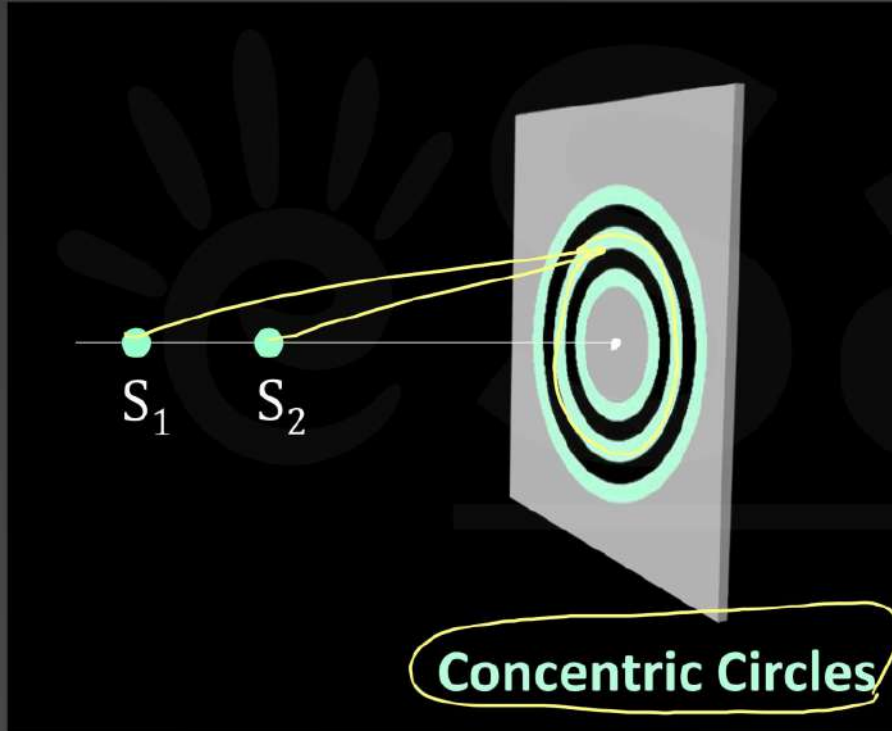
# Shape of Fringes

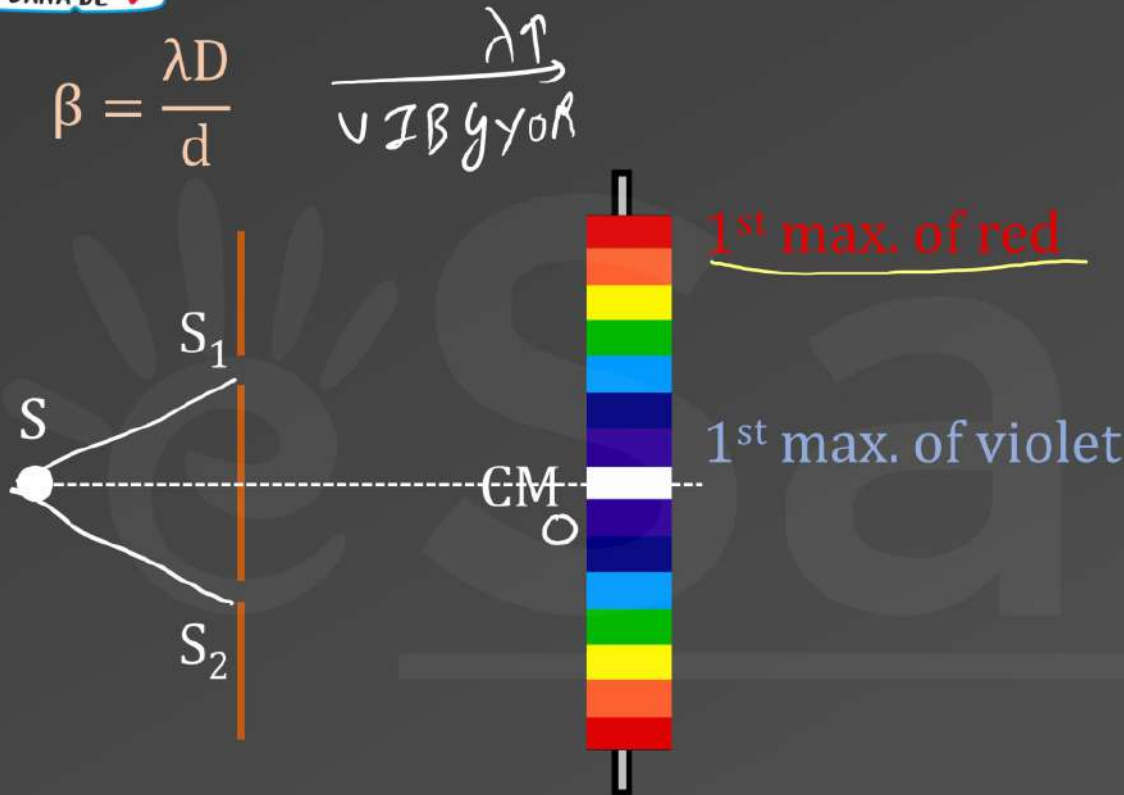


# Shape of Fringes



# Shape of Fringes

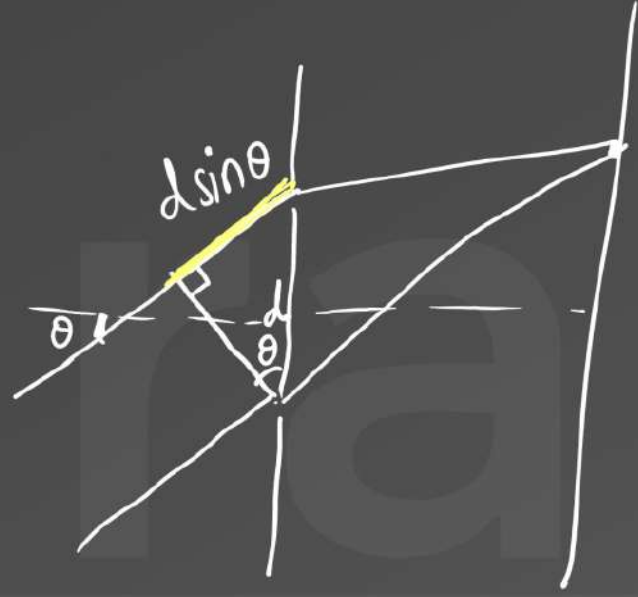
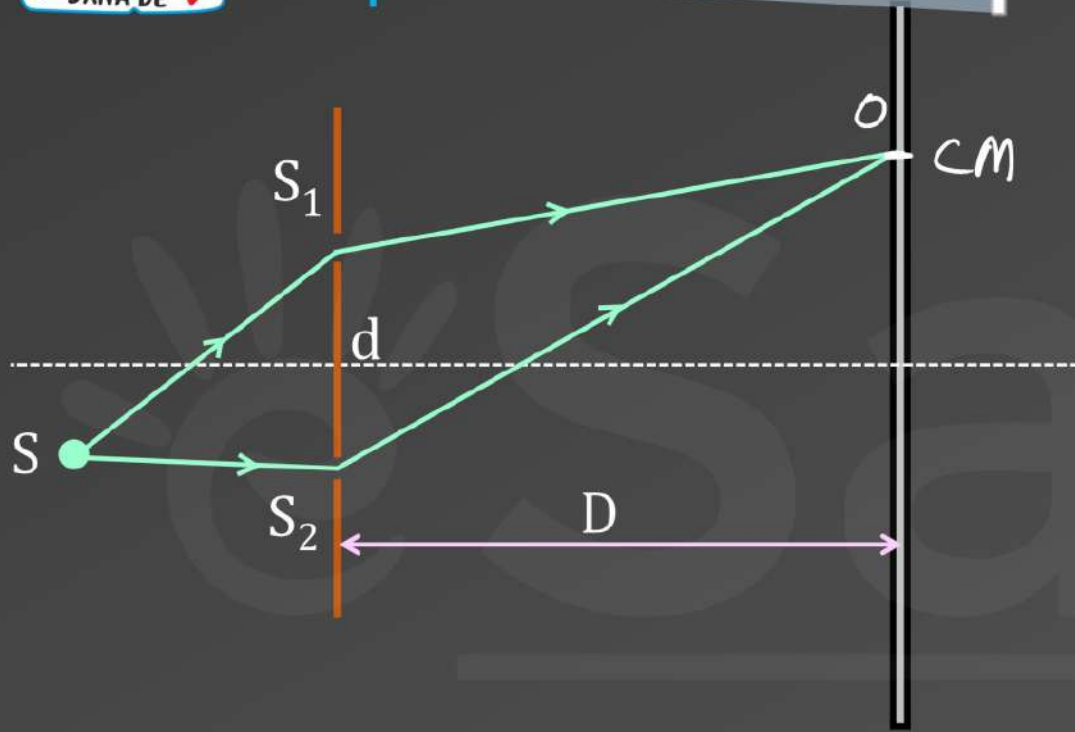




In YDSE with white light, we get a white fringe at central maxima i.e at a point of zero phase difference.

CM is followed by coloured fringes on its both sides.

# Variations in YDSE



In this case CM shifts but fringe width remains same.

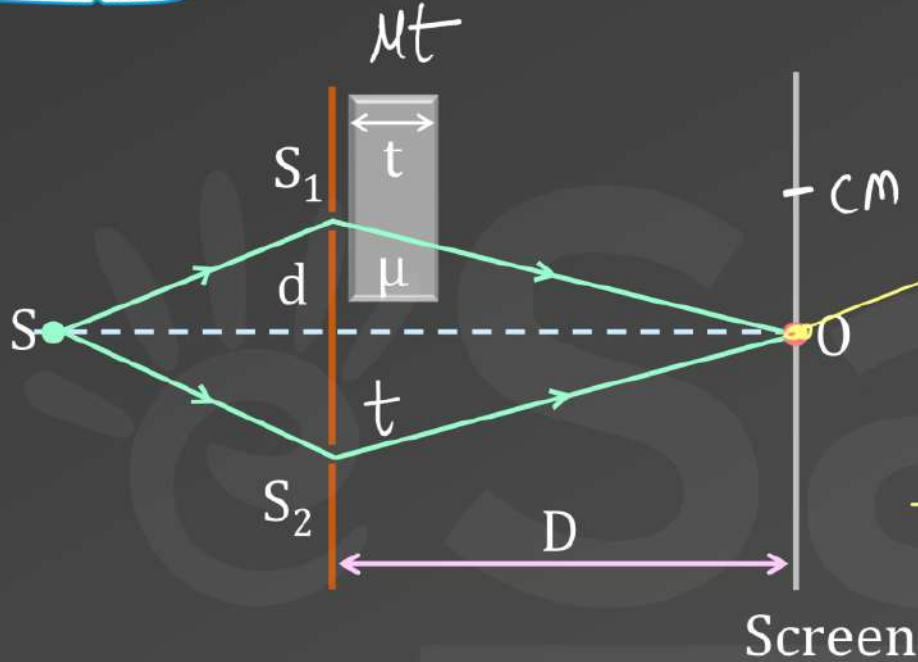
$$\beta = \frac{\lambda D}{d}$$



Optical path =  $\mu t$



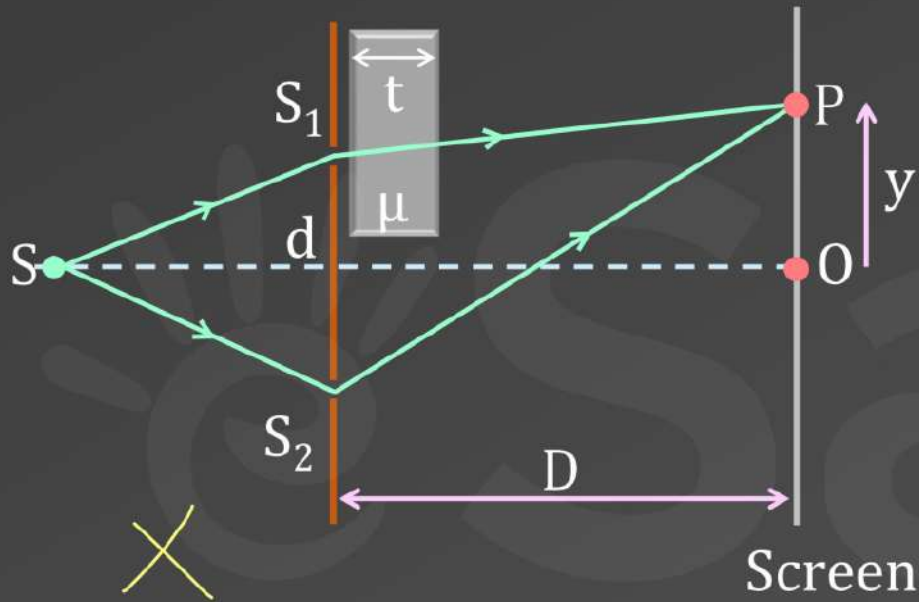
Pattern shifts ↑



Optical Path difference at O

$$\Delta x = (\mu - 1)t$$

$$\beta = \frac{\lambda_{air} D}{d} \rightarrow \text{no change}$$



$$(\Delta x) = (\mu - 1)t - \left(\frac{yd}{D}\right)$$

$$\beta = \frac{\lambda_{air} D}{d} \rightarrow \text{no change}$$

# Thin Film Interference

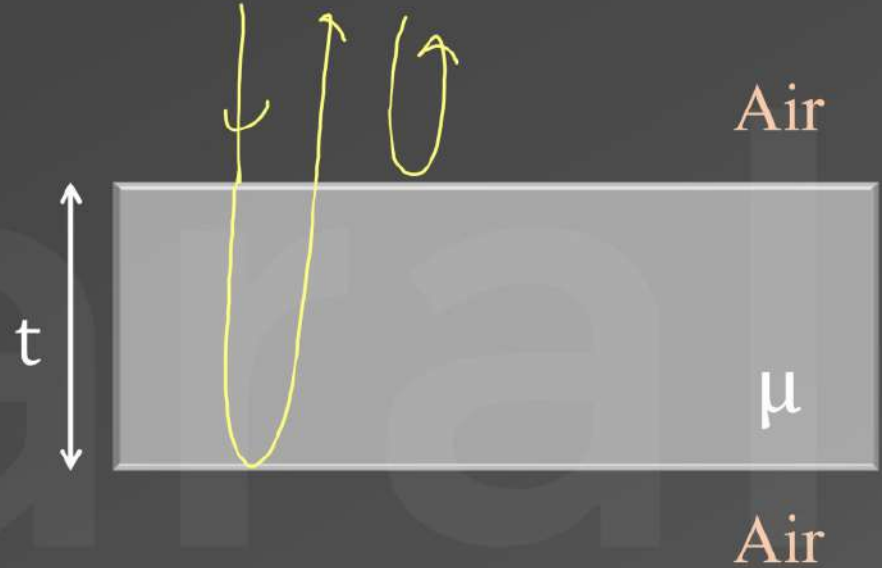


## a) Interference in Reflection

$$(\Delta x)_{\text{opt.}} = \underline{\underline{2\mu t}}$$

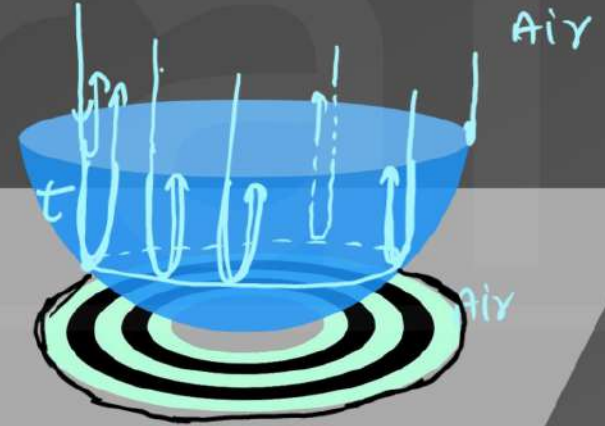
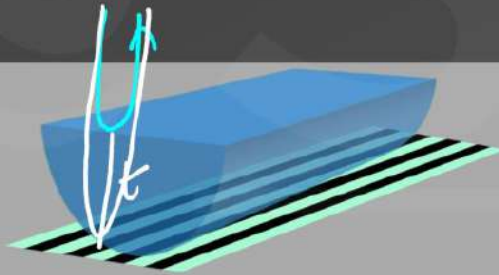
If  $\underline{\underline{2\mu t = n\lambda}}$  Minima

$$2\mu t = \left(n + \frac{1}{2}\right) \lambda \text{ Maxima}$$



# Thin Film Interference

## Newton's Rings

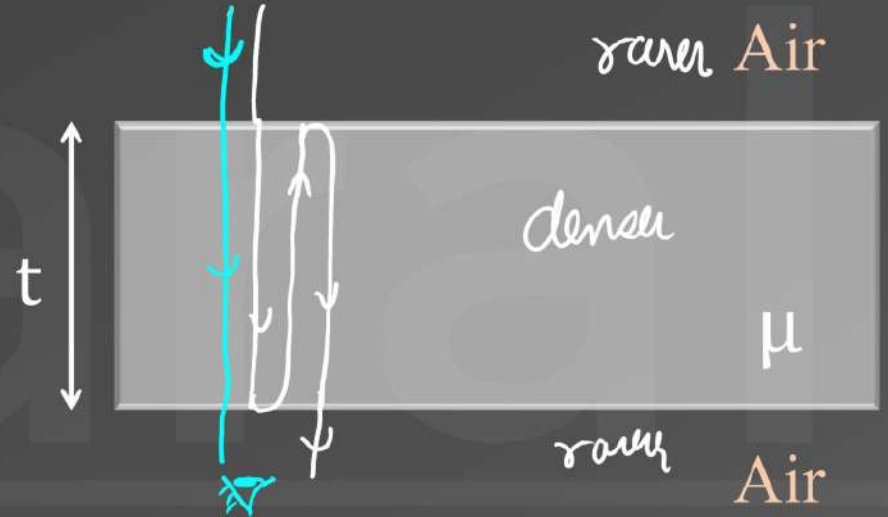


# Thin Film Interference

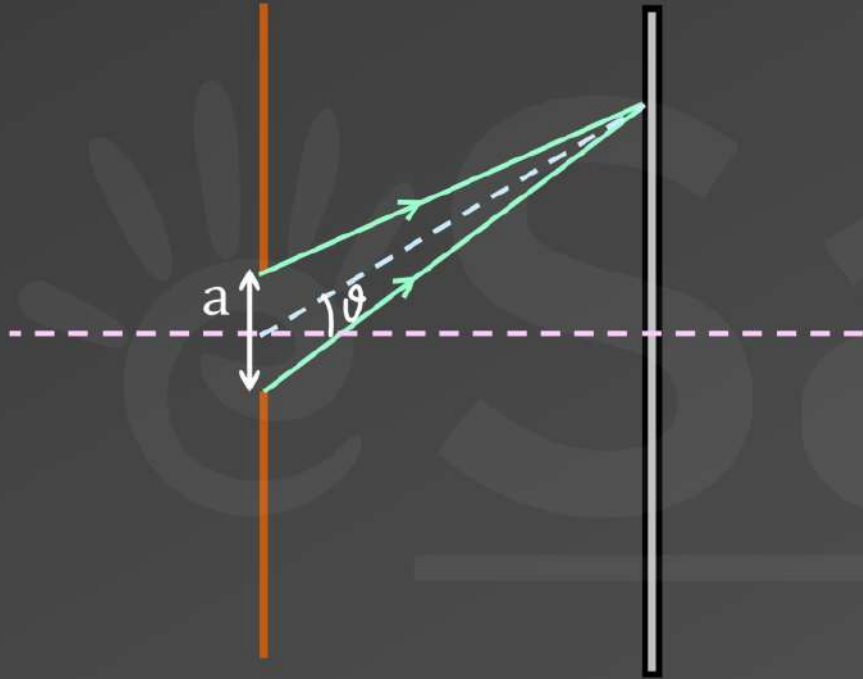
## b) Interference in Transmission

$$2Mt = D\lambda_{opt}$$

$$\begin{matrix} n\lambda_{air} \\ \text{const} \end{matrix} \quad \begin{matrix} (n + \frac{1}{2})\lambda_{air} \\ \text{dest} \end{matrix}$$



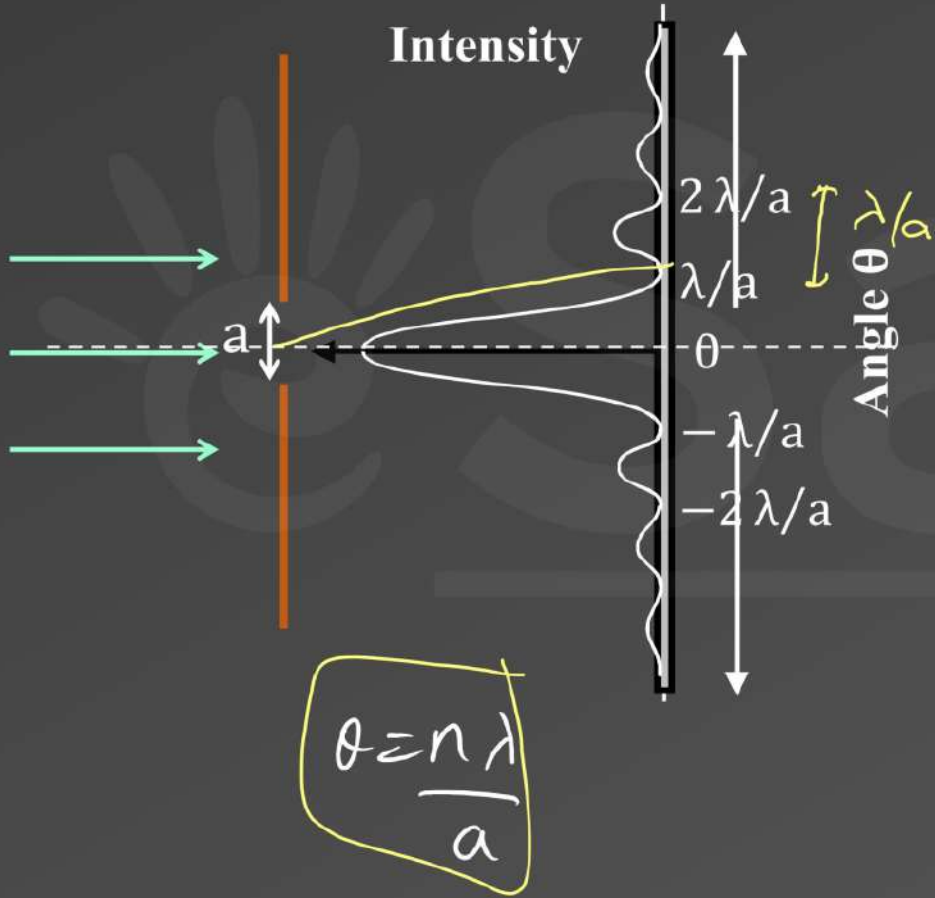
# Diffraction Through Single Slit

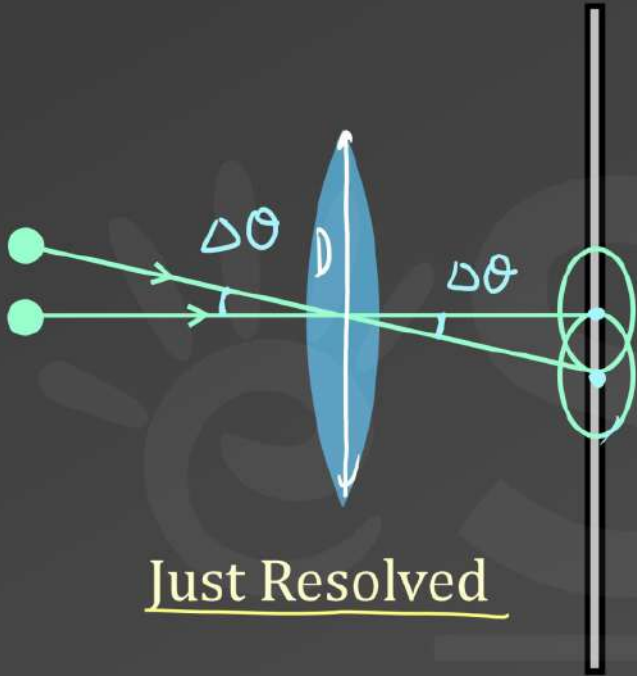


$$a\theta = \left(n + \frac{1}{2}\right)\lambda \quad \text{Maxima}$$

$$a\theta = n\lambda \quad \text{Minima}$$

# Diffraction Through Single Slit





$$\Delta\theta_{\min} = \frac{1.22\lambda}{D}$$

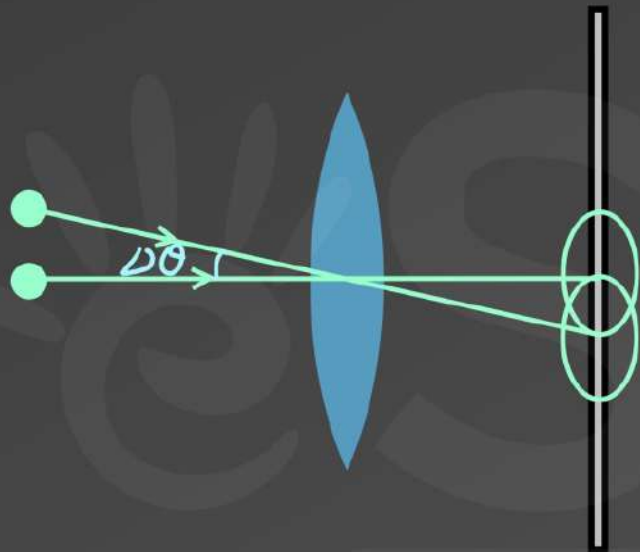
D is Diameter of Lens

Just Resolved

(Resolved : seen as separated)



# Resolving Power of Telescope



$$\text{R. P of Telescope} = \frac{1}{\Delta\theta_{\min}} = \frac{D}{1.22\lambda}$$

D = Diameter of Objective Lens.

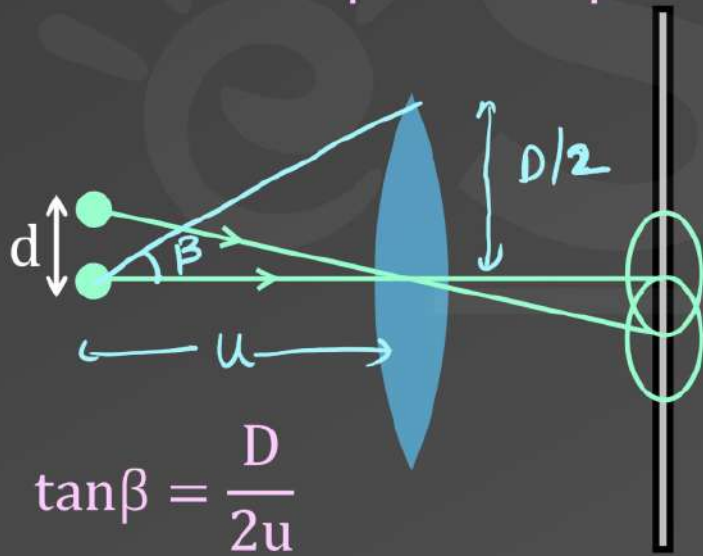


# Resolving Power of Microscope



$$R.P \text{ of Microscope} = \frac{1}{d_{\min}}$$

$$d_{\min} = \frac{1.22\lambda}{2\tan\beta} = \frac{1.22\lambda}{2\sin\beta}$$



$$\tan\beta = \frac{D}{2u}$$

Defined as reciprocal of the distance between 2 objects which can be just resolved when seen through microscope.



Simplest

Polaroid

Polarised Wave

$I_0$



$\theta$



$$I = I_0 \cos^2 \theta$$

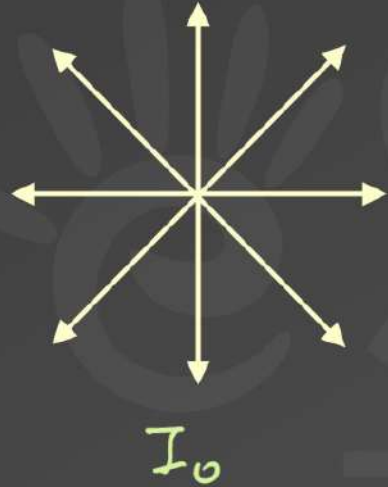


$$I = I_0 \cos^2 \theta$$

Malus' Law



Unpolarised Wave

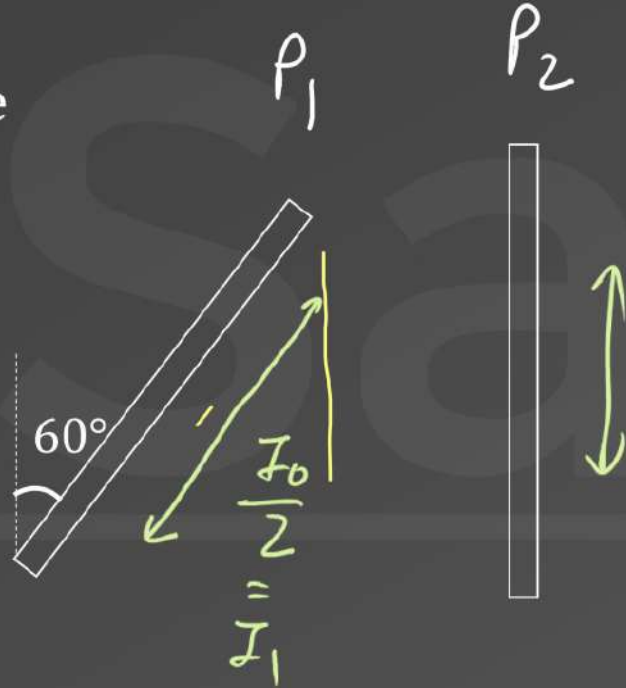
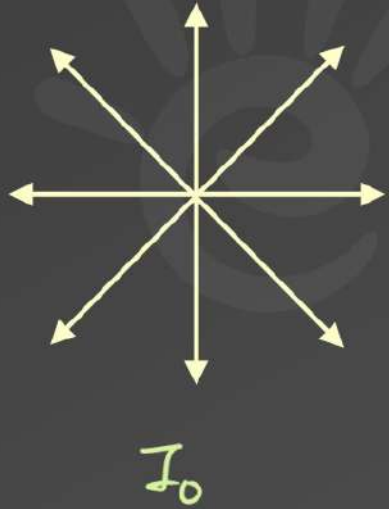


Polaroid



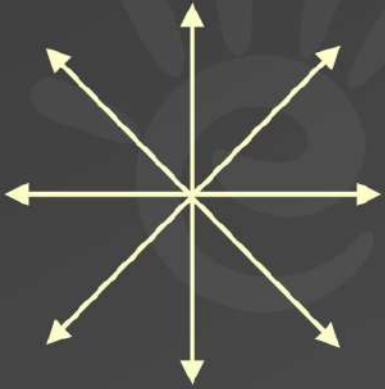
Polarized  
 $\frac{I_0}{2}$

Unpolarised Wave



$$I_2 = I_1 \cos^2 60^\circ$$
$$= \frac{I_0}{2} \times \frac{1}{4} = \boxed{\frac{I_0}{8}}$$

Unpolarised Wave



$P_1$



$\frac{I_0}{2}$

$P_2$

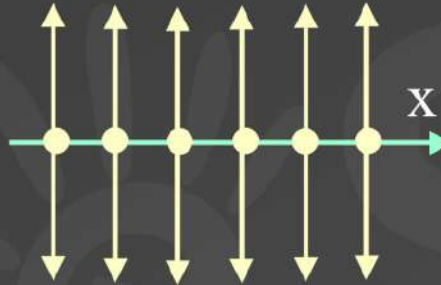


$$\frac{I_0}{2} \cos^2 90^\circ = 0$$

# Polarisation by Scattering

Unpolarised light

y



x

Polarised light



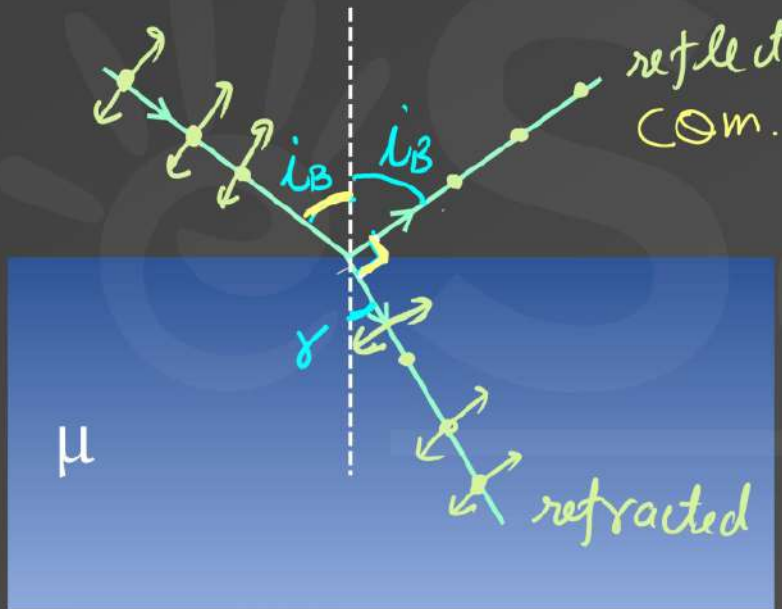
# Polarisation by Reflection



$$\tan i_B = \mu$$

Brewster's Law  
 $\Rightarrow i_B = \tan^{-1}(\mu)$

$$i_B + r = 90^\circ$$



Reflected light is completely polarised when refracted and reflected rays are perpendicular.

In this situation the angle of incidence is called Brewster's Angle.



# QUIZ TIME

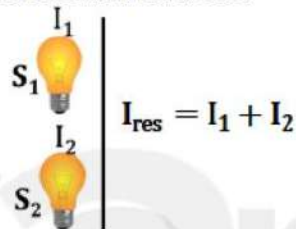


### Constructive Interference

### Destructive Interference

- Two sources are said to be Coherent if they produce waves having constant (with respect to time) phase difference.
- For Incoherent sources, phase difference varies with time.
- Two independent ordinary sources (like lamps) are incoherent sources.

### Incoherent Sources



### Interference of Waves

$$y_1 = A_1 \sin(kx - \omega t)$$

$$y_2 = A_2 \sin(kx - \omega t + \phi)$$

By Superposition Principle

$$y_{res} = y_1 + y_2$$

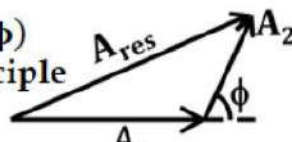
$$(A_{res})^2 = A_1^2 + A_2^2 + 2 A_1 A_2 \cos \phi$$

$$I \propto A^2$$

$$I_{res} = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \phi$$

If  $I_1 = I_2 = I_0$ , then

$$I_{res} = 4I_0 \cos^2\left(\frac{\phi}{2}\right)$$



### Constructive Interference

### Destructive Interference

$$\cos \phi = 1$$

$$\phi = 2n\pi$$

$$\cos \phi = -1$$

$$\phi = (2n + 1)\pi$$

$$A_{max} = (A_1 + A_2)$$

$$A_{min} = (A_1 - A_2)$$

$$I_{max} = 1$$

$$I_{min} = 2$$

$$I_{max} = 4I_0 \text{ (If same source of } I_0)$$

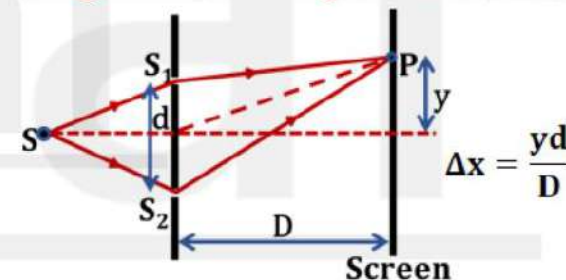
$$I_{min} = 0 \text{ (If same source of } I_0)$$

$$\Delta x = 0, \lambda, 2\lambda, 3\lambda \dots = n\lambda$$

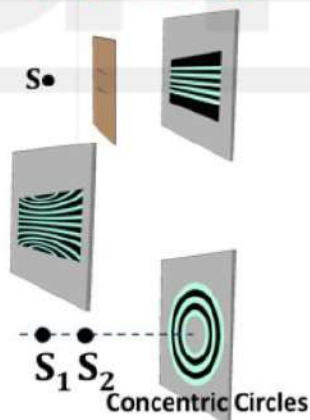
$$\Delta x = 0.5\lambda, 1.5\lambda, 2.5\lambda \dots = \left(n + \frac{1}{2}\right)\lambda$$

## WAVE OPTICS

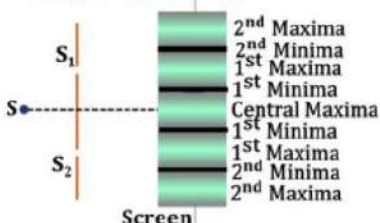
### Young's Double Slit Experiment (YDSE)



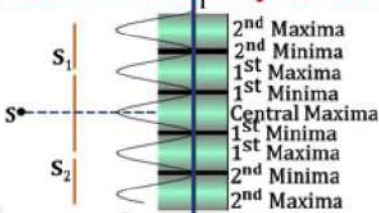
### Shape of Fringes



### Fringe Width $\beta'$



### Variation of Intensity on Screen



$$I_{res} = 4I_0 \cos^2 \frac{\phi}{2}$$

$d$  is distance between slits  $S_1$  and  $S_2$   
 $D$  is distance between slit and screen

$y$	0	$\frac{\lambda D}{2d}$	$\frac{\lambda D}{d}$	$\frac{3\lambda D}{2d}$	$\frac{2\lambda D}{d}$
Max / Min	Central Maxima	1 <sup>st</sup> Minima	1 <sup>st</sup> Maxima	2 <sup>nd</sup> Minima	2 <sup>nd</sup> Maxima

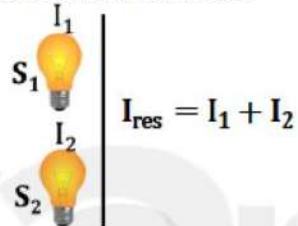




**Constructive Interference**  
**Destructive Interference**

- Two sources are said to be Coherent if they produce waves having constant (with respect to time) phase difference.
- For Incoherent sources, phase difference varies with time.
- Two independent ordinary sources (like lamps) are incoherent sources.

**Incoherent Sources**



**Interference of Waves**

$y_1 = A_1 \sin(kx - \omega t)$   
 $y_2 = A_2 \sin(kx - \omega t + \phi)$

By Superposition Principle

$y_{res} = y_1 + y_2$

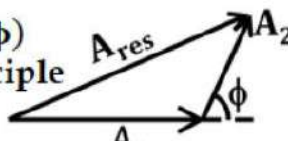
$(A_{res})^2 = A_1^2 + A_2^2 + 2 A_1 A_2 \cos \phi$

$I \propto A^2$

$I_{res} = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \phi$

If  $I_1 = I_2 = I_0$ , then

$I_{res} = 4I_0 \cos^2\left(\frac{\phi}{2}\right)$



**Constructive Interference**

**Destructive Interference**

$\cos \phi = 1$   
 $\phi = 2n\pi$

$\cos \phi = -1$   
 $\phi = (2n + 1)\pi$

$A_{max} = (A_1 + A_2)$

$A_{min} = (A_1 - A_2)$

$I_{max} = (\sqrt{I_1} + \sqrt{I_2})^2$

$I_{min} = (\sqrt{I_1} - \sqrt{I_2})^2$

$I_{max} = 4I_0$  (If same source of  $I_0$ )

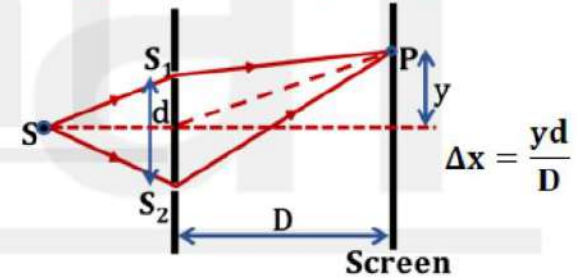
$I_{min} = 0$  (If same source of  $I_0$ )

$\Delta x = 0, \lambda, 2\lambda, 3\lambda \dots = n\lambda$

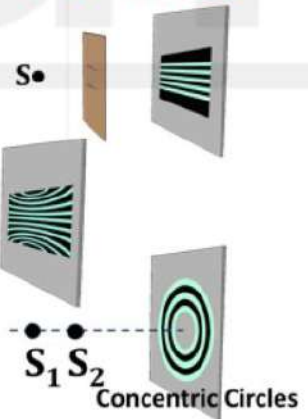
$\Delta x = 0.5\lambda, 1.5\lambda, 2.5\lambda \dots = \left(n + \frac{1}{2}\right)\lambda$

**WAVE OPTICS**

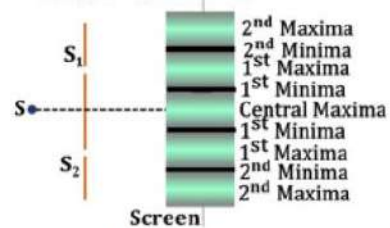
**Young's Double Slit Experiment (YDSE)**



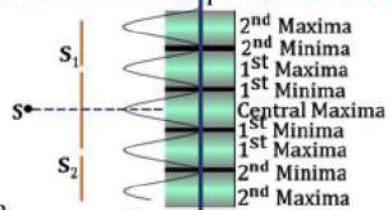
**Shape of Fringes**



**Fringe Width  $\beta'$**



**Variation of Intensity on Screen**



$I_{res} = 4I_0 \cos^2 \frac{\phi}{2}$

$d$  is distance between slits  $S_1$  and  $S_2$   
 $D$  is distance between slit and screen

$y$	0	$\frac{\lambda D}{2d}$	$\frac{\lambda D}{d}$	$\frac{3\lambda D}{2d}$	$\frac{2\lambda D}{d}$
Max / Min	Central Maxima	1 <sup>st</sup> Minima	1 <sup>st</sup> Maxima	2 <sup>nd</sup> Minima	2 <sup>nd</sup> Maxima

## Thin Film Interference

### a) Interference in Reflection

$$\Delta x_{opt} = \left(n + \frac{1}{2}\right) \lambda_{air} \rightarrow \text{Cons}$$

$$2\mu t = \left(n + \frac{1}{2}\right) \lambda_{air} \rightarrow \text{Const}$$

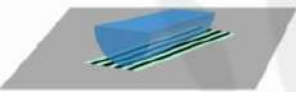
$$2\mu t = n\lambda_{air} \rightarrow \text{Dest}$$

### b) Interference in Transmission

$$(\Delta x)_{opt} = 2\mu t$$

$$2\mu t = \left(n + \frac{1}{2}\right) \lambda_{air} \rightarrow \text{Dest}$$

$$2\mu t = n\lambda_{air} \rightarrow \text{Cons}$$



$$(\Delta x)_{opt} = 2\mu t$$

$$2\mu t = \left(n + \frac{1}{2}\right) \lambda \rightarrow \text{Cons}$$

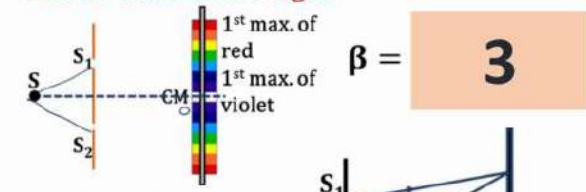
$$2\mu t = n\lambda \rightarrow \text{Des}$$

$$(\Delta x)_{opt} = 2\mu t$$

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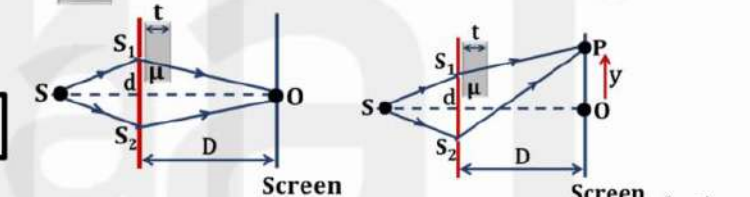
$$2\mu t = n\lambda_{air} \rightarrow \text{Dest}$$

## YDSE with white light



**Variations in YDSE**  
In this case CM shifts but fringe width remains same.

Optical path =  $4 \mu t$

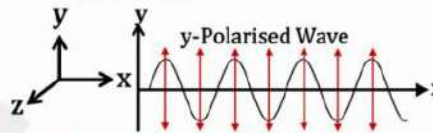


Phase difference at O  
 $\Delta x = (\mu - 1)t$

$\beta = \frac{\lambda_{air} D}{d}$  No change

$\beta = \frac{\lambda_{air} D}{d}$  No change

## Polarisation



## Unpolarised Wave

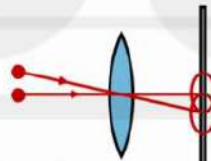
## WAVE OPTICS

## Resolution of Optical Instruments

(Resolved : seen as separated)

$$\Delta \theta_{min} = \frac{1.22 \lambda}{D}$$

Just Resolved



## Resolving Power of Telescope

$$\text{R.P of Telescope} = \frac{1}{\Delta \theta_{min}} = \frac{D}{1.22 \lambda}$$

D = Diameter of Objective Lens.

## Resolving Power of Microscope

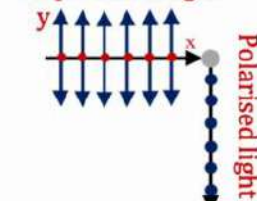
$$\text{R.P of Microscope} = \frac{1}{d_{min}}$$

$$d_{min} = \frac{1.22 \lambda}{2 \tan \beta} = \frac{1.22 \lambda}{2 \sin \beta}$$

$$d_{min} = \frac{1.22 \lambda}{2 \mu \sin \beta} \quad \tan \beta = \frac{D}{2u}$$

## Polarisation by Scattering

### Unpolarised light



## Polarisation by Reflection

$\tan(i_B) = \mu$   
Brewster's Law

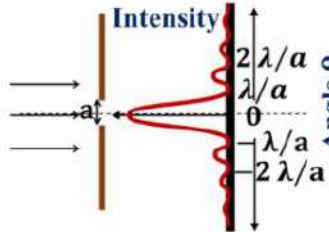
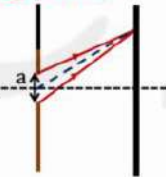
$$i_B = \tan^{-1} \mu$$

$$i_B + r = 90^\circ$$

## Diffraction Through Single Slit

$$a \theta = 5 \lambda \text{ Minima}$$

$$a \theta = \left(n + \frac{1}{2}\right) \lambda \text{ Maxima}$$



## Thin Film Interference

### a) Interference in Reflection

$$\Delta x_{opt} = \left(n + \frac{1}{2}\right) \lambda_{air} \rightarrow \text{Cons}$$

$$2\mu t = \left(n + \frac{1}{2}\right) \lambda_{air} \rightarrow \text{Const}$$

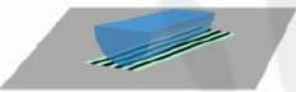
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### b) Interference in Transmission

$$(\Delta x)_{opt} = 2\mu t$$

$$2\mu t = \left(n + \frac{1}{2}\right) \lambda_{air} \rightarrow \text{Dest}$$

$$2\mu t = n\lambda_{air} \rightarrow \text{Cons}$$



$$(\Delta x)_{opt} = 2\mu t$$

$$2\mu t = \left(n + \frac{1}{2}\right) \lambda \rightarrow \text{Cons}$$

$$2\mu t = n\lambda \rightarrow \text{Des}$$

$$(\Delta x)_{opt} = 2\mu t$$

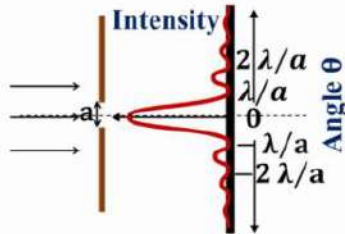
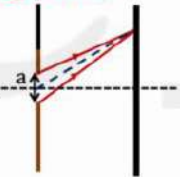
$$2\mu t = \left(n + \frac{1}{2}\right) \lambda_{air} \rightarrow \text{Cons}$$

$$2\mu t = n\lambda_{air} \rightarrow \text{Dest}$$

## Diffraction Through Single Slit

$$a\theta = n\lambda \text{ Minima}$$

$$a\theta = \left(n + \frac{1}{2}\right) \lambda \text{ Maxima}$$



## Resolution of Optical Instruments

(Resolved : seen as separated)

$$\Delta\theta_{min} = \frac{1.22\lambda}{D}$$

### Resolving Power of Telescope

$$R.P \text{ of Telescope} = \frac{1}{\Delta\theta_{min}} = \frac{D}{1.22\lambda}$$

D = Diameter of Objective Lens.

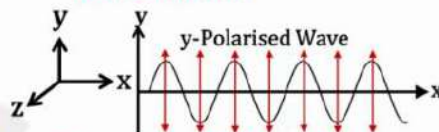
### Resolving Power of Microscope

$$R.P \text{ of Microscope} = \frac{1}{d_{min}}$$

$$d_{min} = \frac{1.22\lambda}{2\sin\beta} = \frac{1.22\lambda}{2\sin\beta}$$

$$d_{min} = \frac{1.22\lambda}{2\mu\sin\beta} \quad \tan\beta = \frac{D}{2u}$$

## Polarisation

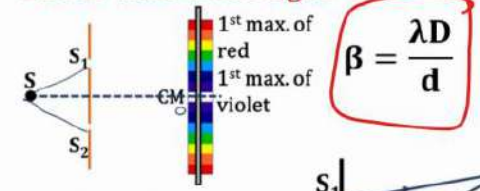


## Unpolarised Wave



## WAVE OPTICS

## YDSE with white light



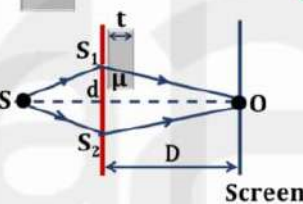
$$\beta = \frac{\lambda D}{d}$$

## Variations in YDSE

In this case CM shifts but fringe width remains same.

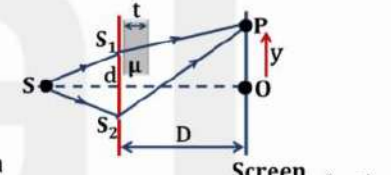


$$\text{Optical path} = \mu t$$



Phase difference at O  
 $\Delta x = (\mu - 1)t$

$$\beta = \frac{\lambda_{air} D}{d} \text{ No change}$$

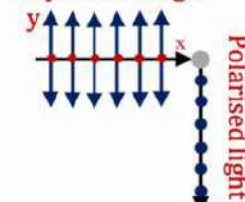


$$(\Delta x) = (\mu - 1)t - \left(\frac{y d}{D}\right)$$

$$\beta = \frac{\lambda_{air} D}{d} \text{ No change}$$

## Polarisation by Scattering

### Unpolarised light



### Polarised light

## Polarisation by Reflection

$$\tan(i_B) = \mu \text{ Brewster's Law}$$

$$i_B = \tan^{-1} \mu$$

$$i_B + r = 90^\circ$$

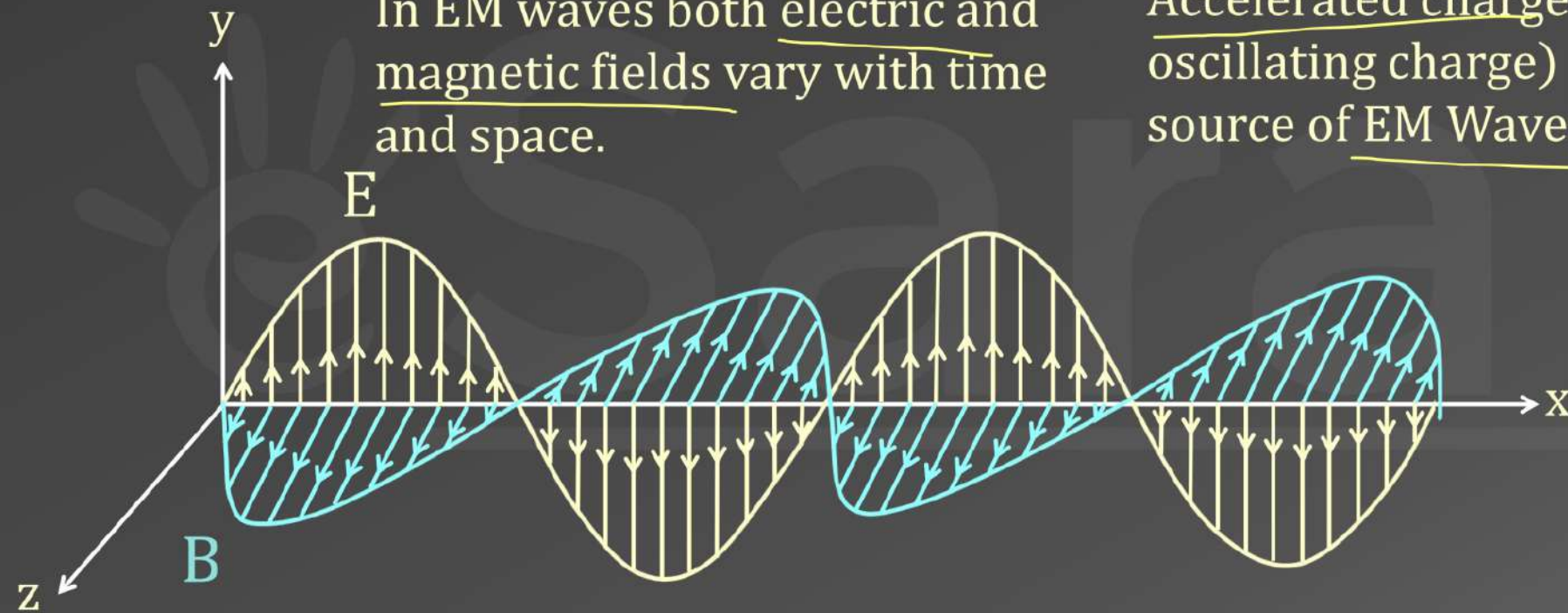
# Electromagnetic Waves

1 Formula

# Superfast Revision

In EM waves both electric and magnetic fields vary with time and space.

Accelerated charge (e.g. a oscillating charge) is a source of EM Waves.



$$E = Bc$$

TRICK

$$\hat{E} \times \hat{B} = \hat{v}$$



$\vec{E}$  and  $\vec{B}$  are perpendicular to each other and are also perpendicular to direction of propagation of wave.



Q) A plane electromagnetic wave of frequency 25 MHz travels in free space along the x-direction. At a particular point in space and time,  $\vec{E} = 6.3 \hat{j}$  V/m. What is  $\vec{B}$  at this point?

Sol.  $E = Bc$

$$B = \frac{E}{c} = \frac{6.3}{3 \times 10^8} = 2.1 \times 10^{-8} \text{ T}$$

$$\hat{E} \wedge \hat{B} = \hat{v}$$

$$\hat{j} \times \hat{k} = \hat{i}$$

$$\vec{B} = 2.1 \times 10^{-8} \hat{k} \text{ T}$$

Energy Density in form of  $\vec{E}$  =  $\frac{1}{2} \epsilon_0 E_{rms}^2$

↑ Energy/vol<sup>m</sup>

"  $\vec{B}$  =  $\frac{1}{2} \frac{B_{rms}^2}{\mu_0}$



Electromagnetic waves can be polarized.

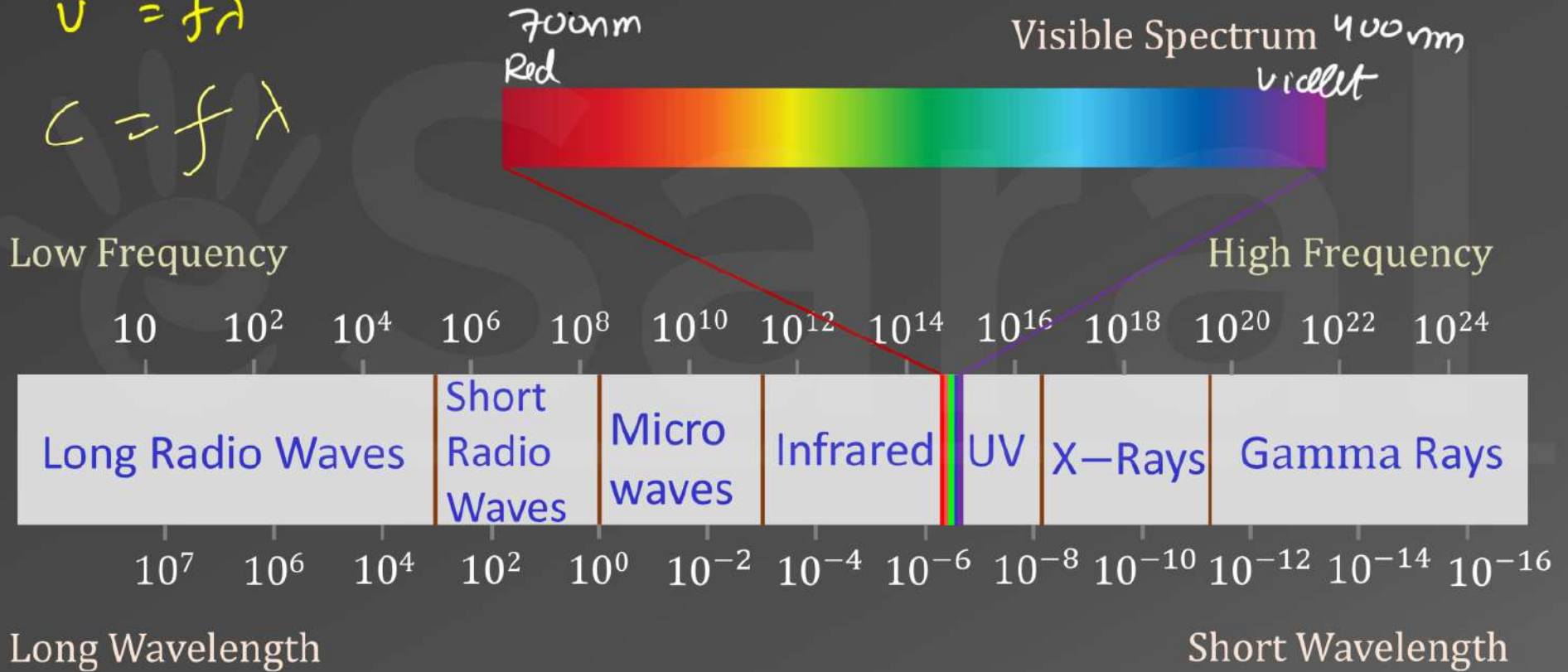
Energy is equally divided in electric and magnetic field.



Total Energy density =  $\epsilon_0 E_{rms}^2 = \frac{B_{rms}^2}{\mu_0}$

Intensity of EM waves =  $\epsilon_0 E_{rms}^2$

$$v = f\lambda$$

$$c = f\lambda$$



Type	Wavelength range	Uses
<u>Radio Waves</u>	$> 0.1 \text{ m}$	<u>Radio and television communication</u>
<u>Microwave</u>	$10^{-1} \text{ m to } 10^{-3} \text{ m}$ $0.1 \text{ m to } 1 \text{ mm}$	<u>Microwave Oven,</u> <u>Radar System</u>
<u>Infrared</u>  (Produced by hot bodies) 	$1 \text{ mm to } 700 \text{ nm}$	<u>Remote Switches</u> and <u>Household</u> <u>electronic devices</u>

Type	Wavelength range	Uses
Visible Rays	700 nm to 400nm	To see objects
<u>Ultraviolet</u>	400 nm to 1nm	<u>Eye surgery,</u> <u>Water purifier</u>
<u>X-rays</u>	$10^{-9}m$ 1nm to $10^{-3} \text{ } 10^{-12}m$ nm	<u>Medical diagnosis</u>
<u>Gamma rays</u> (Produced in Nuclear Reactions)	$< 10^{-3} \text{ nm}$	Medical treatment (to destroy cancer cells)

$$c = \frac{1}{\sqrt{\mu_0 \epsilon_0}}$$

Vacuum



$$v = \frac{1}{\sqrt{\mu \epsilon}} = \frac{1}{\sqrt{\mu_r \mu_0 \epsilon_r \epsilon_0}} = \frac{c}{\sqrt{\mu_r \epsilon_r}}$$

medium

$\mu_0$  - Permeability of free space (vacuum)

$\epsilon_0$  - Permittivity of free space (vacuum)

$\mu$  - Permeability of medium

$\epsilon$  - Permittivity of medium

Q) The dimensions of  $(\mu_0 \epsilon_0)^{-1/2}$  are

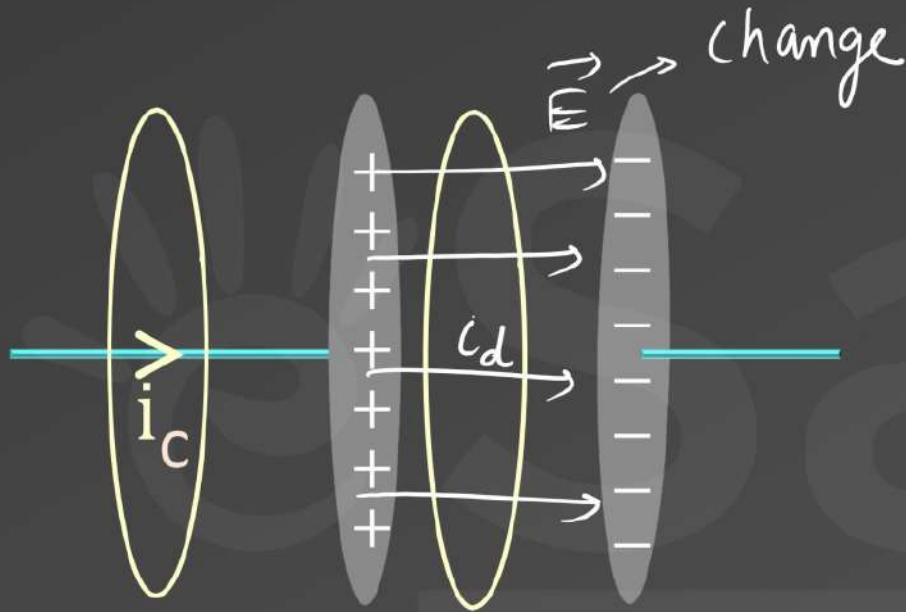
- (1)  $[L^{1/2} T^{-1/2}]$       (2)  $[L^{-1} T]$       (3)  $[L T^{-1}]$       (4)  $[L^{-1/2} T^{-1/2}]$

Sol.

speed  
↓  
 $c = \frac{1}{\sqrt{\mu_0 \epsilon_0}} = (\mu_0 \epsilon_0)^{-1/2}$

$$L T^{-1} = [(\mu_0 \epsilon_0)^{-1/2}]$$

# Displacement Current



$$i_d = \epsilon_0 \frac{d\phi_E}{dt}$$

} Electric Flux

Ampere-Maxwell Law

$$\oint \vec{B} \cdot d\vec{\ell} = \mu_0 (i_c + i_d)$$

$$\oint \vec{B} \cdot d\vec{\ell} = \mu_0 i_c + \mu_0 \epsilon_0 \frac{d\phi_E}{dt}$$





# QUIZ TIME

## Maxwell's Equation

1)  $\oint \vec{E} \cdot d\vec{A} = \frac{Q}{\epsilon_0}$  Gauss's Law for electricity

2)  $\oint \vec{B} \cdot d\vec{A} = 0$  Gauss's Law for magnetism

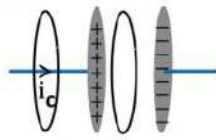
3)  $\oint \vec{E} \cdot d\vec{\ell} = -\frac{d\phi_B}{dt}$  Faraday's Law

4)  $\oint \vec{B} \cdot d\vec{\ell} = \mu_0 i_c + \mu_0 \epsilon_0 \frac{d\phi_E}{dt}$  Ampere-Maxwell Law

$c = \frac{1}{\sqrt{\mu_0 \epsilon_0}}$   $\mu_0$  - Permeability of free space (vacuum)  
 $v = \frac{1}{\sqrt{\mu \epsilon}}$   $\epsilon_0$  - Permittivity of free space (vacuum)  
 $\mu$  - Permeability of medium  
 $\epsilon$  - Permittivity of medium



## Displacement Current

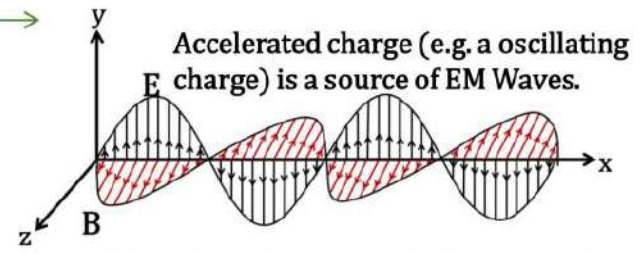


Ampere-Maxwell Law

$$\oint \vec{B} \cdot d\vec{\ell} = \mu_0 (i_c + i_d)$$

$$\oint \vec{B} \cdot d\vec{\ell} = \mu_0 i_c + \mu_0 \epsilon_0 \frac{d\phi_E}{dt}$$

## ELECTROMAGNETIC WAVES



In EM waves both electric and magnetic fields vary with time and space.

1

$\vec{E}$  and  $\vec{B}$  are perpendicular to each other and are also perpendicular to direction of propagation of wave.

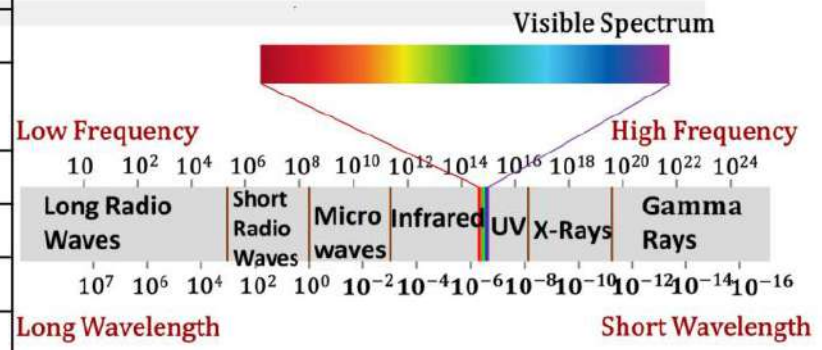
Electromagnetic waves can be polarized.

Energy is equally divided in electric and magnetic field.

Energy Density =  $\frac{1}{2} E_0 E_{rms}^2 = \frac{B_{rms}^2}{2\mu_0}$

Total Energy Density =  $E_0 E_{rms}^2 = \frac{B_{rms}^2}{\mu_0}$

Type	Wavelength Range	Uses
Radio Waves	> 0.1 m	Radio and television communication
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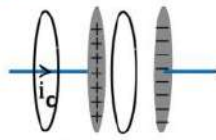
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4)  $\oint \vec{B} \cdot d\vec{\ell} = \mu_0 i_c + \mu_0 \epsilon_0 \frac{d\phi_E}{dt}$  Ampere-Maxwell Law

$c = \frac{1}{\sqrt{\mu_0 \epsilon_0}}$   $\mu_0$  - Permeability of free space (vacuum)  
 $\epsilon_0$  - Permittivity of free space (vacuum)  
 $v = \frac{1}{\sqrt{\mu \epsilon}}$   $\mu$  - Permeability of medium  
 $\epsilon$  - Permittivity of medium



## Displacement Current

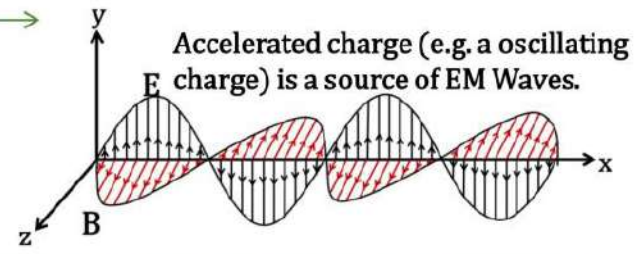


Ampere-Maxwell Law

$$\oint \vec{B} \cdot d\vec{\ell} = \mu_0 (i_c + i_d)$$

$$\oint \vec{B} \cdot d\vec{\ell} = \mu_0 i_c + \mu_0 \epsilon_0 \frac{d\phi_E}{dt}$$

## ELECTROMAGNETIC WAVES



In EM waves both electric and magnetic fields vary with time and space.

$$E = Bc \quad \hat{E} \times \hat{B} = \hat{v}$$

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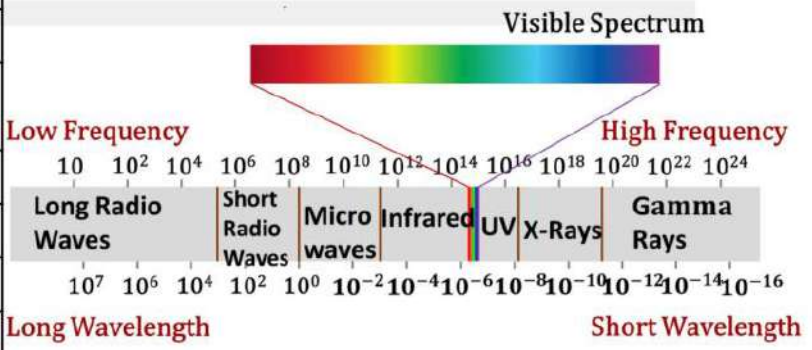
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Rounding Off

**Error**

**Superfast Revision**

3 Min Break

## Errors

Systematic Errors

Random Errors

$$A \pm \Delta A$$

$$50 \text{ kg} \pm 5 \text{ kg}$$

$$45 \text{ kg to } 55 \text{ kg}$$

eSaral



.1 cm

**Least Count** :- The smallest value that can be measured by the measuring instrument is called its Least Count.

Least Count Error :- If the instrument has known least count, the absolute error is taken to be equal to the least count unless otherwise stated.





$$\text{Relative Error} = \frac{\text{Absolute error in a measurement}}{\text{Size of the measurement}}$$

$$50\text{kg} \pm 5\text{kg}$$

$$\text{Relative Error} = \frac{5\text{kg}}{50\text{kg}} = \frac{1}{10}$$

$$A \pm \Delta A$$

$$\text{Relative Error} = \frac{\Delta A}{A}$$





$$50 \text{ kg} \pm 5 \text{ kg}$$

$$50 \text{ kg} \pm 10\%$$

$$\text{PE} = \frac{5}{50} \times 100 = 10\%$$

$$\frac{\Delta A}{A} \times 100 =$$

$$\text{Percentage Error} = \frac{\text{Absolute error in a measurement}}{\text{Size of the measurement}} \times 100$$

# Addition and Subtraction Rule

$$A \pm \Delta A$$

$$B \pm \Delta B$$

+

-

$$R \pm \Delta R$$

$$R \pm \Delta R$$

$$R = \underline{A + B}$$

$$R = \underline{A - B}$$

$$\Delta R = \underline{\Delta A + \Delta B}$$

$$\Delta R = \underline{\Delta A + \Delta B}$$

Absolute error adds

A B

A

B

$$20 \pm 2$$

$$10 \pm 5$$

$$A + B =$$

$$(+): - 30 \pm 7$$

$$A - B$$

$$(-): - \underline{10} \pm \underline{7}$$

# Product and Quotient Rule



$$R = A \times B$$

$$\frac{\Delta R}{R} = \frac{\Delta A}{A} + \frac{\Delta B}{B}$$

$$A \times B^{-1}$$

Divide  $R = A / B$

$$\frac{\Delta R}{R} = \frac{\Delta A}{A} + \frac{\Delta B}{B}$$

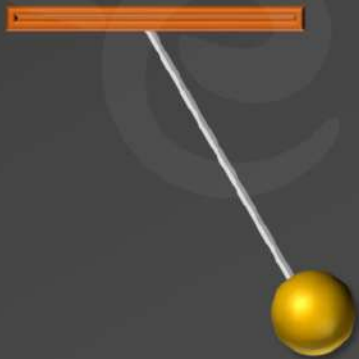




$$R = \frac{A^p B^q}{C^s D^t}$$

$$\frac{\Delta R}{R} = p \frac{\Delta A}{A} + q \frac{\Delta B}{B} + s \frac{\Delta C}{C} + t \frac{\Delta D}{D}$$





Time of 1 osc.

$$T = 2\pi \sqrt{\frac{L}{g}}$$

$$g = 4\pi^2 \frac{L}{T^2}$$

$$\frac{\Delta g}{g} = \frac{\Delta L}{L} + \frac{2\Delta T}{T}$$



For numbers with indicated decimal

1. All nonzero digits (1-9) are to be counted as significant.

2. Zeros that have any nonzero digits anywhere to the left of them are considered significant zeros.

3. All other zeros not covered in rule (2) above are NOT considered significant zeros.

125.0 mm

Sig. Digits

4

12.50 cm

4

0.006000

4

250.0050

7

0.0003

1



For numbers with no indicated decimal

1. All nonzero digits (1-9) are to be counted as significant.

2. The terminal or trailing zero(s) are not significant.

$\overline{13700}$ cm	Sig Dig 3
$\overline{1205000}$	4
$\overline{7812}$ cm	4

$$a \times 10^b$$

'a' is a number between 1 and 10

$$\begin{array}{c} 4 \\ \hline 12.50 \text{ cm} \end{array}$$

$$\begin{array}{c} 4 \\ \hline 1.250 \times 10^1 \text{ cm} \end{array}$$

$$= \begin{array}{c} 4 \\ \hline 1.250 \times 10^2 \text{ mm} \end{array}$$

$$= 1.250 \times 10^5 \mu\text{m}$$

$$= 1.250 \times 10^{-1} \text{ m}$$

Order of Magnitude

$$= 1.2 \times 10^7 \text{ m}$$





## Multiplication or Division

The final result should retain as many significant digits as are there in the original numbers with the least significant digits.

$$\begin{array}{l}
 \begin{array}{r}
 \textcircled{1} \\
 \hline
 8.000 \\
 \textcircled{2} \\
 \hline
 4.0 \\
 \hline
 3.00 \times 800.0 \\
 \hline
 \end{array}
 = 
 \begin{array}{r}
 \textcircled{2} \\
 2.0 \\
 \hline
 \end{array}
 \\
 \\
 \begin{array}{r}
 \begin{array}{r}
 \textcircled{3} \\
 3.00 \\
 \hline
 \end{array}
 \times 
 \begin{array}{r}
 \textcircled{4} \\
 800.0 \\
 \hline
 \end{array}
 = 
 \begin{array}{r}
 \textcircled{3} \\
 2400 \\
 \hline
 \end{array}
 = 
 \begin{array}{r}
 \textcircled{3} \\
 2.40 \times 10^3 \\
 \hline
 \end{array}
 \\
 \\
 \begin{array}{r}
 \textcircled{3} \\
 1.23 \\
 \hline
 \end{array}
 \times 
 \begin{array}{r}
 \textcircled{4} \\
 2.234 \\
 \hline
 \end{array}
 \times 
 \begin{array}{r}
 \textcircled{5} \\
 2.6421 \\
 \hline
 \end{array}
 = 
 \begin{array}{r}
 \textcircled{3} \\
 7.260015 \\
 \hline
 \end{array}
 \\
 = 7.26
 \end{array}$$

## Addition or Subtraction

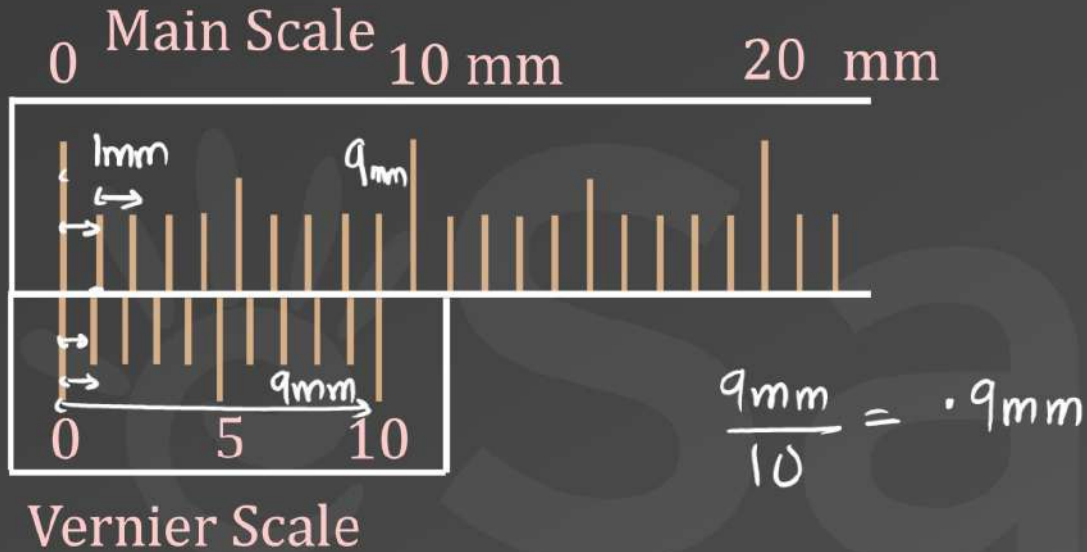
The final result should retain as many decimal places as are there in the original numbers with the least decimal places.

$$115.3 \text{ (3)} \quad \text{---}$$

$$\overset{\textcircled{2}}{100.23} + \overset{\textcircled{1}}{15.1} = 115.3$$

$$\overset{\textcircled{3}}{100.270} + \overset{\textcircled{1}}{1.1} - \overset{\textcircled{2}}{10.21} = \overset{\textcircled{3}}{91.160} = \boxed{91.2}$$

# Vernier Caliper



1 Main Scale Division (MSD) = 1mm

1 Vernier Scale Division (VSD) = 0.9 mm

Least Count of Vernier Calipers = 1 MSD - 1 VSD = 0.1 mm

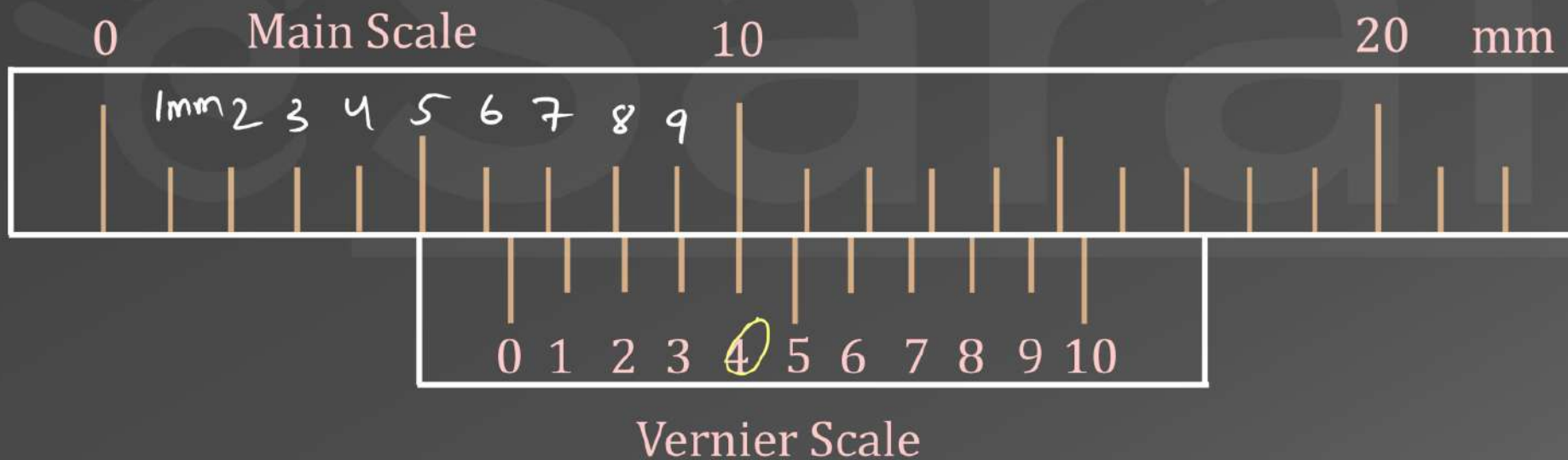


# Vernier Caliper



$$6\text{mm} + (0.1\text{mm}) \times 4 = 6.4\text{mm}$$

Length = MS Reading + Least Count of  
Vernier X VS division Coinciding with MS



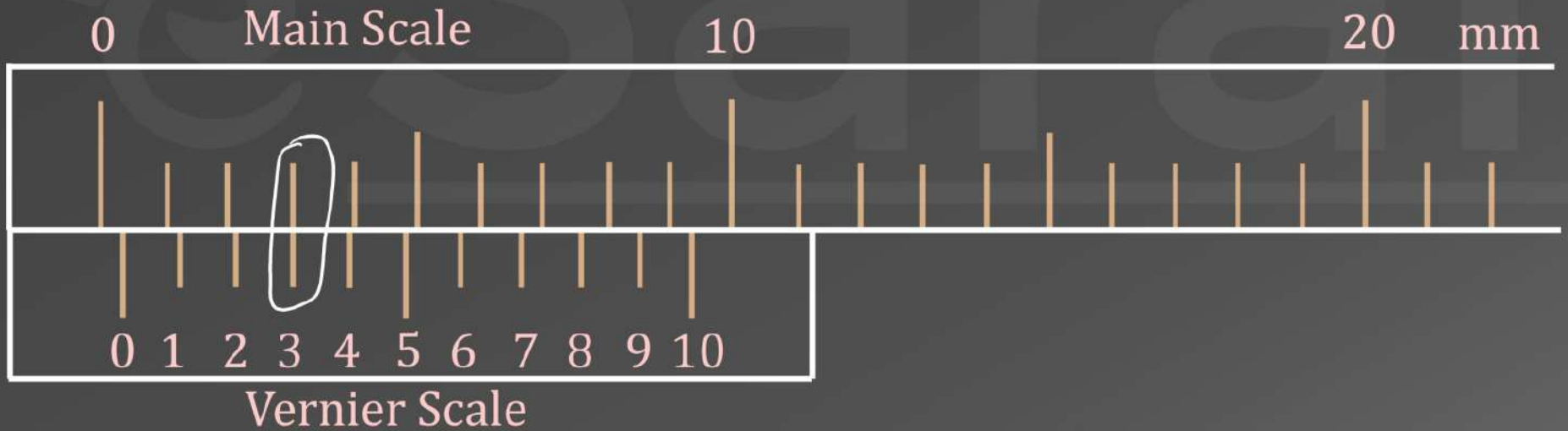
**Positive Zero Error:** If nothing is placed and zero of VS is to the **RIGHT** of zero of MS, then the zero error is positive.

Zero Error is subtracted from the reading to get the corrected value.

$$\text{measured} = 52.9 \text{ mm}$$

$$\begin{aligned} \text{corrected} &= 52.9 - 0.3 \text{ mm} \\ &= 52.6 \end{aligned}$$

$$0 + 0.1 \times 3 = \boxed{0.3 \text{ mm}}$$

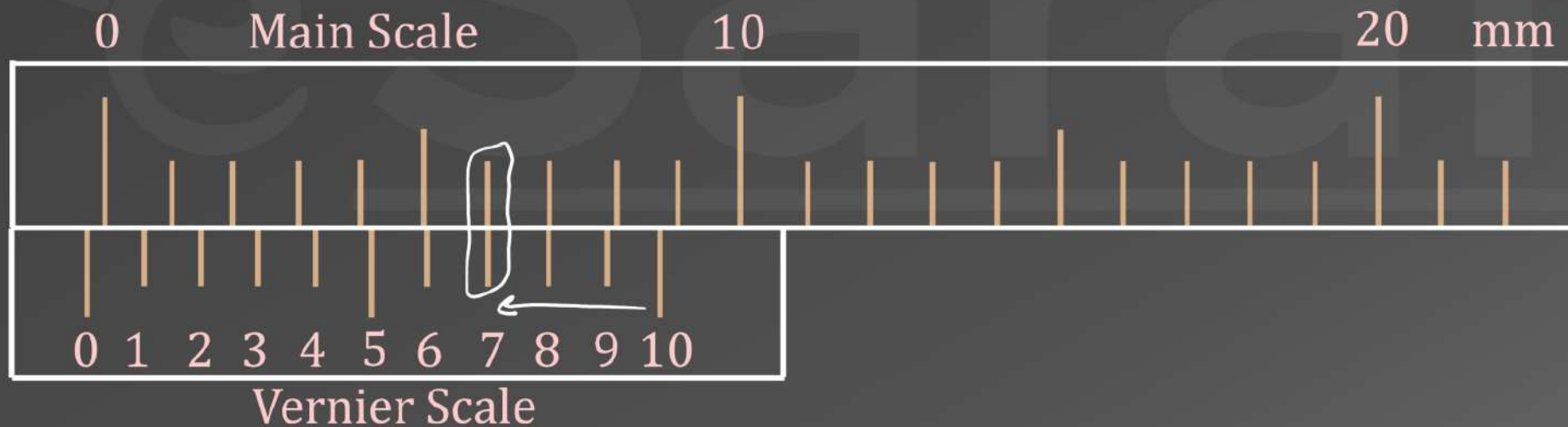


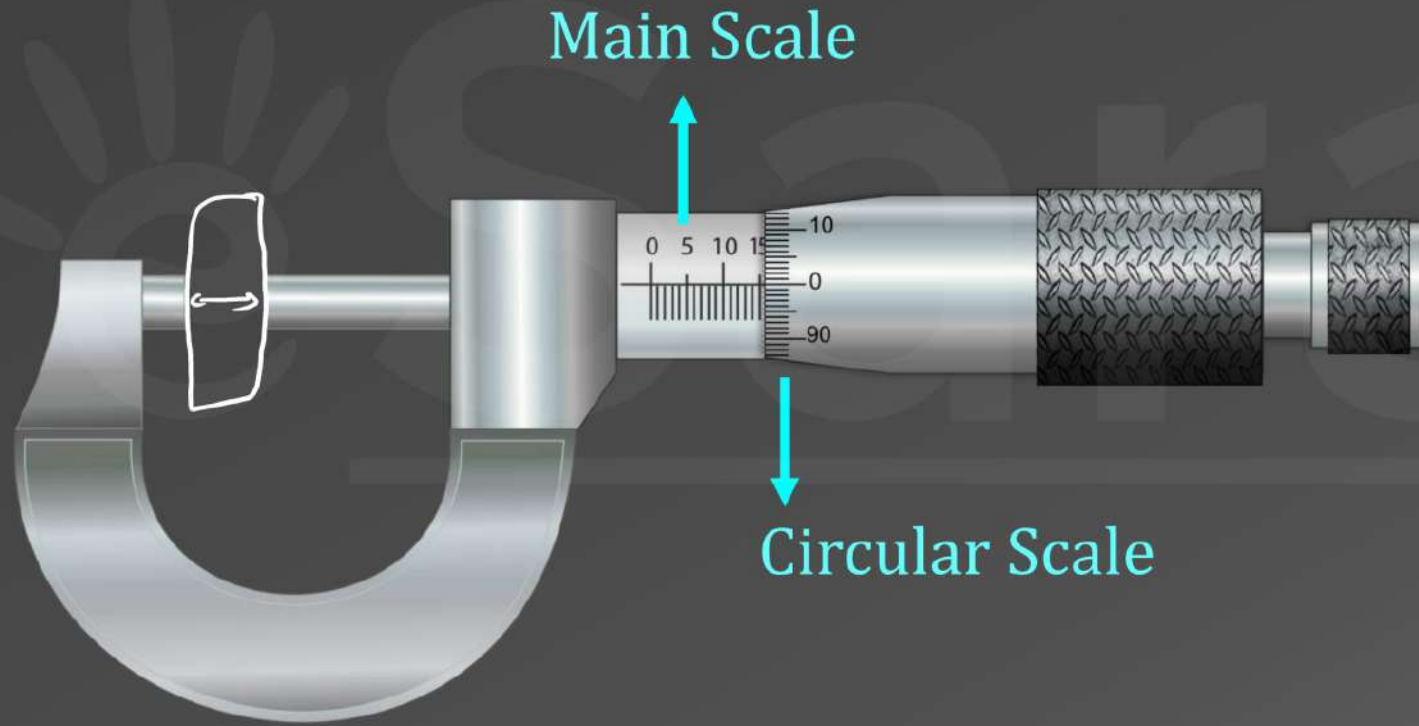
**Negative Zero Error:** If nothing is placed and zero of VS is to the LEFT of zero of MS, then the zero error is negative.

Zero Error is subtracted from the reading to get the corrected value.

$$Zero = (10 - 7) \times .1 = -0.3 \text{ mm}$$

$$52.9 - (-0.3 \text{ mm}) = \underline{\underline{53.2}}$$



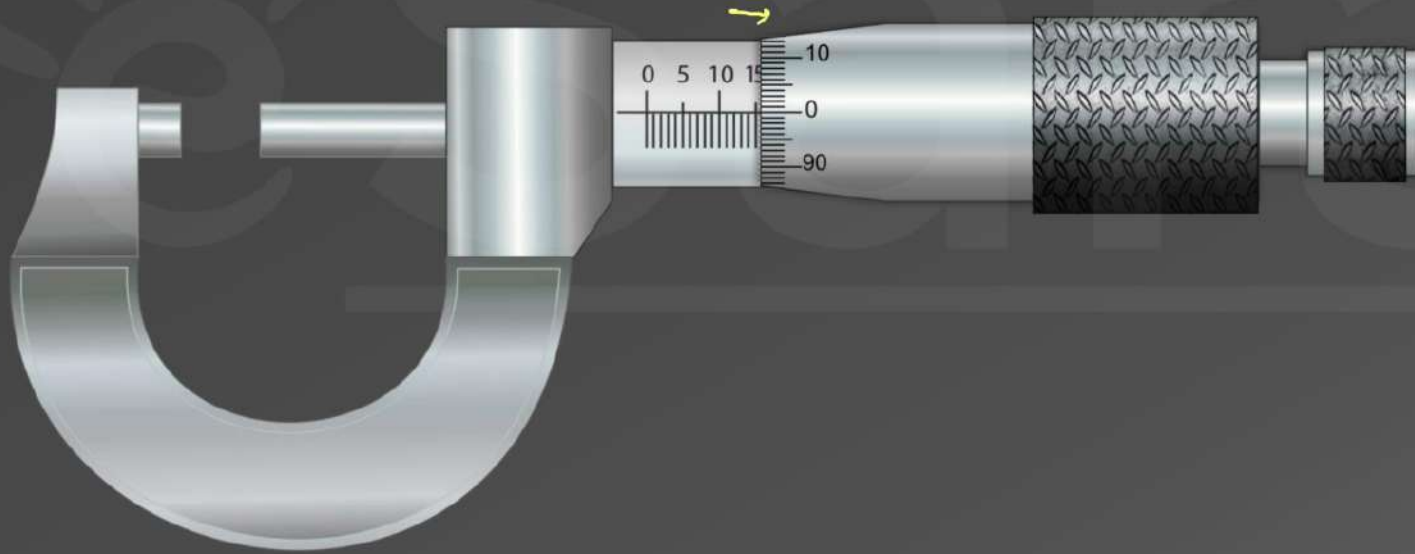




## Pitch



The pitch of screw gauge is the distance between two consecutive threads of the screw, which is equal to the distance moved by the screw due to one complete rotation of the cap.

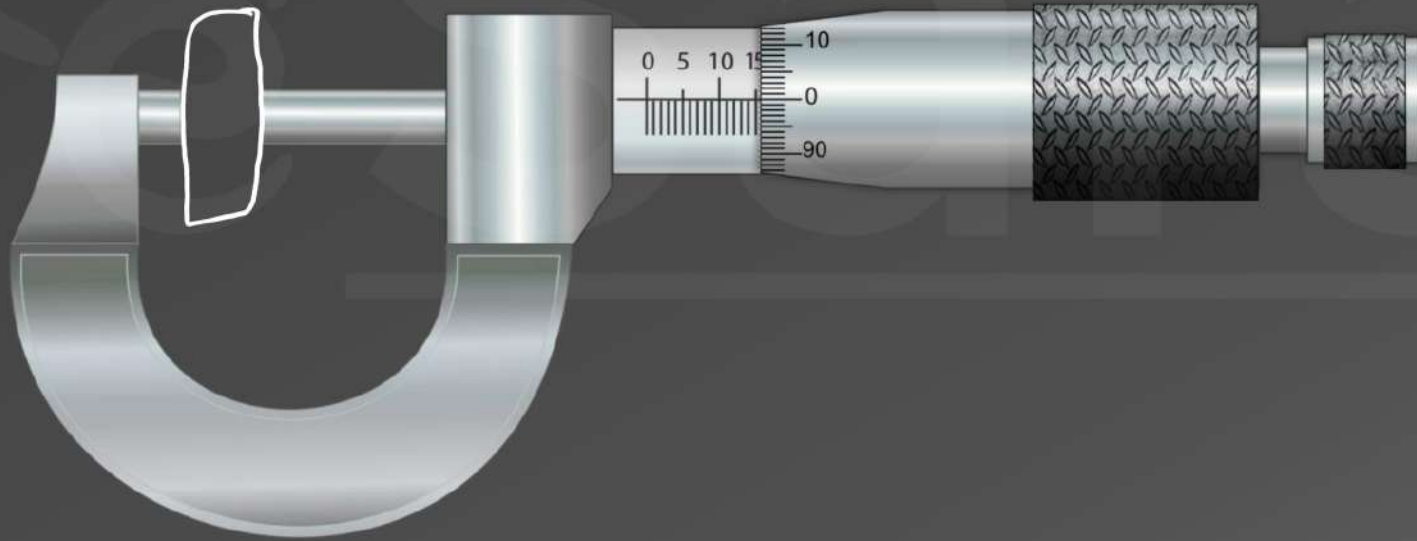


# Least Count



It is equal to pitch divided by the total divisions on the circular scale.

$$\text{Least Count} = \frac{\text{Pitch}}{\text{No. of div on Cir scale}} = \frac{1\text{mm}}{100} = 0.01\text{mm}$$



# Screw Gauge



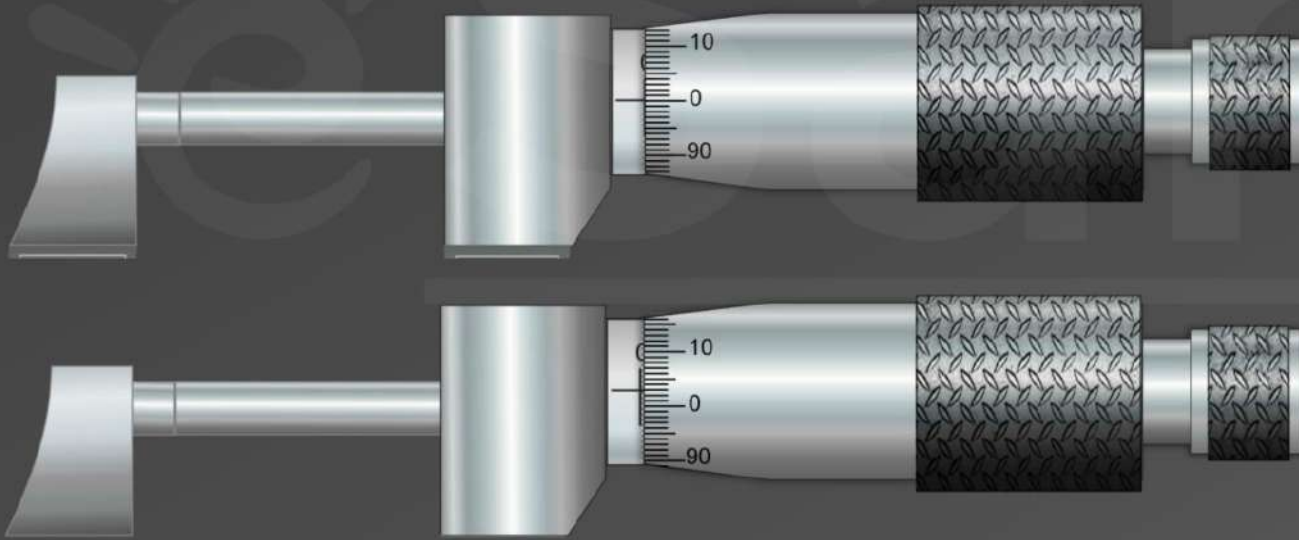
$$\begin{aligned}
 \text{Reading} &= \text{Main Scale Reading} + \text{C/S Scale Cont} \\
 &= \underline{24 \times 1\text{mm}} + \underline{65 \times 0.01\text{mm}} \\
 &= 24\text{mm} + 0.65 = \boxed{24.65\text{mm}}
 \end{aligned}$$



$$\begin{aligned}
 \text{Reading} &= \text{MS Reading} + \text{CS Cont} \\
 &= \underbrace{(\text{MS div} \times 1\text{msd})}_{\boxed{65}} + \underbrace{(\text{CS division coinciding} \times \text{LC})}
 \end{aligned}$$

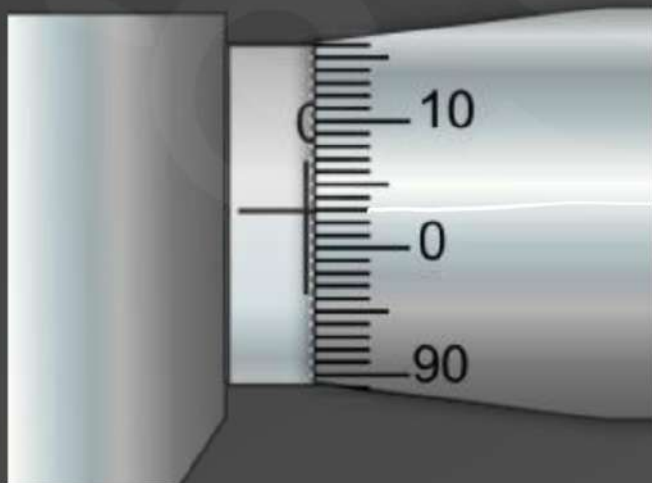
**Positive Zero Error:** If nothing is placed and zero of circular scale is **BELOW** the line of MS , then the zero error is positive.

Corrected Value = Reading – Zero Error



**Positive Zero Error:** If nothing is placed and zero of circular scale is **BELOW** the line of MS, then the zero error is positive.

Corrected Value = Reading – Zero Error



$$\begin{aligned} \text{Zero Error} &= 0 + 3 \times 0.01 \text{ mm} \\ &= 0.03 \text{ mm} \end{aligned}$$

$$62.53 \text{ mm} = \text{Reading}$$

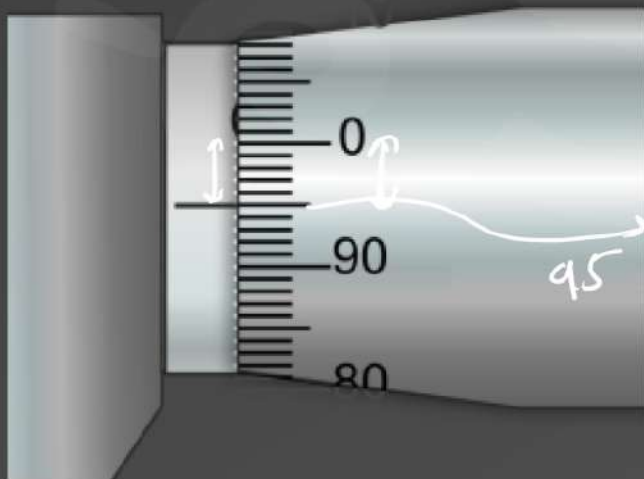
$$\text{Corrected Value} = 62.53 - 0.03 = 62.50 \text{ mm}$$

# Zero Error



**Negative Zero Error:** If nothing is placed and zero of circular scale is **ABOVE** the line of MS, then the zero error is negative.

Corrected Value = Reading - Zero Error



$$- \left[ (100 - 95) \times 0.01 \right]$$

$$- \left[ (\text{Total on CS scale} - (\text{including})) \times \text{LC} \right]$$

$$\text{Zero Error} = -(5 \times 0.01) = -0.05 \text{ mm}$$

$$62.85 \text{ mm Reading}$$

$$\text{Corrected Value} = 62.85 - (-0.05 \text{ mm})$$

$$\therefore = 62.90 \text{ mm}$$



# QUIZ TIME

### Addition and Subtraction Rule

$$\begin{array}{l} A \pm \Delta A \\ + \\ B \pm \Delta B \\ \hline R = A + B \end{array} \quad \begin{array}{l} B \pm \Delta B \\ - \\ A \pm \Delta A \\ \hline R = A - B \end{array}$$

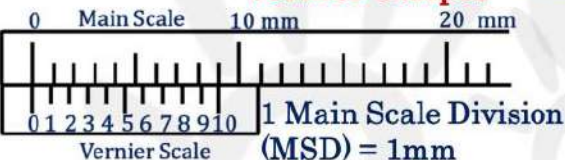
$$\Delta R = \Delta A + \Delta B$$

1

### Product and Quotient rule

$$\begin{array}{l} R = A \times B \\ \frac{dR}{R} = \frac{dA}{A} + \frac{dB}{B} \\ \frac{\Delta R}{R} = \frac{\Delta A}{A} + \frac{\Delta B}{B} \end{array} \quad \begin{array}{l} R = A/B \\ \frac{\Delta R}{R} = \frac{\Delta A}{A} + \frac{\Delta B}{B} \end{array}$$

### Vernier Caliper



1 Vernier Scale Division (VSD) = 0.9 mm

Length = MS Reading + Least Count of Vernier  $\times$  VS division Coinciding with MS

Least Count of Vernier Calipers = 1 MSD - 1 VSD = 0.1 mm

Zero Error is subtracted from the reading to get the corrected value.

### Screw Gauge

**PITCH:** Distance between two consecutive threads of the screw.

$$\text{Least Count} = \frac{\text{Pitch}}{\text{No. of division on circular Scale}}$$

Reading = Main Scale Reading + Circular Scale Count

Corrected Value = Reading - Zero Error

### Power Rule

$$R = \frac{A^p B^q}{C^s D^t}$$

$$\frac{\Delta R}{R} = p \frac{\Delta A}{A} + q \frac{\Delta B}{B} + s \frac{\Delta C}{C} + t \frac{\Delta D}{D}$$

Errors  
Systematic Errors      Random Errors

### ERROR IN MEASUREMENT

**Error** Measurement contains some Uncertainty which is called Error

**Accuracy** is a measure of how close the measured value to the true value of the quantity.

**Precision** is to what resolution or limit the quantity is measured.

**Absolute Error** - The magnitude of the difference between the individual measurement and the true value of the quantity.

**Least Count** :- The smallest value that can be measured by the measuring instrument

**Relative Error** =  $\frac{\text{Absolute error in a measurement}}{\text{Size of the measurement}}$   
(or Fractional) Error

**Scientific Notation**  $a \times 10^b$  'a' is a number between 1 and 10

**Percentage Error** =  $\frac{\text{Absolute error in a measurement}}{\text{Size of the measurement}} \times 100$

### Rules for Determining the Number of Significant Digits

For numbers with no indicated decimal

1. All nonzero digits (1-9) are to be counted as significant.
2. The terminal or trailing zero(s) are **2**

For numbers with indicated decimal

1. All nonzero digits (1-9) are to be counted as significant.
2. Zeros that have any nonzero digits anywhere to the left of them are considered significant zeros.
3. All other zeros not covered in rule (2) above are NOT considered significant zeros.





### Addition and Subtraction Rule

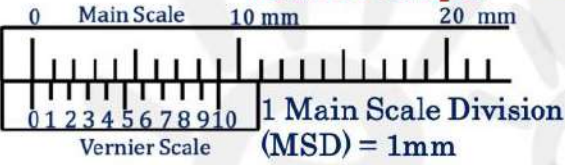
$$\begin{array}{l} A \pm \Delta A \\ + \\ B \pm \Delta B \\ \hline R = A + B \end{array} \quad \left| \quad \begin{array}{l} B \pm \Delta B \\ - \\ A \pm \Delta A \\ \hline R = A - B \end{array}$$

$$\Delta R = \Delta A + \Delta B \quad \Delta R = \Delta A + \Delta B$$

### Product and Quotient Rule

$$\begin{array}{l} R = A \times B \\ \frac{dR}{R} = \frac{dA}{A} + \frac{dB}{B} \\ \frac{\Delta R}{R} = \frac{\Delta A}{A} + \frac{\Delta B}{B} \end{array} \quad \left| \quad \begin{array}{l} R = A/B \\ \frac{\Delta R}{R} = \frac{\Delta A}{A} + \frac{\Delta B}{B} \end{array}$$

### Vernier Caliper



Length = MS Reading + Least Count of Vernier  $\times$  VS division Coinciding with MS

Least Count of Vernier Calipers = 1 MSD - 1 VSD = 0.1 mm

Zero Error is subtracted from the reading to get the corrected value.

### Screw Gauge

**PITCH:** Distance between two consecutive threads of the screw.

$$\text{Least Count} = \frac{\text{Pitch}}{\text{No. of division on circular Scale}}$$

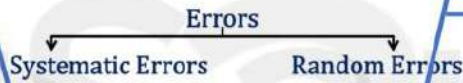
Reading = Main Scale Reading + Circular Scale Count

Corrected Value = Reading - Zero Error

### Power Rule

$$R = \frac{A^p B^q}{C^s D^t}$$

$$\frac{\Delta R}{R} = p \frac{\Delta A}{A} + q \frac{\Delta B}{B} + s \frac{\Delta C}{C} + t \frac{\Delta D}{D}$$



### ERROR IN MEASUREMENT

**Error** Measurement contains some Uncertainty which is called Error

**Accuracy** is a measure of how close the measured value to the true value of the quantity.

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$$\text{Percentage Error} = \frac{\text{Absolute error in a measurement}}{\text{Size of the measurement}} \times 100$$

### Rules for Determining the Number of Significant Digits

For numbers with no indicated decimal

1. All nonzero digits (1-9) are to be counted as significant.
2. The terminal or trailing zero(s) are not significant.

For numbers with indicated decimal

1. All nonzero digits (1-9) are to be counted as significant.
2. Zeros that have any nonzero digits anywhere to the left of them are considered significant zeros.
3. All other zeros not covered in rule (2) above are NOT considered significant zeros.

# Course Details

Lectures



Practice



Tests

Sheets

Prev. Yr.

Study Plan

Topic-Wise

Doubt Solving

Review

Mentorship



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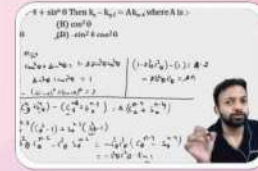
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# Complete Physics Mega Revision Timetable

15 Feb

Electrostatics

Current electricity

Capacitor

 **Surprise Gift** 

16 Feb

Calorimetry

Elasticity

Thermal Expansion

Heat Transfer

KTG

Thermodynamics

Fluid Mechanics

17 Feb

Magnetic effect of current

Magnetism and matter

Emi

AC

18 Feb

UD

Vector

Kinematics 1D

Kinematics 2D

NLM

Friction

Circular motion

Work power energy

COM

19 Feb

Ray optics

Optical Instruments

Wave optics

EM Waves

Errors in measurement

20 Feb

Rotation motion

Gravitation

SHM

Wave on string

Sound wave

21 Feb

Atomic structure

Dual nature of radiation

X-rays

Nuclear physics

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